

Analogy

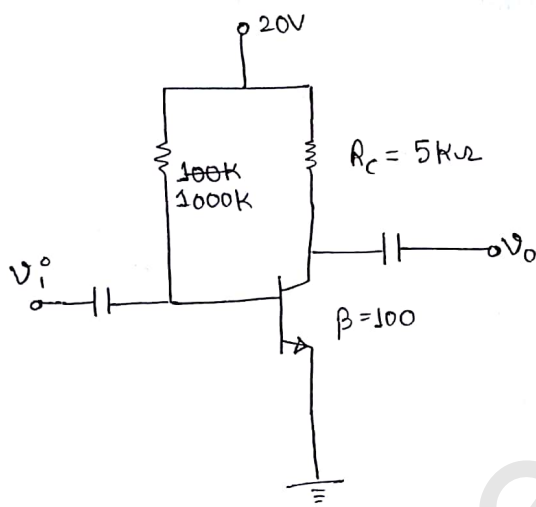
15 July 2017

Amplifier

Amplifier = Amplitude + Magnifier

Never is not amplifier bcz i/p power = o/p power

Q



$$-20 + 1000I_B + V_{BE} = 0$$

$$I_B = 19.3 \mu A$$

$$I_B \approx 20 \mu A$$

$$I_C = 2 \text{ mA}$$

$$V_{CE} = 20 - 5 \times 2 \\ = 10$$

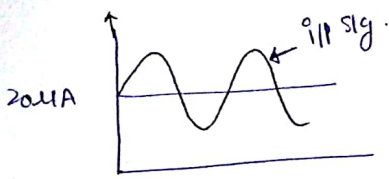
$$V_{BE} = 0.7 = 700 \text{ mV}$$

$$I_B = 20 \mu A$$

$$I_C = 2 \text{ mA}$$

$$V_{CE} = 10 \text{ V}$$

what is small sig and large sig.



$$i_B = 1 \mu A \sin \omega t$$

if i_{ip} sig $1 \mu A$
 $2 \mu A$
 $3 \mu A$
 then called

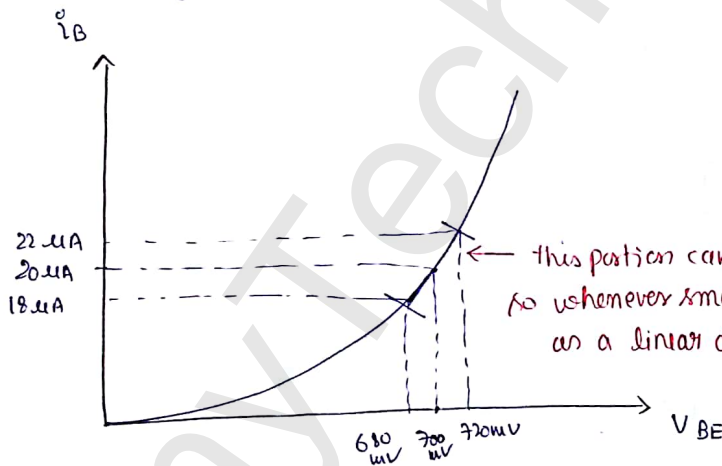
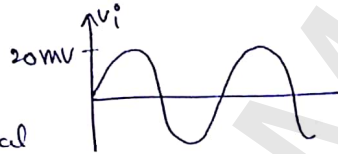
Small sig.

if i_{ip} sig is comparable to $20 \mu A$
 then called large sig.

Small sig Analysis in T_{BE} linear char assume $\frac{\partial i_B}{\partial V_{BE}} \approx \frac{1}{\beta}$ (Benefit)

let $V_i = 20 \text{ mV} \sin \omega t$

give rise to the sinusoidal
 Base (ac current) of $2 \mu A$



this portion can be used as linear.
 so whenever small sig tx. can be used
 as a linear device.

let us assume that change in i_B due to change in V_{BE} , change in i_B is

$$\Delta i_B = \pm 2 \mu A$$

so change in i_C

$$\Delta i_C = \beta \Delta i_B = 100 \times \pm 2 \mu A$$

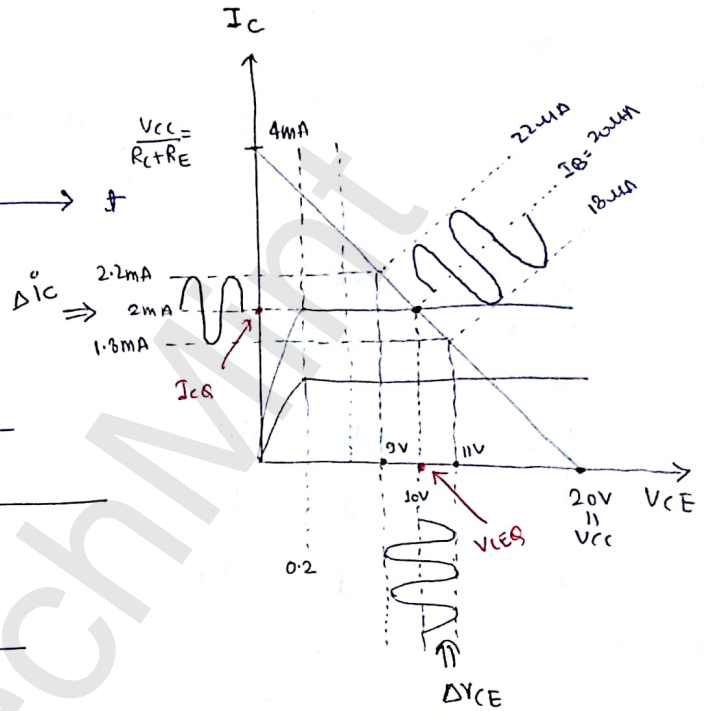
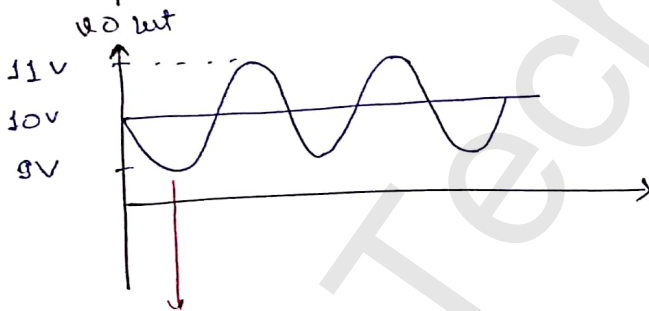
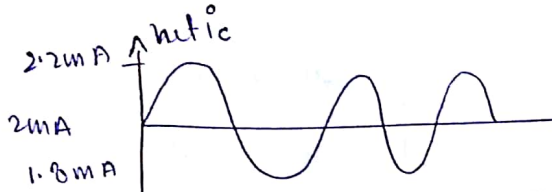
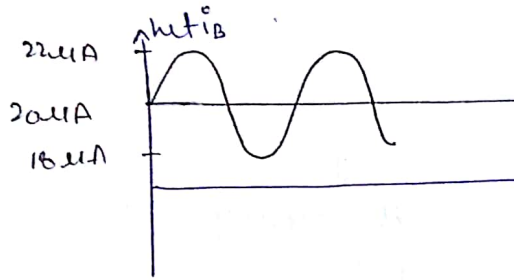
$$= \pm 0.2 \text{ mA}$$

$$V_o = V_{ce} = V_{cc} - i_c R_c$$

$$\Delta V_o = 0 - \Delta i_c R_c \rightarrow \text{greater the } R_c, \text{ greater the gain, so for higher gain, } R_c \text{ should be high.}$$

$$\Delta V_o = -(\pm 0.2 \text{ mA}) \times 5 \text{ K}$$

$$\Delta V_o = \mp 1 \text{ V}$$



CE is 180° phase shift due to above $\Delta V_o = \mp 1 \text{ V}$

but the o/p will be don't contain dc. it will contain pure a.c of $\pm 1 \text{ volt}$ variation.

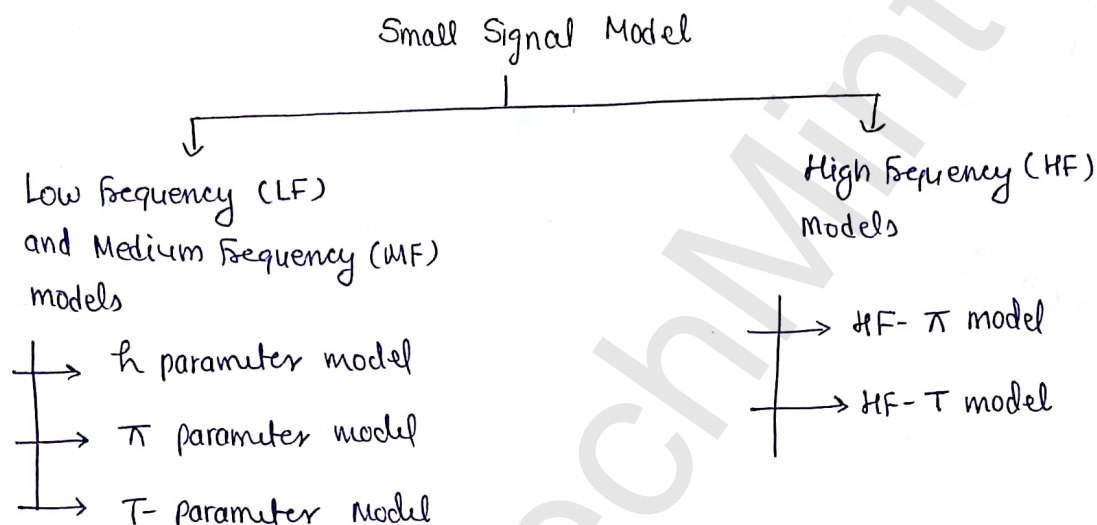
ss we applied i/p voltage of $20 \text{ mV} \sin \omega t$ and o/p we are getting as of $1 \text{ V} \sin \omega t$

$$\frac{1000 \text{ mV}}{20 \text{ mV}} = 50 \text{ times}$$

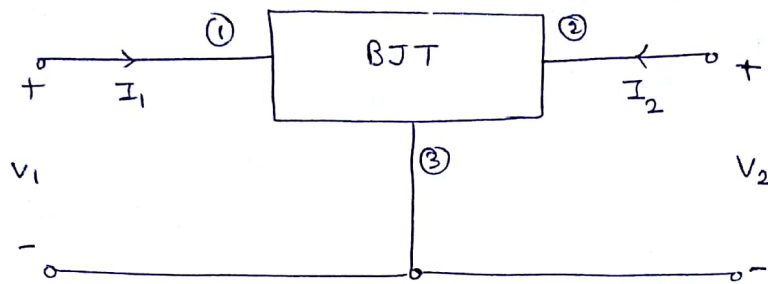
o/p is 50 times greater than i/p. //

Analysis of small signal amplifier

In the analysis of small sig Amplifier transistor behave as a ~~non~~-linear element and it is replaced with an equivalent ckt known as equivalent model ckt.



Hybrid - Parameter model



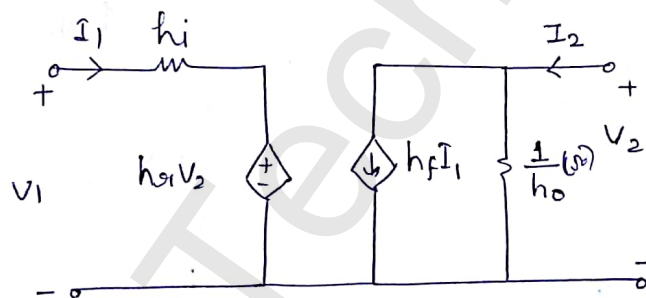
$$V_1 = h_{11} I_1 + h_{12} V_2$$

$$V_1 = h_i I_1 + h_r V_2$$

$$I_2 = h_{21} I_1 + h_{22} V_2$$

$$I_2 = h_f I_1 + h_o V_2$$

Conversion formulae:



I. Common collector parameters in terms of common emitter parameters

$$h_{fc} = -(1 + h_{fe})$$

$$h_{ic} = h_{ie}$$

$$h_{oc} = h_{oe}$$

$$h_{sic} = 1 - h_{sre} \approx 1$$

II. CB parameters in terms of CE parameters

$$h_{fb} = \frac{-h_{fe}}{1+h_{fe}} \text{ (once asked in object)}$$

$$h_{ob} = \frac{h_{oe}}{1+h_{fe}}$$

$$h_{ib} = \frac{h_{ie}}{1+h_{fe}}$$

$$h_{rb} = \frac{h_{ie}h_{oe}}{1+h_{fe}} - h_{re}$$

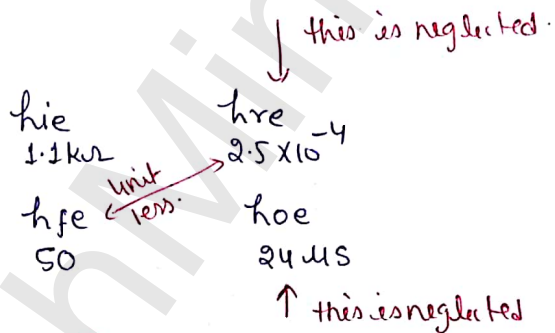
Standard CE parameters:

$$h_{fe} = 50$$

$$h_{ie} = 1.1 \text{ k}\Omega$$

$$h_{oe} = 24 \mu\text{S}$$

$$h_{re} = 2.5 \times 10^{-4}$$

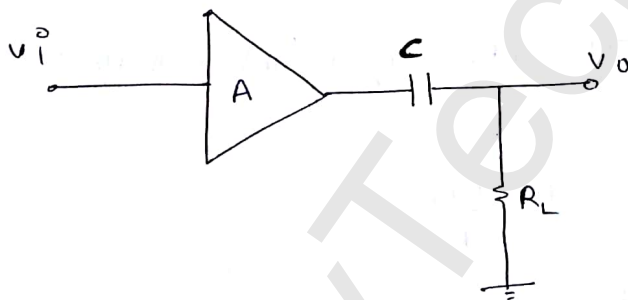


<u>CE to CB</u>	<u>CB to CE</u>	<u>CE to CC</u>
$h_{ib} = \frac{h_{ie}}{1+h_{fe}}$	$h_{ie} = \frac{h_{ib}}{1+h_{fb}}$	$h_{ic} = h_{ie}$
$h_{rb} = \frac{h_{ie}h_{oe} - h_{re}}{1+h_{fe}}$	$h_{re} = \frac{h_{ib}h_{ob} - h_{rb}}{1+h_{fb}}$	$h_{rc} \approx 1$
$h_{fb} = \frac{-h_{fe}}{1+h_{fe}}$	$h_{fe} = \frac{-h_{fb}}{1+h_{fb}}$	$h_{fc} = -(1+h_{fe})$
$h_{ob} = \frac{h_{oe}}{1+h_{fe}}$	$h_{oe} = \frac{h_{ob}}{1+h_{fb}}$	$h_{oc} \approx h_{oe}$

Medium Frequency AC Analysis

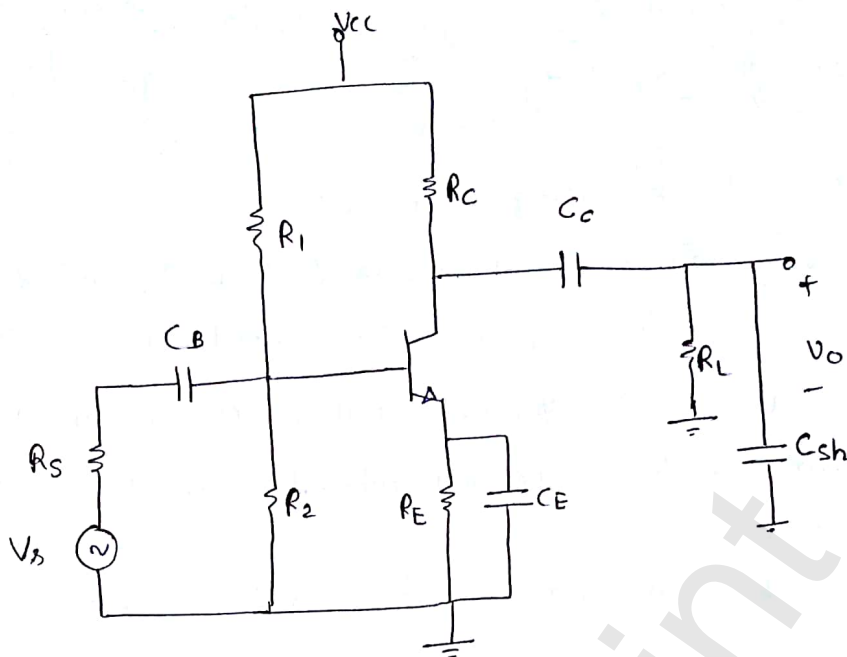
Procedure to Analyse amp^r ckt

- Step ① Identify the BJT config in the ckt.
- ② Convert the given ckt into medium freq^c ac equivalent ckt by replacing large capacitances (C_E , C_B , C_C) by short ckt and small capacitances (C_{sh} , C_{π} , C_{μ}) by open ckt. and deactivate all the dc sources. (dc batteries should be grounded and dc current source should be open ckt)
- ③ Using appropriate model calculate the desired values.



RC coupled amplifier
means
load is sensitive → caps^c is used for connecting load to amp^r.

We will use a general ckt (Self Bias BJT ckt to bias BJT in active region) to explain all above



- Self bias ckt is used to operate BJT in active region and to maintain I_c stable

can't remove R_E bcz $S = 1 + \frac{R_{th}}{R_E}$

if $R_E = 0$ $S = \infty$ unstable

- Bypass cap^c C_E prevents decrease in voltage gain.
- Blocking cap^c C_B and coupling cap^c C_c provides dc isolation to the biasing ckt, so that no dc current flows out of the ckt and no dc current enters the biasing ckt from outside.
- C_B , C_c and C_E are large capacitances {in μF range} bcz they should act as short ckt for ac signal

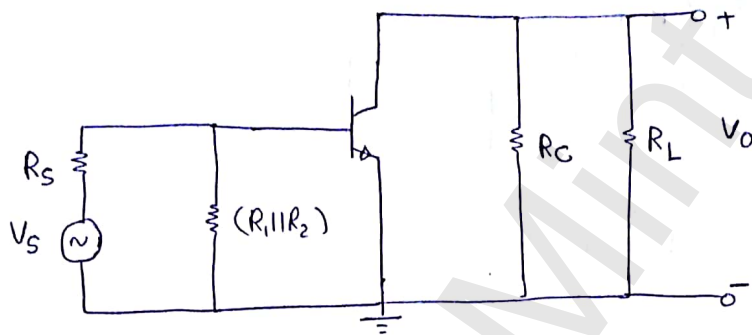
$$X_C = \frac{1}{\omega C} \approx 0$$

- C_{sh} (shunt cap^a) is connected to control bandwidth of amp^r. it is a small capacitance of (pF range) and act as open ckt for dc sig.

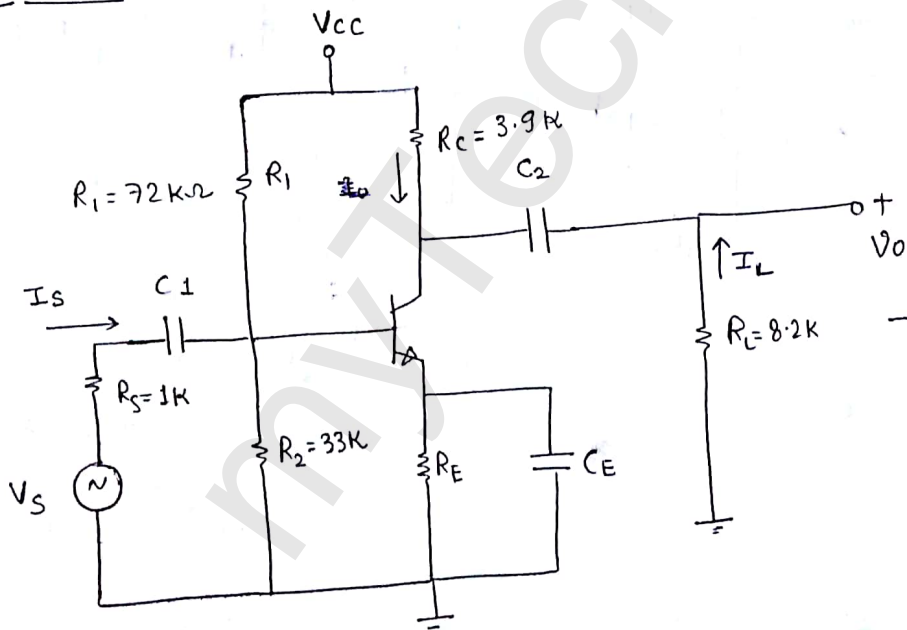
o In ac analysis dc supply (V_{CC}) will be disabled or replaced with short ckt.

MF Ac equivalent ckt

If we have to do ac analysis by default we do MF ac analysis. medium freq^c



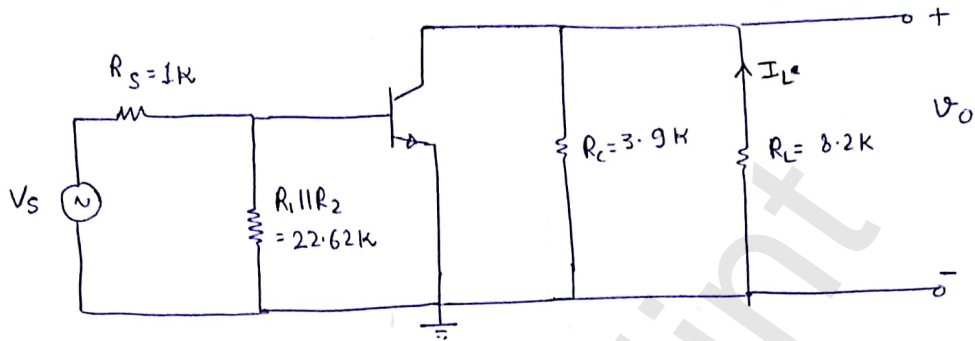
Question



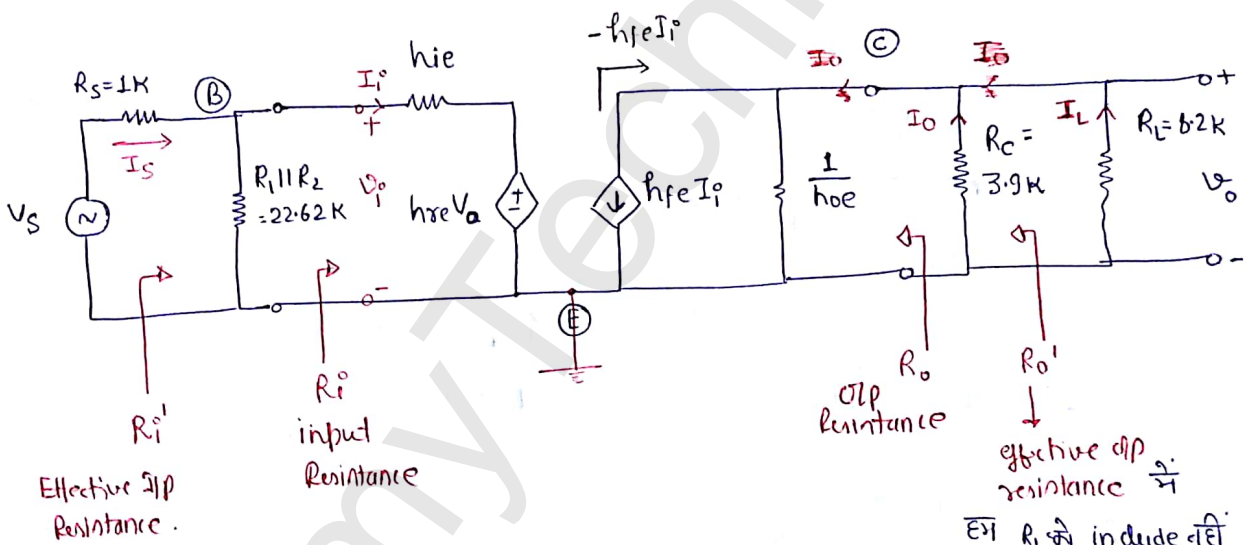
In the amp^r ckt shown Tx has $h_{fe} = 75$, $h_{ie} = 2.5k$, $h_{re} = 2 \times 10^{-4}$, $h_{oe} = 20 \mu$
 calculate voltage gain $\left\{ \frac{V_o}{V_s} \right\}$, current gain $\left(\frac{I_o}{I_s} \right)$, \uparrow p and \downarrow p resistors.

Solution :- First identify BJT config.

Draw AC equivalent ckt



Replace BJT with its model



Current gain

$$A_I = \frac{I_L}{I_i}$$

we will use current division rule

Dont remember formula

$$I_L = \frac{(R_c \parallel \frac{1}{h_{oe}})}{(R_c \parallel \frac{1}{h_{oe}}) + R_L} (h_{fe} I_i) = \frac{(3.91150)}{(3.91150) + 8.2} \times h_{fe}$$

$$= \frac{3.62}{3.62 + 8.2} \times 75 = 22.92$$

$$\frac{I_L}{I_i} = A_i = \left(\frac{R_c \parallel \frac{1}{h_{oe}}}{R_c \parallel \frac{1}{h_{oe}} + R_L} \right) h_{fe} = \frac{24.39}{24.39} = 1$$

② Input Resistance

$$R_i^o = \frac{V_i^o}{I_i^o}$$

KVL in loop @

$$V_i^o = h_{ie} I_i + h_{re} V_o$$

$$V_i^o = h_{ie} I_i + h_{re} (-I_L R_L)$$

$$V_i^o = h_{ie} I_i - h_{re} R_L I_L$$

$$\frac{V_i^o}{I_i^o} = h_{ie} - h_{re} R_L \cdot \frac{I_L}{I_i}$$

$$R_i^o = h_{ie} - h_{re} R_L \cdot A_i$$

$$= 2.5k - 2 \times 10^{-4} \times 8.2k \times 24.39 \times 22.92$$

$$R_i^o = 2.46k$$

③ voltage gain

$$A_v = \frac{V_o}{V_i} = \frac{-I_L R_L}{V_i} = -\frac{A_i I_i R_L}{V_i} = -\frac{A_i R_L}{R_i}$$

$$A_v = -\frac{22.92}{2.46} \times 8.2 = -76.04$$

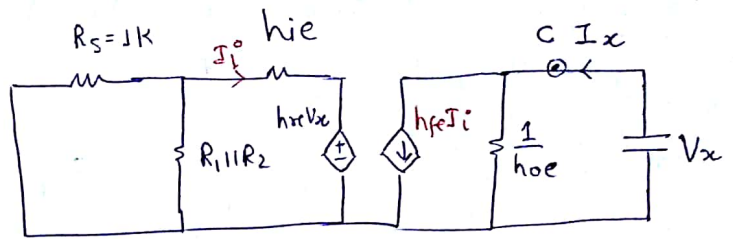
-ve sign shows 180° phase shift

4. O/P resistance (R_o)

KCL:

$$I_x = h_{fe} I_i + \frac{V_x}{\frac{1}{h_{oe}}}$$

$$I_x = h_{fe} I_i + V_x h_{oe} \quad \text{--- (1)}$$



KVL in i/p loop

$$R_s' I_i + h_{ie} I_i + h_{re} V_x = 0$$

$$I_i = \frac{-h_{re} V_x}{R_s' + h_{ie}}$$

putting above value in eqⁿ (1)

$$I_x = h_{fe} \left(\frac{-h_{re} V_x}{R_s' + h_{ie}} \right) + h_{oe} V_x$$

$$\boxed{\frac{I_x}{V_x} = \frac{1}{R_o} = Y_o = h_{oe} - \frac{h_{fe} h_{re}}{R_s' + h_{ie}}}$$

$$\begin{aligned} R_s' &= R_s \parallel R_1 \parallel R_2 \\ &= 1 \parallel 22.62 \\ &= 0.96 \end{aligned}$$

$$Y_o = 20 \times 10^{-6} - \frac{25 \times 2 \times 10^{-4}}{(2.5 + 0.96) \times 10^3}$$

$$Y_o = 1.566 \times 10^{-5}$$

$$R_o = 63.837 \text{ k}\Omega$$

5. R_i'

$$\begin{aligned} R_i' &= R_i \parallel R_2 \parallel R_1 = 2.22 \text{ k}\Omega \\ &= 2.46 \parallel 22.62 \end{aligned}$$

6. R_o'

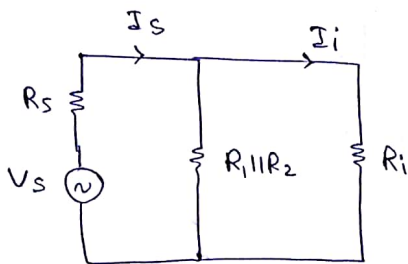
$$\begin{aligned} R_o' &= R_o \parallel R_c = 3.675 \text{ k}\Omega \\ &= 63.837 \parallel 3.9 \end{aligned}$$

आज लिंगे बि i/p and o/p resistance के पूछा है तो R_i' and R_o' find करनी है

7. Current gain ($A_{Is} = \frac{I_L}{I_s}$)

$$A_{Is} = \frac{I_L}{I_s} = \frac{I_L}{I_i} \cdot \frac{I_i}{I_s}$$

$$A_{Is} = A_I \cdot \frac{I_i}{I_s}$$



$$I_i = \frac{R_1 || R_2}{R_1 || R_2 + R_i} I_s$$

$$A_{Is} = A_I \cdot \frac{R_1 || R_2}{(R_1 || R_2) + R_i}$$

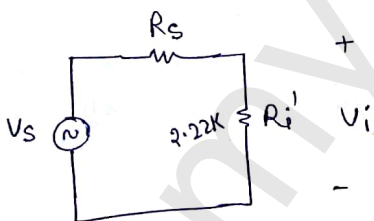
$$= \frac{22.92 \times 22.62}{22.62 + 2.46} = 20.67$$

8. voltage gain

$$A_{Vs} = \frac{V_o}{V_s} = \frac{V_o}{V_i} \cdot \frac{V_i}{V_s}$$

$$R_i' = 2.22k$$

$$A_{Vs} = A_v \cdot \frac{V_i}{V_s}$$



$$V_i = \frac{R_i'}{R_i' + R_s} \cdot V_s$$

$$\Rightarrow \frac{V_i}{V_s} = \frac{R_i'}{R_i' + R_s} = \frac{2.22}{2.22 + 1} = 0.689$$

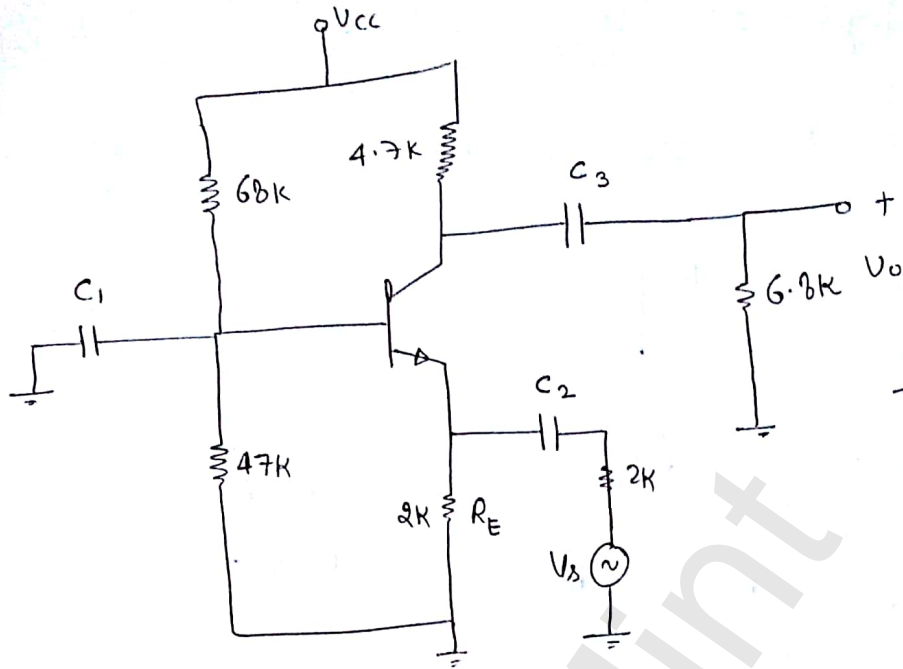
$$A_{Vs} = A_v \cdot \frac{R_i'}{R_i' + R_s}$$

$$A_{Vs} = -76.4 \times 0.689$$

$$= -52.67$$

↑
overall gain is less than ^{only} BJT gain.

Question



In the ckt shown above $h_{fe} = 50$ $h_{ie} = 1.2k$, $h_{re} = 2.5 \times 10^{-4}$ $h_{oe} = 24 \mu\Omega$
 calc voltage gain i/p and o/p resistance

Solⁿ

Common Base

$$h_{fb} = - \frac{h_{fe}}{1 + h_{fe}} = \frac{-50}{1 + 50} = -0.98$$

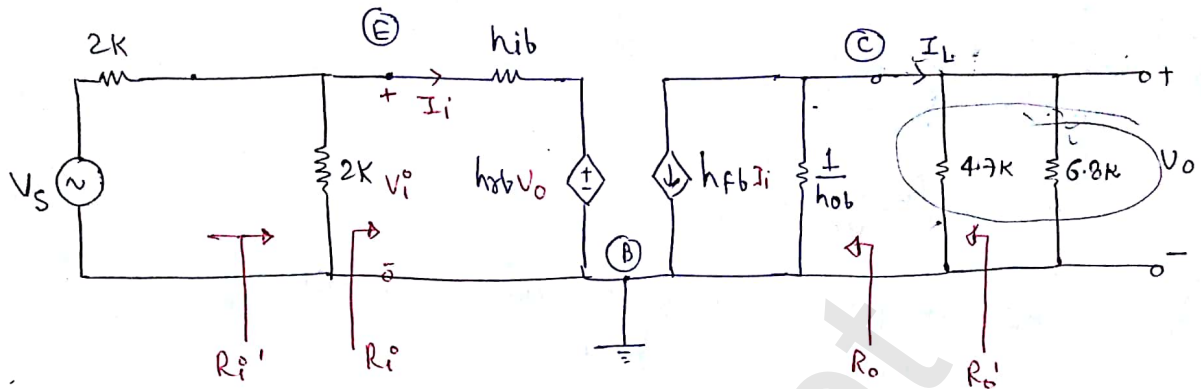
$$h_{ib} = \frac{h_{ie}}{1 + h_{fe}} = \frac{1.2}{51} = 23.52 \Omega$$

$$h_{rb} = \frac{1.2 \times 10^{-3} \times 24 \times 10^{-6}}{1 + 50} - 2.5 \times 10^{-4} = 3.24 \times 10^{-4}$$

$$h_{ob} = \frac{24 \times 10^{-6}}{51} = 0.47 \mu\Omega$$

Ac equivalent

ASK? why i am not taking the load current, the current across 6.8k



$$R_L' = 4.7 \parallel 6.8 = 2.78 \text{ k}\Omega$$

1. Current gain

$$A_I = \frac{I_L}{I_i}$$

KCL:

$$I_L = \frac{1}{\frac{1}{h_{ob}} + R_L'} (-h_{fb} I_i)$$

~~$V_o = I_L R_L'$~~
 $V_o = I_L R_L'$

$$\frac{I_L}{I_i} = \frac{1}{\frac{1}{0.47 \times 10^{-6}} + 2.78} (-0.98) \approx 0.98$$

2. Input resistance

$$R_i = \frac{V_i}{I_i}$$

KVL:

$$V_i = h_{ib} I_i + h_{ob} V_o$$

$$= h_{ib} I_i + h_{ob} (I_L R_L')$$

$$R_i = \frac{V_i}{I_i} = h_{ib} + h_{ob} A_I R_L' = 23.4 \Omega = 24.4 \Omega$$

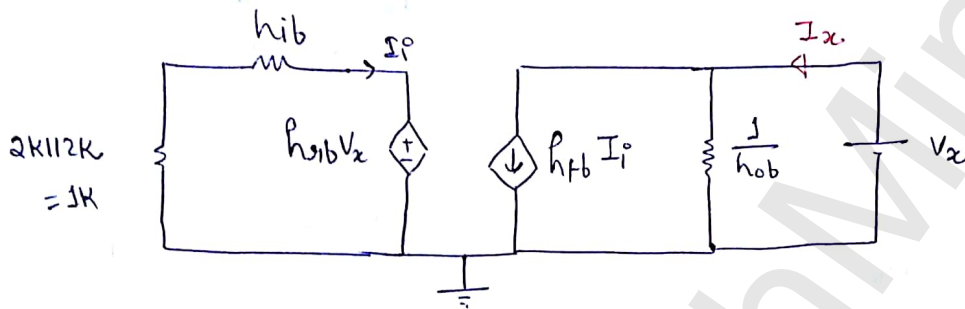
voltage gain ($A_v = \frac{V_o}{V_i}$)

$$A_v = \frac{V_o}{V_i} = \frac{I_L R_L'}{V_i}$$

$$A_v = \frac{A_T I_i R_L'}{V_i}$$

$$A_v = \frac{A_T R_L'}{R_i} = \frac{0.98 \times 2.78 \times 10^3}{24.4 \Omega} = 111.66$$

output resistance



$$I_x = h_{fb} I_i + V_x h_{ob} \rightarrow \textcircled{1}$$

KVL in i_p loop

$$1k I_i + h_{ib} I_i + h_{ob} V_x = 0$$

$$I_i = \frac{-V_x h_{ob}}{h_{ib} + 1k}$$

$$I_x = h_{fb} \left(\frac{-V_x \cdot h_{ob}}{h_{ib} + 1k} \right) + h_{ob} V_x$$

$$\frac{1}{R_o} = \frac{I_x}{V_x} = h_{ob} - \frac{h_{fb} h_{ob}}{h_{ib} + 1k}$$

$$0.47 \times 10^{-6} - \frac{(0.98)(3.24 \times 10^{-4})}{23.52 + 1000}$$

$$R_o = 1201.68 \text{ k}\Omega$$

(very high)

$$= 1.28 \text{ M}\Omega$$

$$R_i' = R_i \parallel 2k = 24.4k \parallel 2000 = 24.1k$$

$$R_o' = R_o \parallel R_c = R_o \parallel 4.7k \\ = 1.2M \parallel 4.7k \approx 4.7k$$

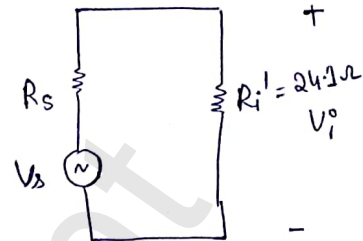
voltage gain

$$A_{vs} = \frac{V_o}{V_s} = \frac{V_o}{V_i} \cdot \frac{V_i}{V_s} = A_v \cdot \frac{V_i}{V_s}$$

$$A_{vs} = A_v \cdot \frac{R_i'}{R_i' + R_s}$$

$$= 111.6 \times \frac{24.1}{24.1 + 1000}$$

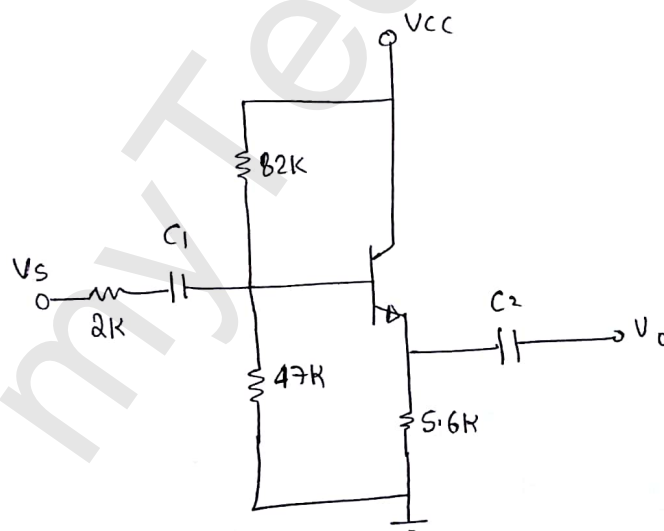
$$A_{vs} = 1.328$$



$$\frac{V_i'}{V_s} = \frac{R_i'}{R_i' + R_s}$$

||

In the ckt shown below BJT has $\beta_{fe} = 50$ $h_{ie} = 1.5k$ $h_{re} = 2 \times 10^{-4}$
 $h_{oe} = 22 \mu s$ calc voltage gain i_{ip} and o_p resistance.

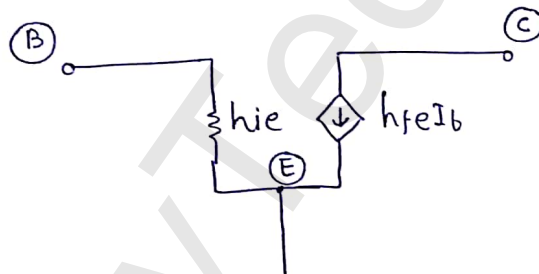
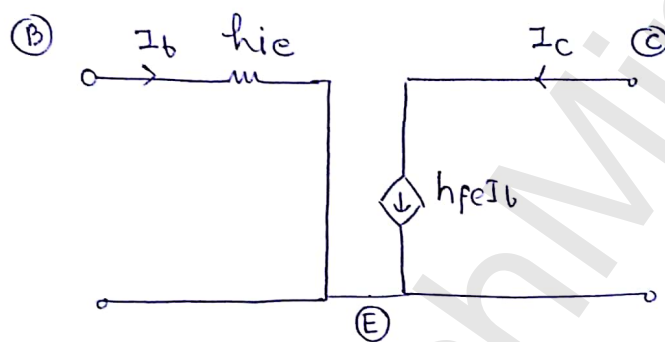


H parameter are configuration based For different config CE, CB, CC we need conversion formulae ~~and different ckt~~. so we use approximate h parameter - these we have just two parameters.

Approximate H-parameter of BJT Amplifier.

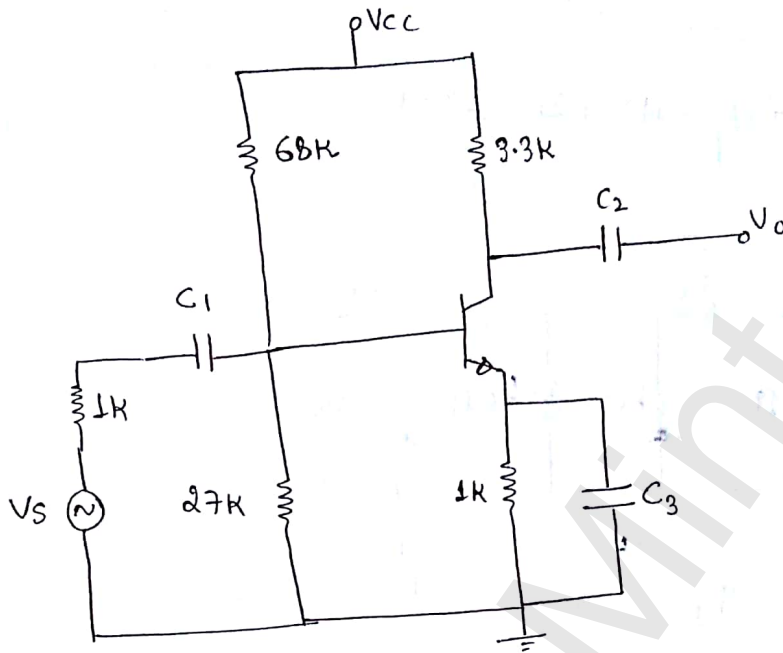
$$h_{re} \approx 0$$

$$h_{oe} \approx 0$$

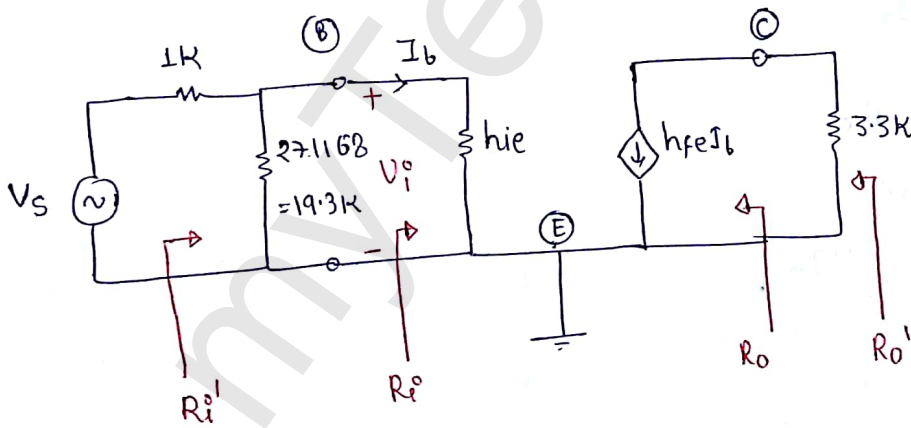


Now whatever configuration either CE, CC, CB we will just replace BJT by this and don't bother about h_{fc} or h_{ic} . values will not be exact i.e answers

Q In the amp^r ckt shown below Tx has $h_{fe} = 60$, $h_{ie} = 2K\Omega$ calc V_{out} gain $\frac{V_o}{V_s}$, i_{ip} and O_p resistance.



Solⁿ. CE config.
approximation



$$V_o = -h_{fe} I_b \times 3.3K \quad \text{--- (1)}$$

$$V_i = h_{ie} I_b \quad \text{--- (2)}$$

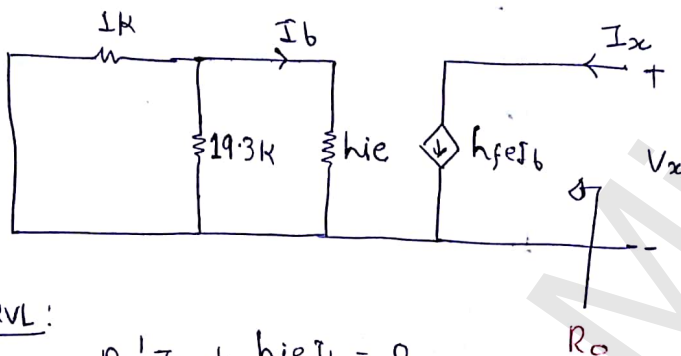
$$R_i = \frac{V_i}{I_b} = h_{ie}$$

If we are given h_{fe} and h_{ie} means use approximate ckt. if we are given h_{fe} , h_{ie} and h_{oe} then also use approximate ckt but add $\frac{1}{h_{oe}}$ resistance.

Voltage gain

$$A_v = \frac{V_o}{V_i} = \frac{-h_{fe} \times 3.3K}{h_{ie}}$$

$$R_i' = 19.3K \parallel h_{ie} = (19.3 \parallel 2) = 1.81K$$



KVL:

$$R_s' I_b + h_{ie} I_b = 0$$

$$(R_s' + h_{ie}) I_b = 0$$

$$\Rightarrow I_b = 0$$

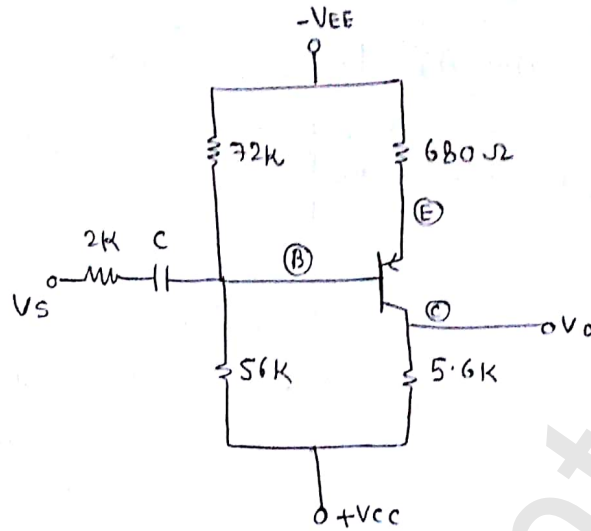
$$R_o = \frac{V_x}{I_x} = \frac{V_x}{0} = \infty$$

$$R_o' = R_o \parallel R_c$$

$$= \infty \parallel R_c$$

$$R_o' = R_c = 3.3K$$

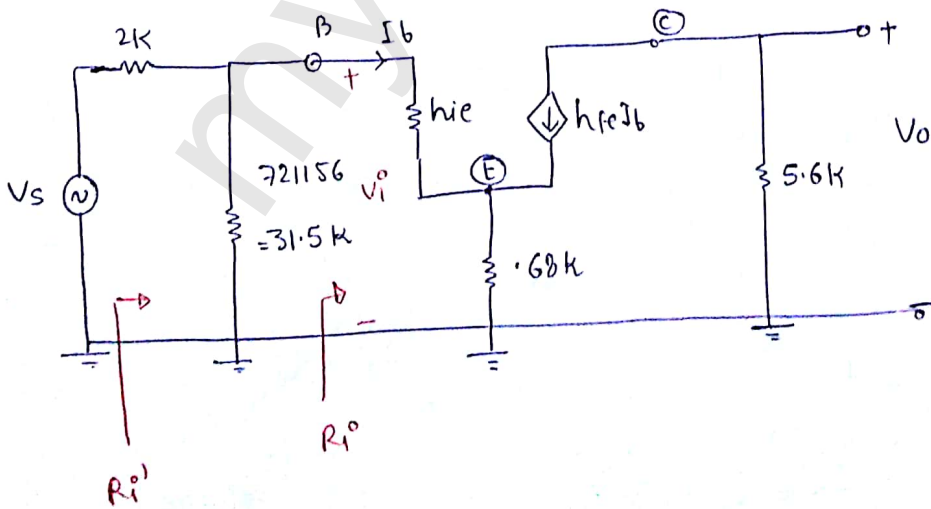
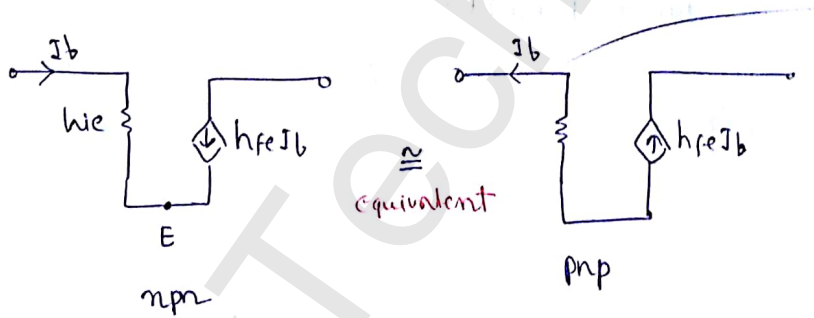
10



In the ckt shown below transistor has $h_{fe} = 50$ $h_{ie} = 1.5k\Omega$, Current gain, voltage gain, i/p resistance, o/p resistance.

Solⁿ

Either pnp or npn there will be no change in model.



$$V_o = I_b h_{ie} + (1+h_{fe}) I_b \cdot R_E$$

$$\Rightarrow \frac{V_o}{I_b} = \boxed{R_i = h_{ie} + (1+h_{fe}) R_E}$$

If C_E is present

$$R_i = h_{ie}$$

If C_E is absent

$$R_i = h_{ie} + (1+h_{fe}) R_E$$

$$V_o = -h_{fe} I_b \times 5.6K$$

$$\therefore A_v = \frac{V_o}{V_i} = \frac{-h_{fe} \times 5.6K}{h_{ie} + (1+h_{fe}) R_E}$$

→ If C_E present this term will be removed.

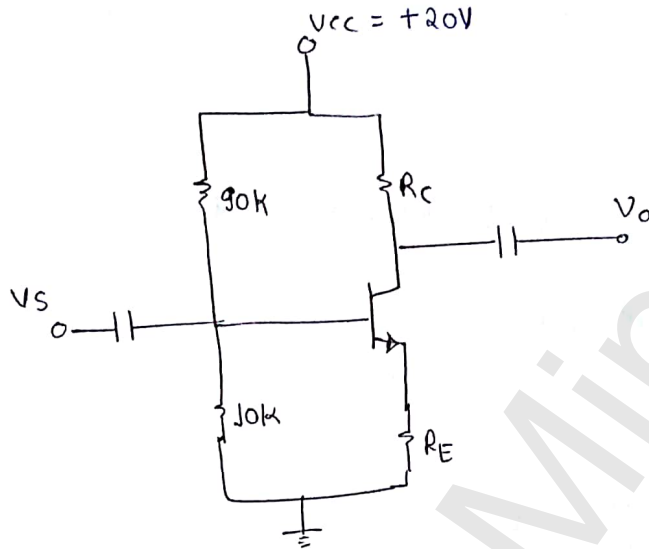
Q1. What is the effect on i_p resistance when the cap^c is removed accidentally & what is the effect on voltage gain.

Q2. What is the effect on i_p resistance in cap^c is connected across emitter resistance.

10

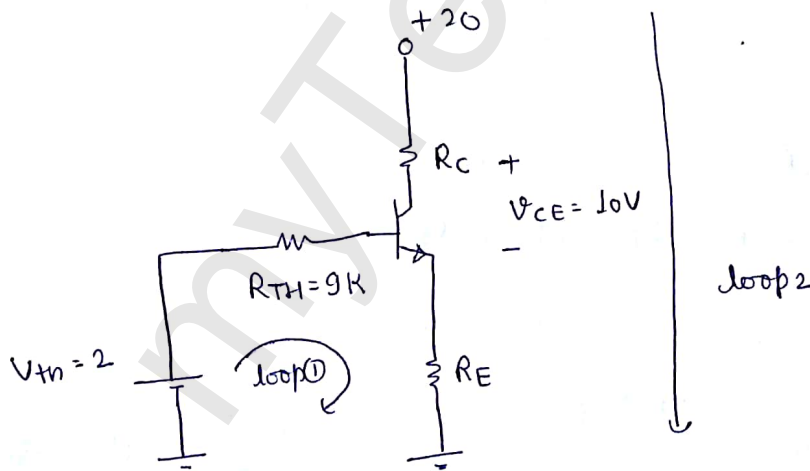
V_{CC}
0

In the circuit shown below transistor has large β $V_{BE} = 0.7$, $V_{CEQ} = \frac{V_{CC}}{2}$
 Calc voltage gain $\frac{V_o}{V_s}$



Solⁿ

We are given no h parameter and we are also not given R_c & R_E
 So 1st find R_c and R_E



β is very large

$$I_B \approx 0$$

$$I_C \approx I_E$$

KVL in loop ①

$$-V_{th} + I_B R_{th} + V_{BE} + I_C R_E = 0$$

$$\Rightarrow I_C = \frac{V_{th} - V_{BE}}{R_E} = \frac{1.3}{R_E}$$

KVL in loop 2

$$-20 + R_C I_C + 10 + I_C R_E = 0$$

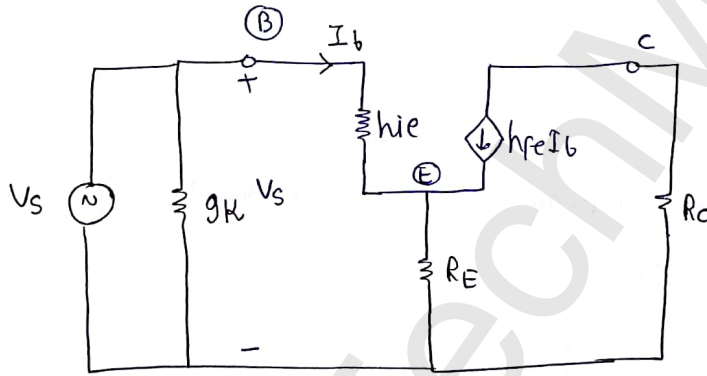
$$(R_C + R_E) I_C = 10$$

$$(R_C + R_E) \times \frac{1.3}{R_E} = 10$$

$$\Rightarrow \frac{R_C}{R_E} = 6.69$$

Voltage gain is found for ac eq^v ckt not for dc

so we will draw ac eq^v ckt



$$V_o = -h_{fe} I_b R_C \quad \text{--- (1)}$$

$$V_s = h_{ie} I_b + (1+h_{fe}) I_b R_E \quad \text{--- (2)}$$

$$A_{v_s} = \frac{V_o}{V_s} = \frac{-h_{fe} R_C}{h_{ie} + (1+h_{fe}) R_E}$$

$$A_{v_s} \approx \frac{-h_{fe} R_C}{(1+h_{fe}) R_E}$$

bcz we don't know h_{ie}
since $(1+h_{fe}) R_E$ is $\gg h_{ie}$

$$A_{v_s} \approx \frac{-h_{fe} R_C}{h_{fe} R_E} = -\frac{R_C}{R_E}$$

$$A_{vs} = -\frac{R_c}{R_E}$$

but if V_o is across the resistor R_L आर का है, तो

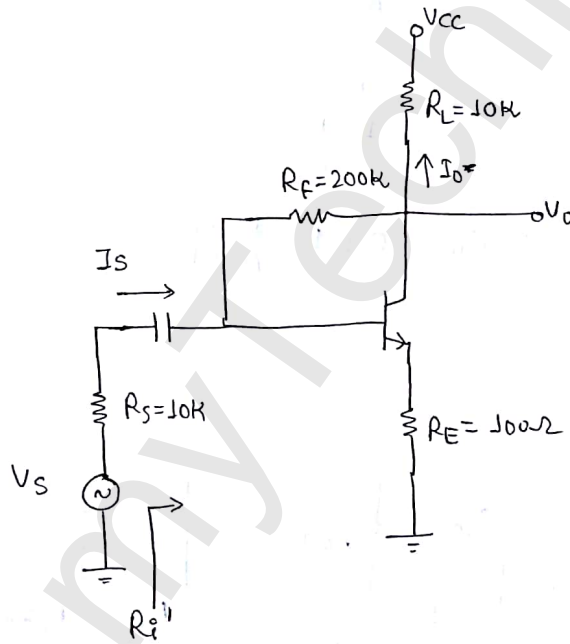
$$A_{vs} = -\frac{(R_c || R_L)}{R_E}$$

*** Remb^y directly for gate.

$$A_{vs} = -\frac{R_c}{R_E} = -6.69$$

Answer,

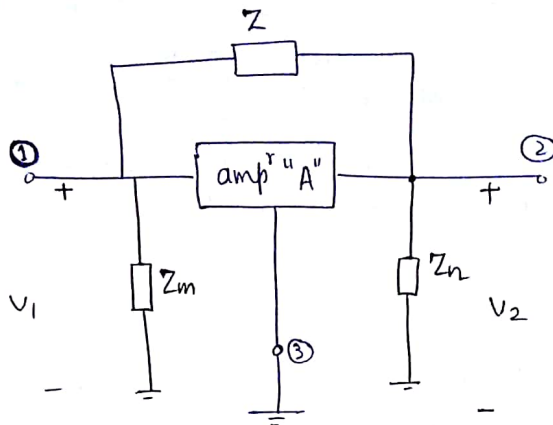
NO



For the ckt shown below BJT has $h_{ie} = 1.1k\Omega$, $h_{fe} = 50$ calc $A_{Is} = \frac{I_o}{I_s}$

$$A_{vs} = \frac{V_o}{V_s} \text{ and } R_i'$$

Miller's Theorem! -



$$Z_m = \frac{Z}{1-A}$$

$$Z_n = \frac{Z}{1-\frac{1}{A}}$$

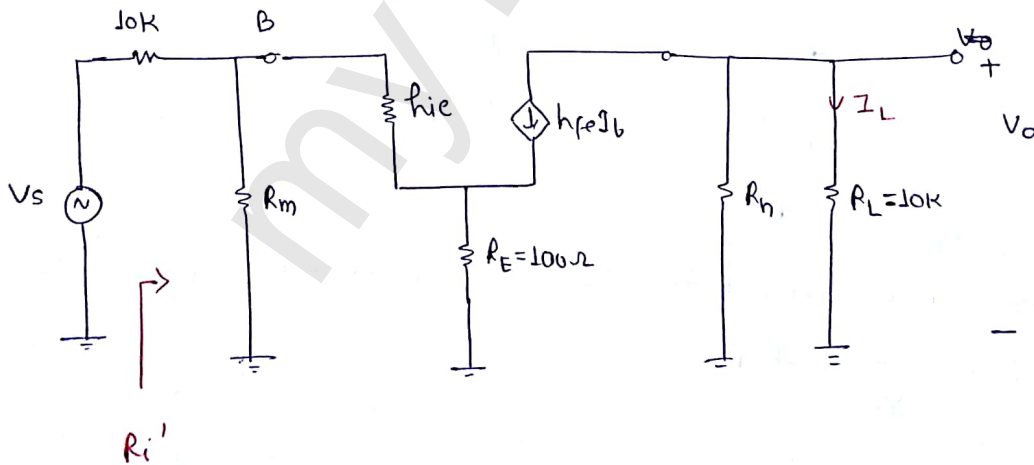
A = open loop gain
(i.e. without considering the effect of Z)

$$R_m = \frac{R}{1-A}$$

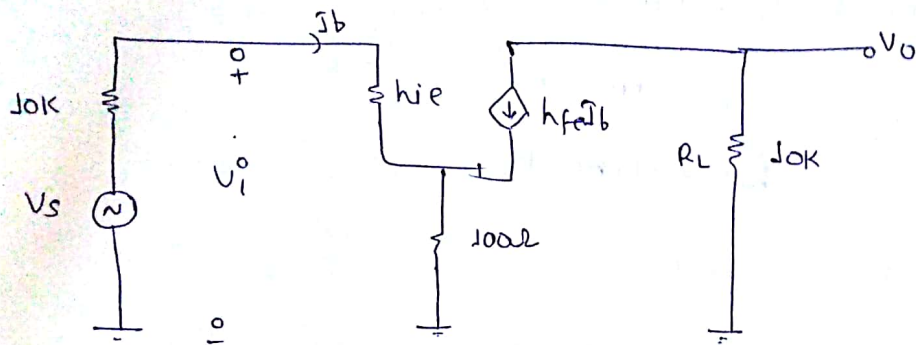
$$R_n = \frac{R}{1-\frac{1}{A}}$$

$C_m = (1-A)C$	$C_n = C \left(1 - \frac{1}{A}\right)$
----------------	--

Solⁿ



To calc open loop gain R_m & R_n are not considered i.e feedback is neglected



$$V_o = -h_{fe} I_b R_L$$

$$V_i = h_{ie} I_b + (1+h_{fe}) I_b R_E$$

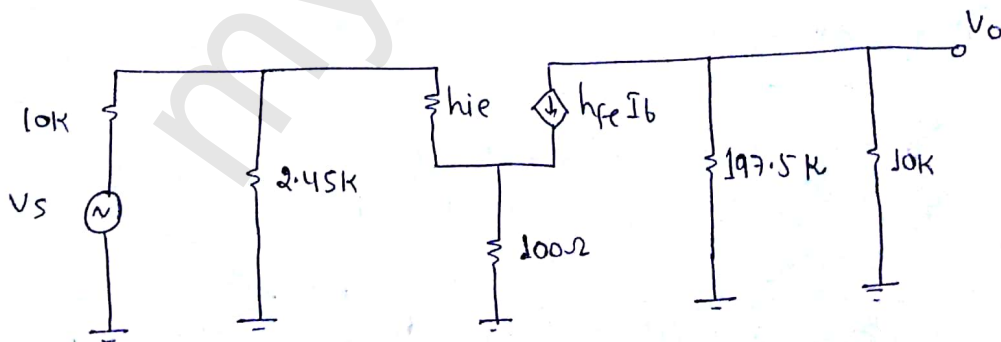
voltage gain without feedback.

$$A = \frac{V_o}{V_i} = \frac{-h_{fe} R_L}{h_{ie} + (1+h_{fe}) R_E} = -80.6$$

Now calc R_m & R_n

$$R_m = \frac{200k}{1-A} = \frac{200k}{81.6} = 2.45k$$

$$R_n = \frac{200k}{1 - \frac{1}{A}} \approx 197.5k$$



Now finding $A_{v_s} = \frac{V_o}{V_s}$

$$V_o = -h_{fe} I_b (R_n \parallel 10k)$$

$$V_i = h_{ie} I_b + (1+h_{fe}) R_E I_b$$

$$\frac{V_o}{V_i} = A_{vf} = \frac{-h_{fe} (R_n \parallel 10k)}{h_{ie} + (1+h_{fe}) R_E}$$

$$A_{vf} = -76.7$$

$$R_i = \frac{V_i}{I_b} = h_{ie} + (1+h_{fe}) R_E = 6.2k\Omega$$

$$R_i' = R_n \parallel 6.2k = 1.75k \quad \text{Ans}$$

From op ckt

$$I_L = \frac{R_n}{R_L + R_L} (-h_{fe} I_b)$$

$$\frac{I_L}{I_b} = -47.6$$

Current gain

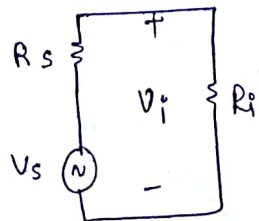
$$A_{is} = \frac{I_L}{I_s} = \frac{I_L}{I_b} \cdot \frac{I_b}{I_s} = (-47.6) \times \frac{R_m}{R_m + R_i}$$

$$A_{is} = -13.48$$

$$A_{vs} = \frac{V_o}{V_s} = \frac{V_o}{V_i} \cdot \frac{V_i}{V_s} = -76.7 \times \frac{R_i'}{R_i' + R_s}$$

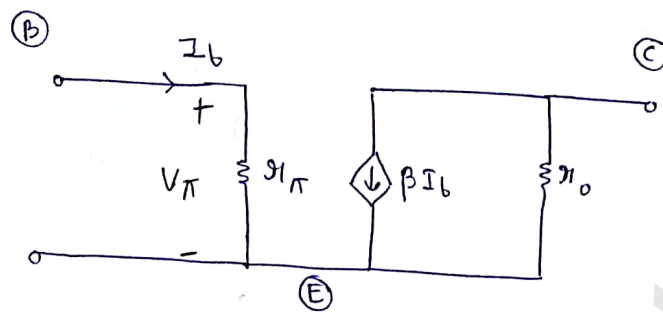
$$A_{vs} = -11.4$$

-ve sign is indicating gain.



$$\frac{V_i'}{V_s} = \frac{R_i'}{R_i' + R_s}$$

π Model generally used for CE
(CE-Model)



comparing with approximate h-parameter model:

$$g_{\pi} = h_{ie}$$

$$\beta = h_{fe}$$

$$g_o = \frac{1}{h_{oe}}$$

π parameter

$$\beta \quad g_{\pi} \quad g_m \quad g_o$$

Calculation of π parameter

(I) g_m (Transconductance of BJT)

It is the rate of change of

$$g_m = \frac{\partial I_c}{\partial V_{BE}}$$

We have

$$V_{BE}/V_T$$

$$I_c = I_{c0} e^{V_{BE}/V_T}$$

$$\frac{\partial I_c}{\partial V_{BE}} \equiv \frac{I_{c0}}{V_T} e^{V_{BE}/V_T} = \frac{I_c}{V_T}$$

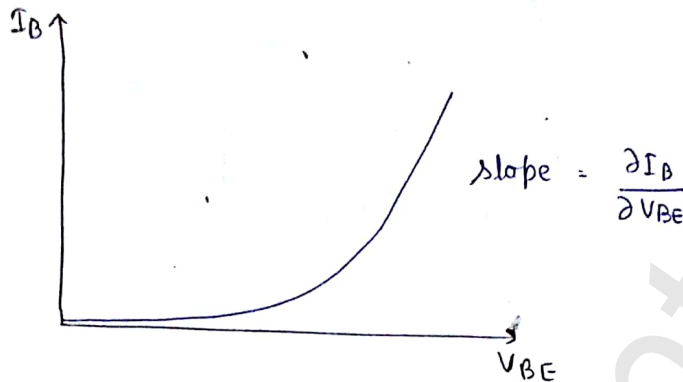
$$g_m = \frac{I_c}{V_T}$$

effective g_m can be

BJT	
g_m vs I_c	linear
g_m vs V_{BE}	exponential curve

$g_{i\pi}$

$g_{i\pi}$ is reciprocal of slope of i/p char of CE config.



$$g_{i\pi} = \frac{1}{\text{slope}} = \frac{\partial V_{BE}}{\partial I_B}$$

$$g_{i\pi} = \frac{\partial V_{BE}}{\partial I_B}$$

$$g_{i\pi} = \frac{\partial V_{BE}}{\partial I_C} \cdot \frac{\partial I_C}{\partial I_B}$$

$$g_{i\pi} = \frac{1}{g_m} \times \beta$$

$$g_{i\pi} = \frac{\beta}{g_m}$$

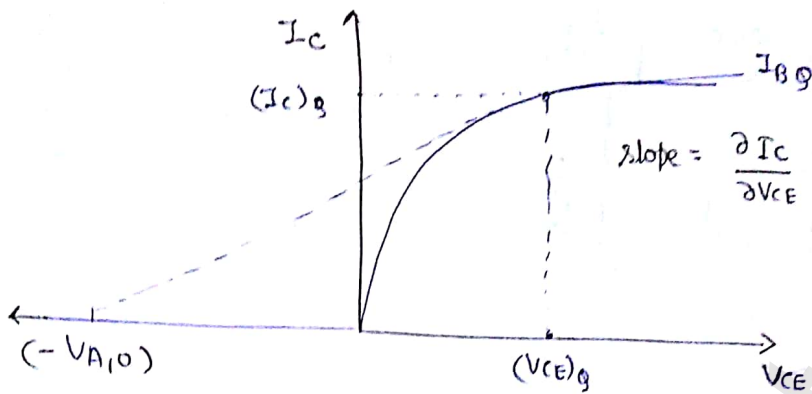
$$g_{i\pi} = \beta \times \frac{V_T}{I_C}$$

$$g_{i\pi} = \frac{\beta \times V_T}{\beta I_B}$$

$$g_{i\pi} = \frac{V_T}{I_B}$$

I_B - DC - Q point base current

r_{10} :- It is reciprocal of the slope of o/p char of CE configuration.



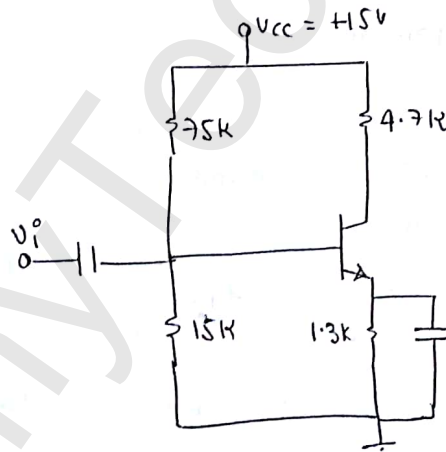
$$r_{10} = \frac{1}{\text{slope}} = \frac{\partial V_{CE}}{\partial I_C}$$

$$\Rightarrow r_{10} = \frac{V_{CEQ} + V_A}{I_{CQ}}$$

$V_A =$ Early voltage

If early voltage is not given $r_{10} = \infty$.

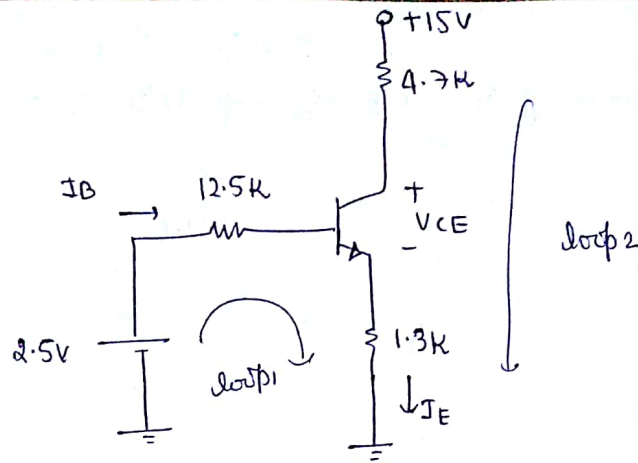
110



Qn - The ckt shown. Tx. has $\beta = 200$, $V_{BE} = 0.7V$ calc.

- ① operating point of BJT
- ② r_{10} parameter
- ③ voltage gain
- ④ i/p and o/p resistance, given early voltage = 80 volt.
- ⑤

Solⁿ



KVL in loop 1

$$-2.5 + 12.5kI_B + 0.7 + 1.3kI_E = 0$$

$$12.5kI_B + 201 \times 1.3kI_B = 2.5 - 0.7$$

$$I_B = \frac{1.8}{12.5k + 201 \times 1.3k} = 6.57 \mu A$$

$$I_C = 1.314 \text{ mA}$$

$$V_{CE} = 7.1 \text{ V}$$

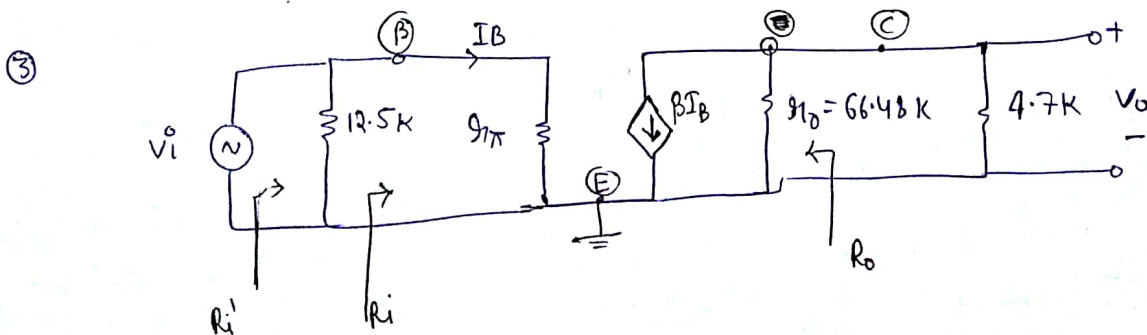
① operating point (7.1V, 1.314 mA)

② π parameter

$$g_m = \frac{I_C}{V_T} = \frac{1.314 \text{ mA}}{26 \text{ mV}} = 50 \text{ ms}$$

$$g_{\pi} = \frac{\beta}{g_m} = \frac{200}{50 \times 10^3} = 4 \text{ k}\Omega$$

$$g_o = \frac{V_{CE} + V_A}{I_C} = \frac{7.1 + 80}{1.314 \text{ mA}} = 66.48 \text{ k}\Omega$$

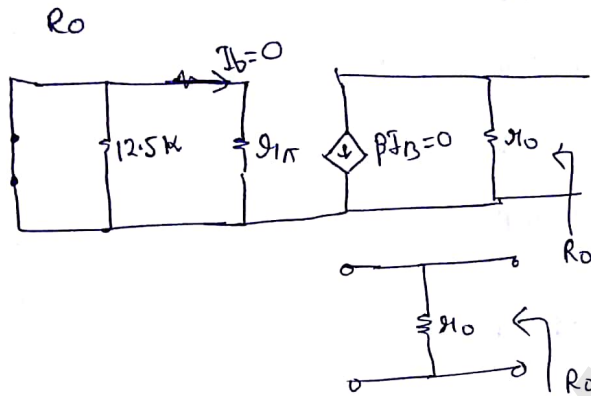


④ Input Resistance

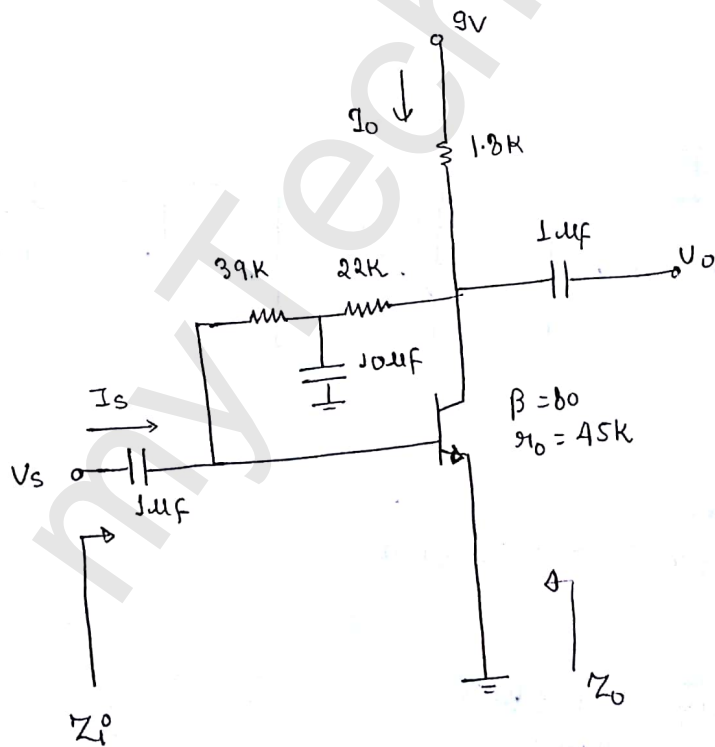
$$R_i' = \beta (12.5 \parallel 91k)$$

$$= (12.5 \parallel 114) = 3.03k\Omega$$

⑤ op Resistance



$$R_o = 66.48k\Omega$$



Find $Z_i, Z_o, \frac{V_o}{V_s}, \frac{I_o}{I_b}$

By -ve ffb the close loop gain des but now due to 10uF cap^c the effect of -ve ffb is removed bcz for ac cap^c act as short ckt so now 39k is i/p and 22k is o/p resistance so for ac 39, 22k are not the ffb

Solⁿ First dc analysis.

KVL

$$-9 + 1.8K(I_B + I_C) + 61K I_B + V_{BE} = 0$$

$$1.8K I_B + 80 \times 1.8K I_B + 61K I_B = 8.3$$

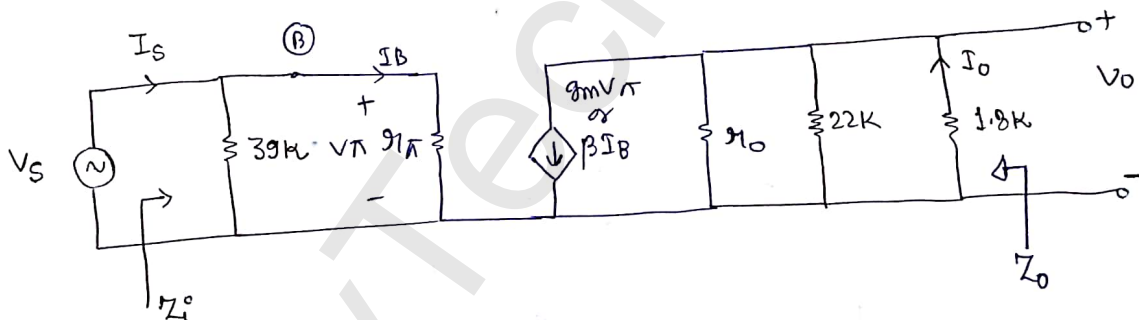
$$I_B = 40.13 \mu A$$

$$I_C = 3.21 \text{ mA}$$

$$g_m = \frac{I_C}{V_T} = \frac{3.21 \text{ mA}}{26 \text{ mV}} = 123.4 \text{ ms}$$

$$r_{\pi} = \frac{\beta}{g_m} = \frac{80}{123.4 \times 10^{-3}} = 0.648 \text{ k}\Omega \approx 0.65 \text{ k}\Omega$$

ac analysis



a) input resistance.

$$Z_i = (39k || r_{\pi})$$

$$Z_i = (39k || 0.65) = 0.64 \text{ k}\Omega$$

b) output resistance

$$Z_o = (r_o || 22k || 1.8k)$$

$$= (45 || 22 || 1.8)$$

$$Z_o = 1.6 \text{ k}\Omega$$

c)
$$V_o = -g_m V_{\pi} (r_o || 22k || 1.8)$$

$$\frac{V_o}{V_s} = \frac{V_o}{V_{\pi}} = -0.123 \times 1.6 \text{ k}$$

$$\frac{V_o}{V_s} = -196.8$$

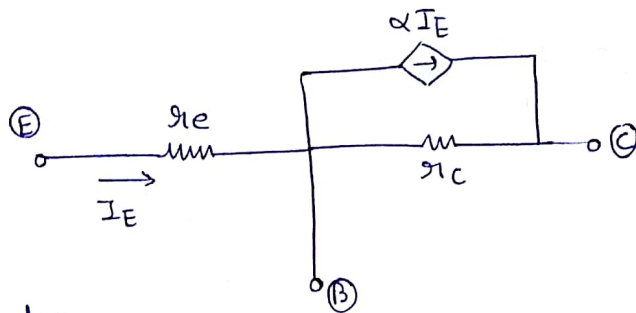
$$A_I = \frac{I_o}{I_s} = \left(\frac{-V_o}{1.8K} \right) \times \frac{640K}{V_s}$$

$$A_I = \left(\frac{V_o}{V_s} \times \frac{640}{1.8} \right)$$

$$= \frac{146.8 \times 64}{1.8} = 69.97$$

$$A_I \approx 70$$

T model of BJT (generally designed according to CB model)



T model parameter
 α, g_e, g_c

g_e is the ac resistance of emitter junction J_E or it is reciprocal of the slope of I_p characteristics of CB

(resistance) of diode $g_d = \frac{nV_T}{I_D}$

here $I_D = I_E$ $n=1$ for BJT

$$g_e = \frac{V_T}{I_E}$$

$I_E = Q$ point emitter current

$$g_e = \frac{V_T}{I_E} = \frac{V_T}{I_C} \cdot \frac{I_C}{I_E}$$

$$g_e = \frac{1}{g_m} \cdot \alpha$$

objective

$$\alpha = g_m g_e$$

$$\beta = g_m g_\pi$$

$$\frac{\alpha}{\beta} = \frac{g_e}{g_\pi}$$

$$g_e = \frac{\alpha}{g_m}$$

$$= \frac{\alpha}{\beta/g_\pi} = g_\pi \times \frac{\alpha}{\beta}$$

$$g_e = g_\pi \times \frac{\beta/\beta+1}{\beta}$$

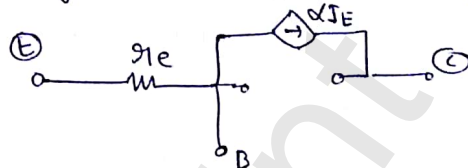
$$g_e = \frac{g_\pi}{1+\beta}$$

g_c :

g_c is a resistance of collector to base junction r_c or it is reciprocal of slope of o/p characteristics of CB configuration

$$g_c = (1 + \beta) g_{i0} \leftarrow \text{directly written}$$

g_c will go in $M\Omega$ range so in differential amp^r analysis α can remove g_c and α becomes



Q

$$\beta = 100$$

$$V_{BE} = 0.7V$$

Early voltage = 100V and it is operating at (10V, 2mA) calc

① π parameter

② T parameter

Solⁿ

$$g_m = \frac{I_c}{V_T} = \frac{2}{26} = 0.0769$$

$$g_e = 12.8\Omega$$

$$g_c = 5.5 M\Omega$$

$$g_{\pi} = \beta = g_{\pi} g_m$$

$$g_{\pi} = \frac{100}{0.0769} = 1300.4 \Omega$$

$$g_e = \frac{g_{\pi}}{(1 + \beta)} = \frac{1300.4}{(101)} = 12.875 \Omega$$

$$g_{i0} = \frac{(V_{CE})_0 + V_A}{(I_c)_Q} = \frac{10 + 100}{2} = 55 K$$

$$g_c = g_{i0} (1 + \beta) = 101 \times 55 = 5.5 M\Omega$$

π parameter

$$g_{\pi} = 1.3 K\Omega$$

$$g_{i0} = 55 K$$

$$g_m = 0.0769$$

$$\beta = 100$$

T parameter

$$g_e = 12.875 \Omega$$

$$g_c = 5.5 M\Omega$$

$$g_m = 0.0769$$

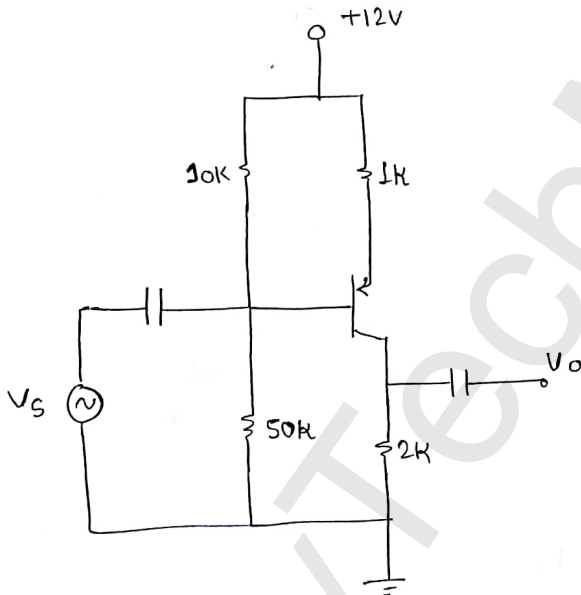
$$\alpha = g_m g_c = 0.99$$

Q In the ckt shown below $\beta = 100$ $V_A = \infty$

- ① The small sig voltage gain $A_v = \frac{V_o}{V_s}$ is
- (a) -1.6
 - (b) -3.18
 - (c) -4.73
 - (d) -10.43

Sol ② If the total instantaneous emitter to collector voltage is to remain in the range $1V \leq V_{EC} \leq 11V$ the max^m undistorted swing in the o/p voltage is

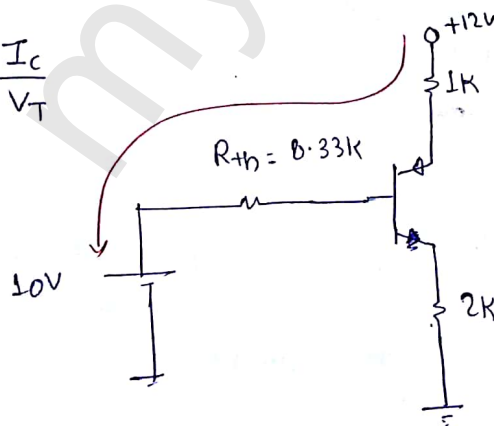
- a) 2.58 V (p-p)
- b) 5.16 V (p-p)
- c) 1.48 V (p-p)
- d) 2.96 V (p-p)



Solⁿ

$$I_m = \frac{I_c}{V_T}$$

Find I_c



$$-12 + I_E \times 1K + V_{EB} + 0.34K I_B + 10 = 0$$

$$101 I_B \times 1K + 0.34K I_B = 2 - 0.7$$

$$109.34 I_B = 1.3$$

$$I_B = \frac{1.3}{109.34} = 11.8 \mu A$$

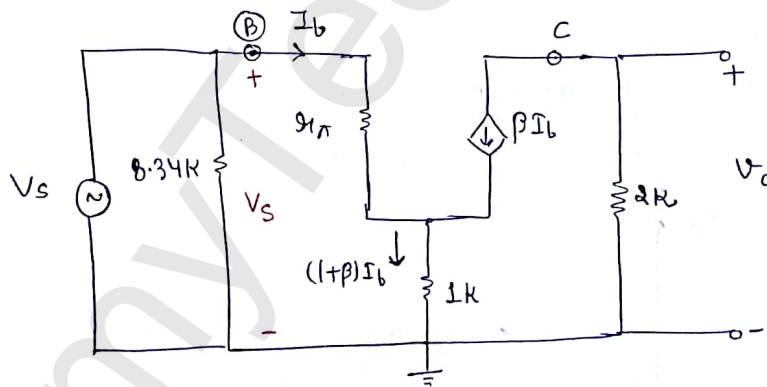
$$I_C = 1.18 \text{ mA}$$

$$I_E = 1.2 \text{ mA}$$

$$V_{EC} = 8.42 \text{ V}$$

$$g_m = \frac{I_C}{V_T} = \frac{1.18 \text{ mA}}{26 \text{ mV}} = 45 \text{ mS}$$

$$g_{\pi} = \frac{\beta}{g_m} = 2.18 \text{ k}\Omega$$



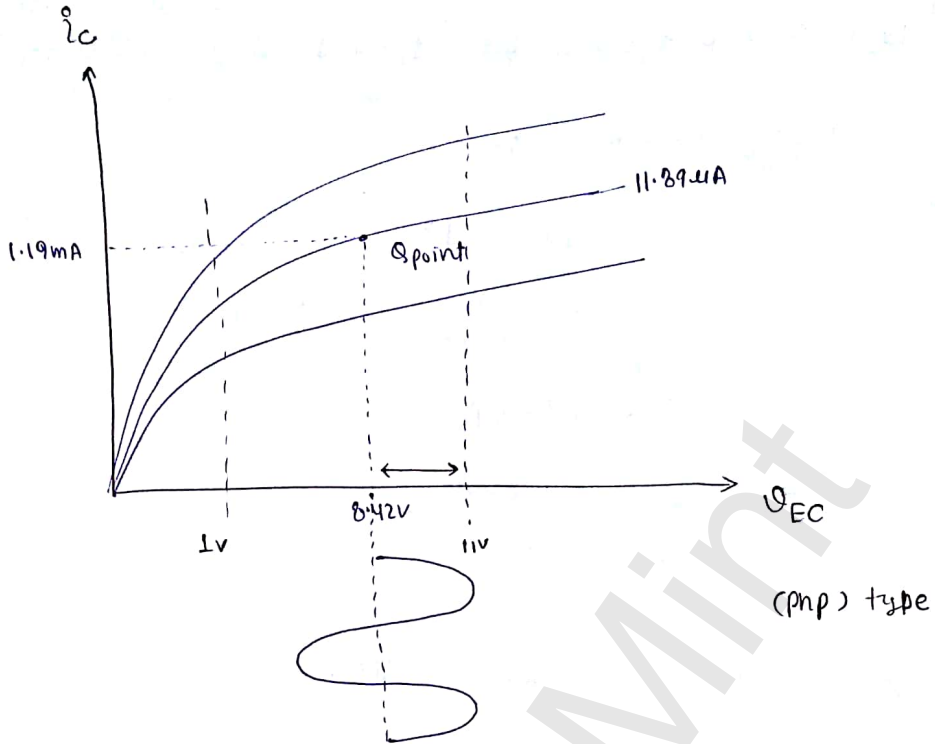
$$V_o = -\beta I_B \times 2K$$

$$V_s = g_{\pi} I_B + (1+\beta) I_B \times 1K$$

$$\therefore \frac{V_o}{V_s} = \frac{-\beta \times 2K}{g_{\pi} + (1+\beta) 1K}$$

option @ is correct.

②

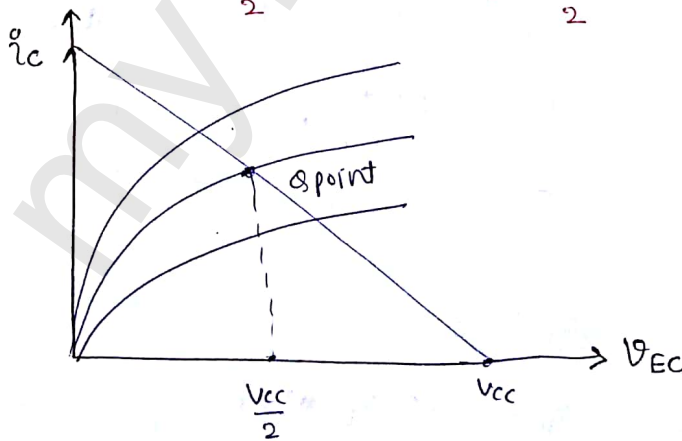


$$\text{O/P peak voltage} = 11 - 8.42 = 2.58V$$

$$\text{So peak to peak swing in O/P voltage} = 2 \times 2.58 = 5.16V$$

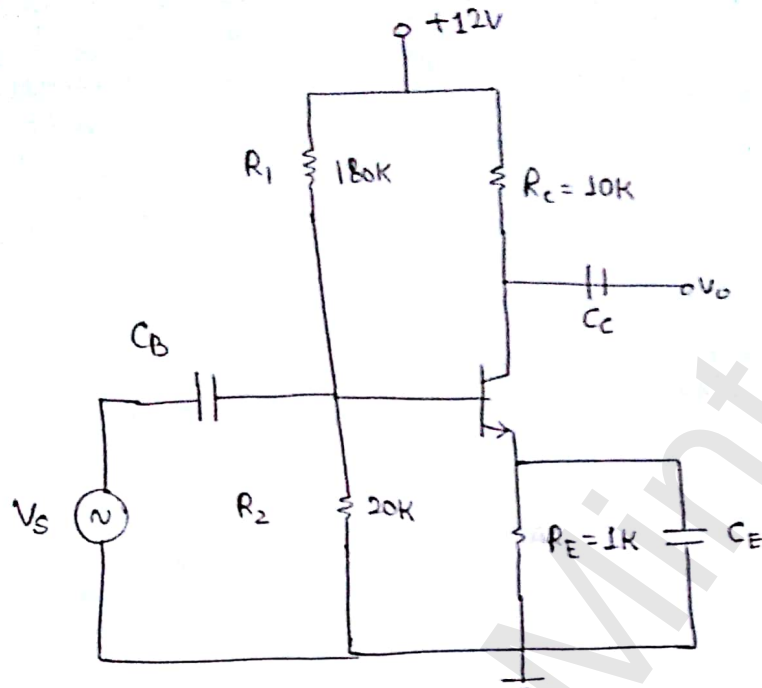
Sometime question - For maximum symmetrical swing the Q point should

be at $\frac{V_{CC}}{2}$ i.e. $V_{CEQ} = \frac{V_{CC}}{2}$



Low freq^c analysis of

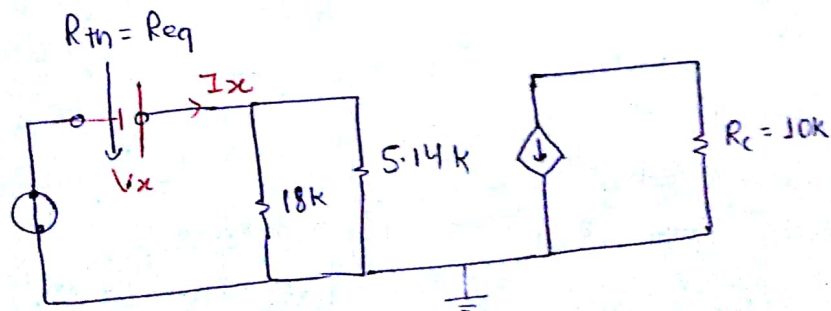
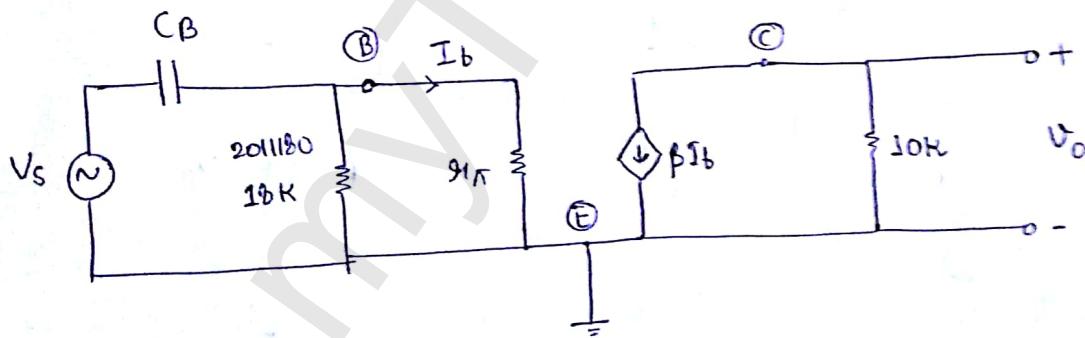
10



If the lower cut off freq^c due to C_B is 20Hz then calc the value of C_B
 $\beta = 80$ $r_o = \infty$

Soln

$$R_{\pi} = 5.14\text{k}\Omega$$



$$1811.514$$

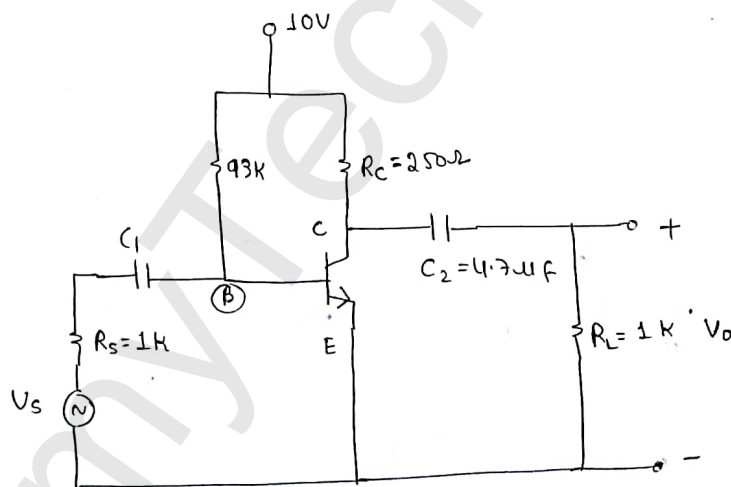
$$R_{eq} = 3.99 \text{ k}\Omega$$

$$f = \frac{1}{2\pi R_{eq} C}$$

$$f = \frac{1}{2\pi \times 3.99 \times 10^3 \times C}$$

$$20 = \frac{1}{2\pi \times 3.99 \times 10^3 \times C}$$

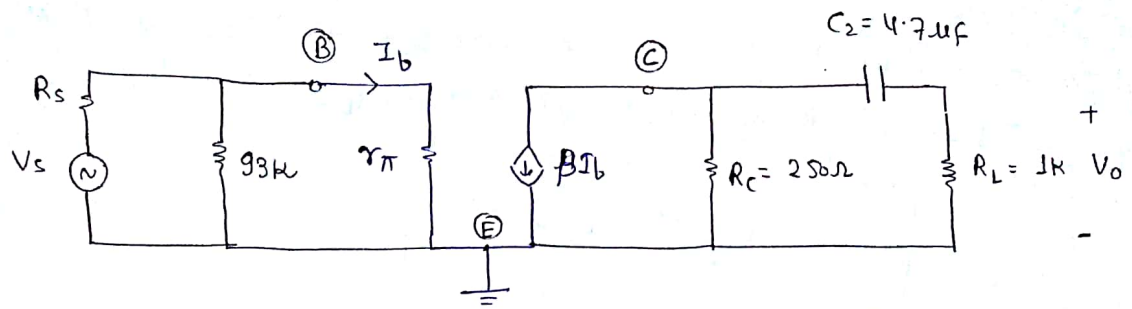
110



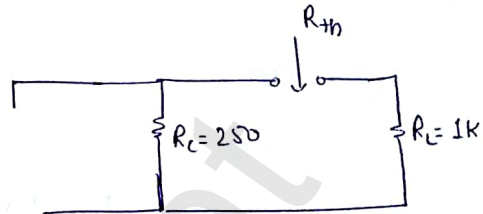
consider CE ckt shown below

$$\beta = 100, g_m = 0.3861 \frac{\text{Amp}}{\text{V}} \quad g_{o_b} \approx \infty \quad g_{i_n} = 259 \Omega$$

Calc lower cut off freq due to C_2 .



$$f_L = \frac{1}{2\pi R_{eq} C_2}$$



$$R_{eq} = R_{th} = R_C + R_L$$

$$= 250 + 1000 = 1250 = 1.25 \text{ k}$$

$$f_L = \frac{1}{2\pi 1250 \times 4.7}$$

$$= 27 \text{ Hz} \quad \text{Ans.}$$

Note* If the values of all the capacitors C_B , C_C and C_E are given then the lower cut off f_{m^c} can be calculated as

step ① Calculate the individual lower cut off f_{m^c} ies by considering one cap^c and s.c other two.

$$\text{Let } f_1 \longrightarrow C_B$$

$$f_2 \longrightarrow C_C$$

$$f_3 \longrightarrow C_E$$

step ② The overall lower cut off f_{m^c} will be the highest of 3 frequencies if it is higher by 4 times in comparison to other two frequencies

$$f_1 \longrightarrow 2 \text{ Hz}$$

$$f_2 \longrightarrow 9 \text{ Hz}$$

$$f_3 \longrightarrow 40 \text{ Hz}$$

If no f_{m^c} is found to be greater 4 times than the other two then the overall lower cutoff f_{m^c} can be calculated as f_L

$$f_L = 1.1 \sqrt{f_1^2 + f_2^2 + f_3^2}$$

$f_1 \rightarrow 2\text{Hz}$

$f_2 \rightarrow 9\text{Hz}$

$f_3 \rightarrow 15\text{Hz}$ } greater than 4 times of f_1 but not 4 times of f_2

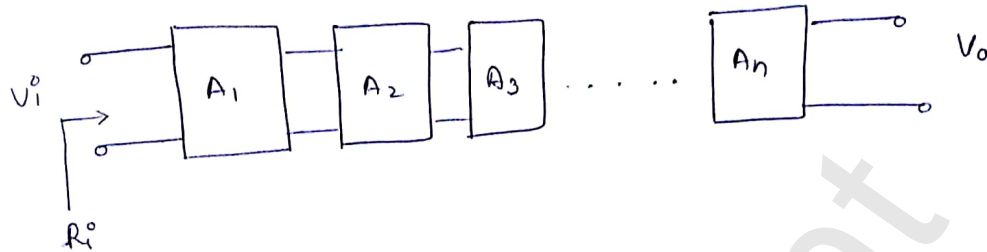
Comparison of CE, CC and CB amplifiers

S.No.	Parameter	CE amp ^r	CC amp ^r	CB amp ^r
1.	A_v	Large	≈ 1	Large
2.	A_i	Large	Large	≈ 1
3.	R_i	Medium	large	≈ 1
4.	R_o	medium	small	large
5.	Phase-shift in op & i/p voltage	180°	0°	0°
6.	Applications	As an audio amp ^r or LF amp ^r	Buffer ^r	HF amp ^r

Buffer amp^r (i.e. voltage amp^r)
i.e. CC amp^r

Buffer is used for impedance matching. Impedance matching is done for maximum power transfer.

Multistage Amplifiers

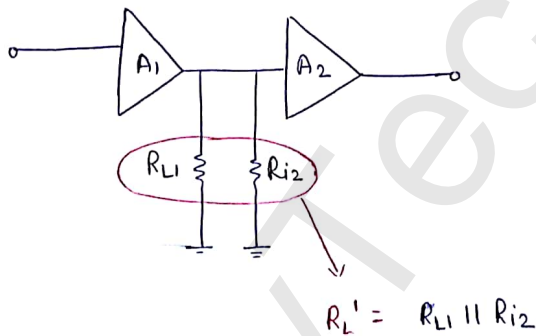


$$A_v = A_{v1} A_{v2} A_{v3} \dots A_{vn}$$

$$A_T = A_{T1} A_{T2} A_{T3} \dots A_{Tn}$$

$$A_p =$$

Two amp^r in cascade



Case 1: If R_{i2} is very large

$$R_L' = R_L \parallel R_{i2} \approx R_L$$

$$A_v = A_1 A_2$$

ये A_1 connected हो है R_{i2} बहुत बड़ा है जो कि प्रभाव नहीं डालता

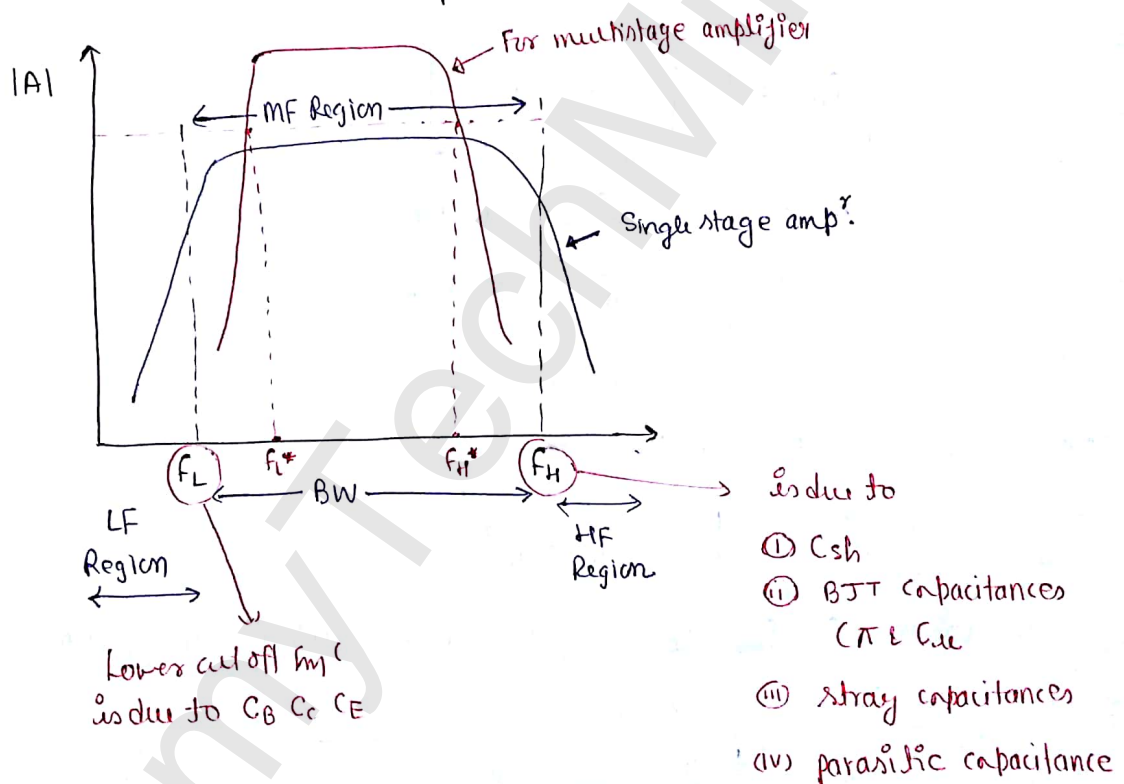
\Rightarrow Non-interactive cascading.

Case 2: If R_{i2} is small

$$R_L' = R_{L1} \parallel R_{i2} \quad (\downarrow) \quad \text{Loading effect}$$

Gain of 1st stage decreases. bcz the gain of 1st stage depends on the load of 1st stage which is fed by the R_{i2}
 \Rightarrow Interactive cascading

Gain vs f_m^c For RC coupled amp^r



Note * gain Bandwidth product of amp^r remain constant
 * In multistage amp^r gain is \uparrow ed, hence BW is reduced.

case 1: For non interactive cascading

Let us assume that f_L is the lower cut off f_m^c and f_H is the higher cut off f_m^c of individual stage.

so overall lower cut off f_m^c

$$f_L^* = \frac{f_L}{\sqrt{2^{1/n} - 1}}$$

stage
↑
 $n=2$

$$f_L^* = 1.55 f_L$$

$n=3$

$$f_L^* = 1.96 f_L$$

Remb^x

overall higher cutoff f_m^c

$$f_H^* = f_H \sqrt{2^{1/n} - 1}$$

$$n=2 \quad ; \quad f_H^* = 0.64 f_H$$

$$n=3 \quad ; \quad f_H^* = 0.51 f_H$$

Case 2: For interactive cascading

$$f_L^* = \sqrt[1.1]{f_{L1}^2 + f_{L2}^2 + f_{L3}^2 + \dots}$$

where $f_{L1}, f_{L2}, f_{L3}, \dots$ are lower cut off f_m^c of each stage

$$\frac{1}{f_H^*} = \sqrt[1.1]{\frac{1}{f_{H1}^2} + \frac{1}{f_{H2}^2} + \frac{1}{f_{H3}^2} + \dots}$$

where f_{H1}, f_{H2}, f_{H3} are higher cut off frequency of individual stage

Q 3 Identical cascaded stages have an overall upper 3dB f_{m^c} of 20kHz and lower 3dB f_{m^c} of 20Hz what are f_L and f_H of each stage assume non-interactive stages.

Solⁿ $m = 3$

$$f_L^* = 20\text{Hz}$$

$$f_H^* = 20\text{kHz}$$

$$f_L^* = \frac{f_L}{\sqrt{2^{1/n} - 1}}$$

$$f_L = f_L^* \sqrt{2^{1/n} - 1}$$

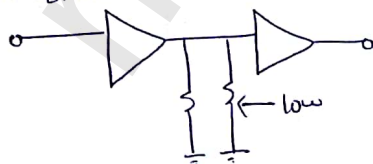
$$f_L = 20 \times \sqrt{2^{1/3} - 1}$$

$$f_H^* = f_H \sqrt{2^{1/n} - 1}$$

$$f_H = \frac{f_H^*}{\sqrt{2^{1/n} - 1}} = \frac{20\text{kHz}}{\sqrt{2^{1/3} - 1}}$$

Q The first and IInd stage of a 2 stage RC coupled amp^r have the lower cut off frequencies to be 100Hz and 200Hz respectively. Their upper cut off frequencies are 140kHz and 100kHz respectively find the overall 3dB BW required.

Solⁿ RC coupled amp^r का i/p resistance दोनो $\frac{N}{E}$ से interactive cascading. दोनो stages की lower cut off f_{m^c} अलग-अलग $\frac{N}{E}$ से interactive cascading की formula की use की।



$n = 2$

$$f_{L1} = 100\text{Hz}$$

$$f_{L2} = 200\text{Hz}$$

$$f_L^* = 1:1 \sqrt{(100)^2 + (200)^2}$$

$$= \sqrt{246\text{Hz}} = f_L^*$$

$$f_{H1} = 140$$

$$f_{H2} = 100$$

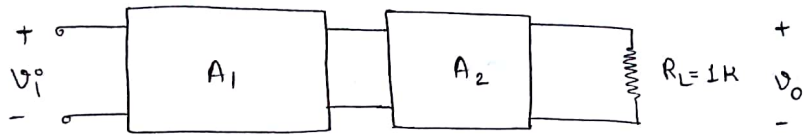
$$\frac{1}{f_H^*} = 1:1 \sqrt{\frac{1}{(140)^2} + \frac{1}{(100)^2}}$$

$$= \sqrt{73.975\text{kHz}} = f_H^*$$

$$BW^* = F_H^* - F_L^*$$

$$BW^* \approx F_H^*$$

110

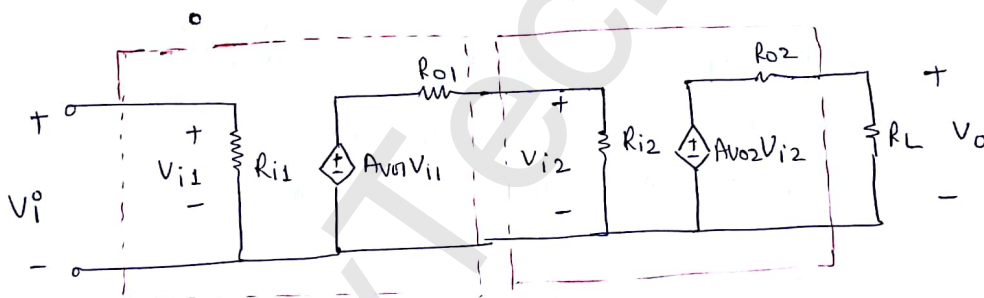


$$A_1 : A_{v0} = 10 \quad R_i = 10k\Omega \quad R_o = 1k\Omega$$

$$A_2 : A_{v0} = 5 \quad R_i = 5k\Omega \quad R_o = 200\Omega$$

A cascade connection of two voltage amp^r A_1 and A_2 is shown below the open loop voltage gain A_{v0} , i/p resistance R_i and o/p resistance are given. Calc^e the approximate overall voltage gain.

solⁿ.



$$V_o = \frac{R_L}{R_{o2} + R_L} A_{v02} V_{i2}$$

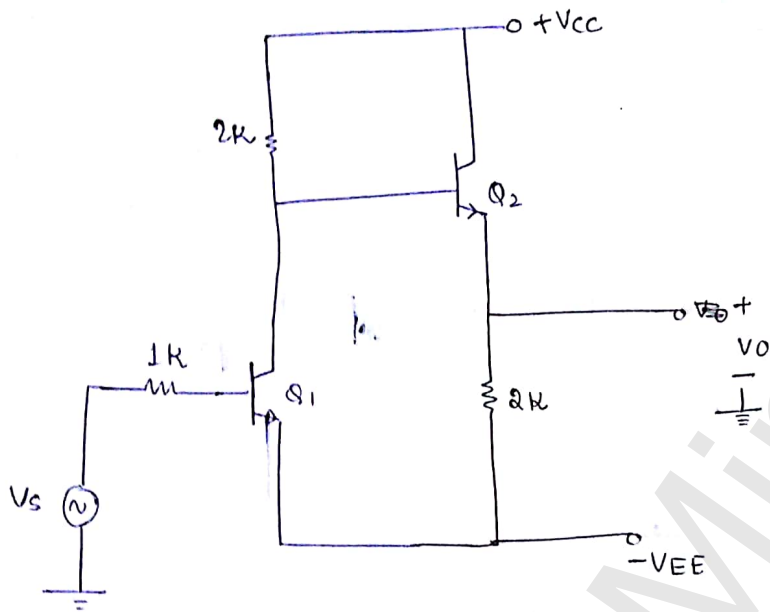
$$V_{i2} = \frac{R_{i2}}{R_{o1} + R_{i2}} A_{v01} V_{i1}$$

$$V_o = \frac{R_L}{R_{o2} + R_L} A_{v02} \times \frac{R_{i2}}{R_{o1} + R_{i2}} A_{v01} \cdot V_{i1}$$

$$\Rightarrow \frac{V_o}{V_{i1}} = \frac{V_o}{V_i} = A_v = \frac{R_L}{R_{o2} + R_L} \cdot A_{v02} \times \frac{R_{i2}}{R_{o1} + R_{i2}} \times A_{v01} = 34.72$$

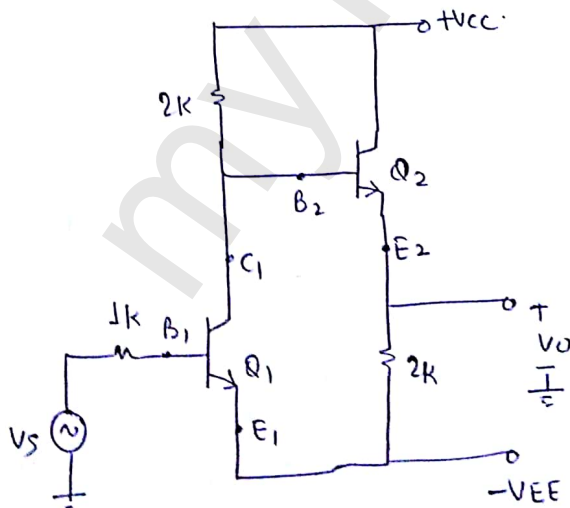
Q Draw the circuit of Darlington amp^r and explain its advantages.

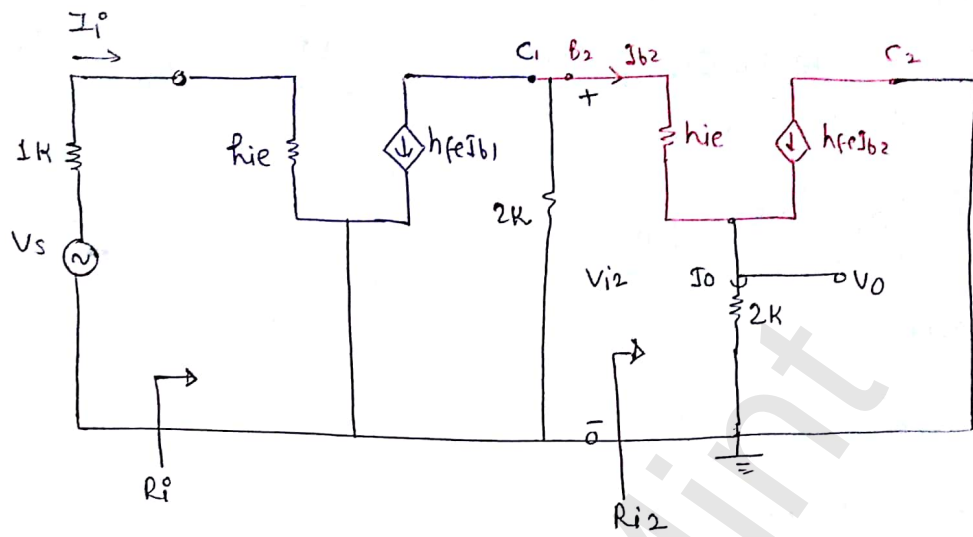
110



For the cascaded amp^r shown find the i/p impedance, current gain and voltage gain making any reasonable assumption if required that h parameters are $h_{ie} = 1.1k\Omega$, $h_{fe} = 50$

Solⁿ





$$I_0 = (1+h_{fe})I_{b2}$$

$$V_{i2} = h_{ie}I_{b2} + (1+h_{fe})I_{b2} \times 2k$$

$$\frac{V_{i2}}{I_{b2}} = R_{i2} = h_{ie} + (1+h_{fe})2k$$

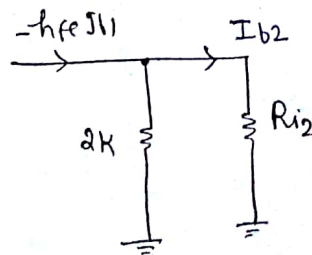
$$= 1.1k + 51 \times 2k$$

$$R_{i2} = 103.1k$$

$$I_{b2} = \frac{2k}{2k + R_{i2}} (-h_{fe}I_{b1})$$

$$= \frac{2k \times (-50)}{2k + 103.1k} I_{b1}$$

$$I_{b2} = -0.957I_{b1}$$



1. Current gain

$$A_I = \frac{I_o}{I_i} = \frac{(1+h_{fe}) I_{b2}}{I_{b1}} = \frac{(1+50) \cdot (-0.95) I_{b1}}{I_{b1}}$$

$$A_I = -48.45 \quad A_{m \equiv}$$

2. Input resistance.

$$R_i^o = \frac{V_i^o}{I_i^o}$$

$$V_i^o = I_i^o \times R_{ie}$$

$$R_i^o = R_{ie}$$

$$R_i^o = 1.1 \text{ k}\Omega$$

3. Voltage gain

$$A_V = \frac{V_o}{V_s} = \frac{I_o \times 2 \text{ k}}{V_s}$$

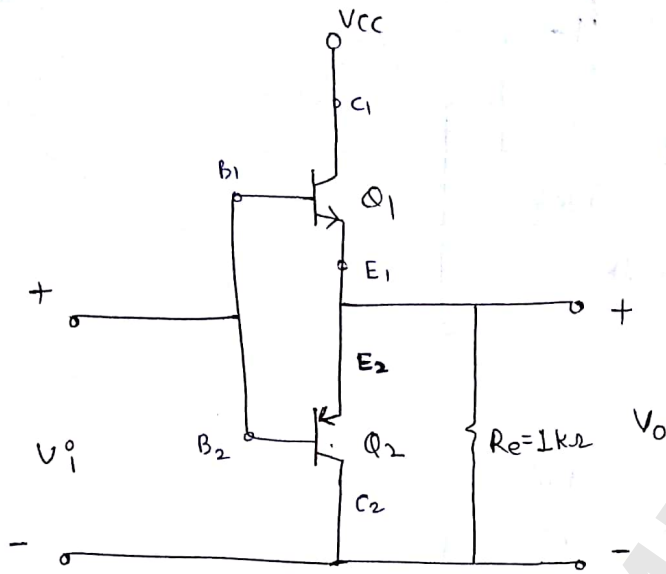
$$= \frac{(1+h_{fe}) I_{b2} \times 2 \text{ k}}{V_s}$$

$$= \frac{51 \times (-0.95 I_{b1}) \times 2 \text{ k}}{I_{b1} (1 \text{ k} + R_{ie})} = 46.2144$$

$$-V_s + 1 \text{ k} I_{b1} + R_{ie} I_{b1} = 0$$

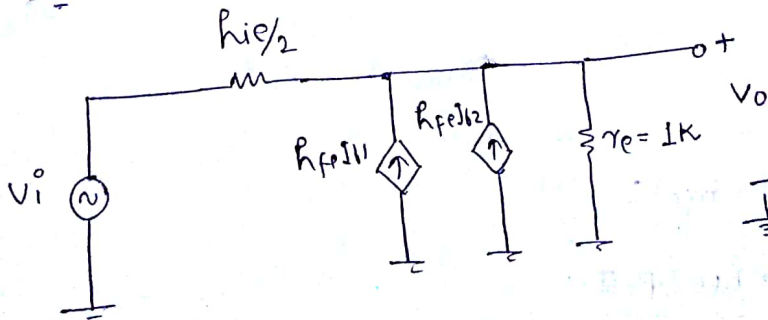
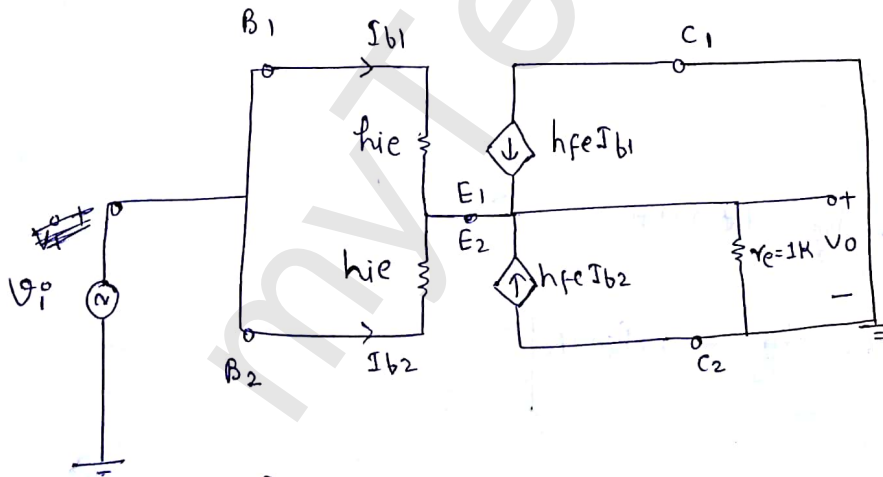
$$V_s = (1 \text{ k} + R_{ie}) I_{b1}$$

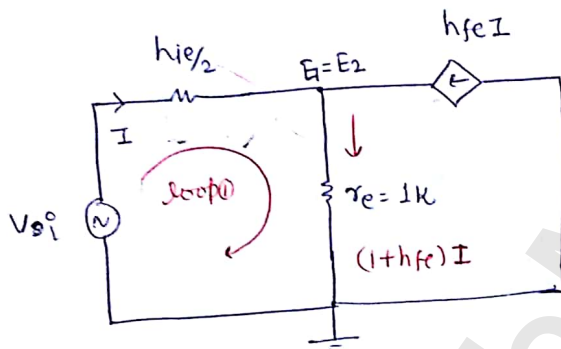
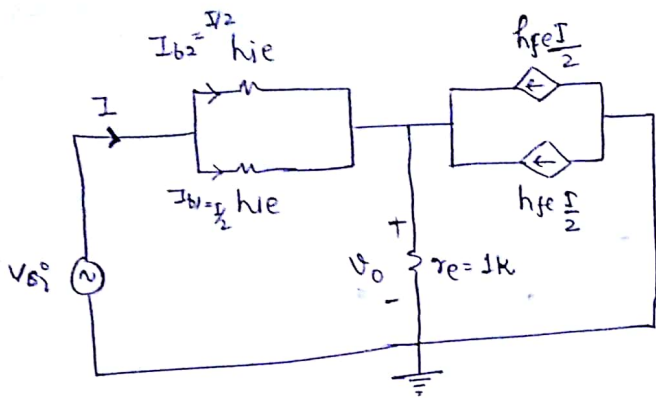
Q



Derive the expression for voltage gain A_v and i/p resistance R_i

Find the values of A_v and R_i if $h_{ie} = 1k\Omega$, $h_{fe} = 100$, $R_E = 1k\Omega$





① Input resistance

$$R_i = \frac{V_i^\circ}{I}$$

KVL in loop ①

$$-V_i^\circ + I \times \frac{h_{ie}}{2} + R_e (1+h_{fe})I = 0$$

$$\frac{V_i^\circ}{I} = R_i = \frac{h_{ie}}{2} + (1+h_{fe})R_e$$

② Voltage gain

$$A_v = \frac{V_o}{V_i^\circ}$$

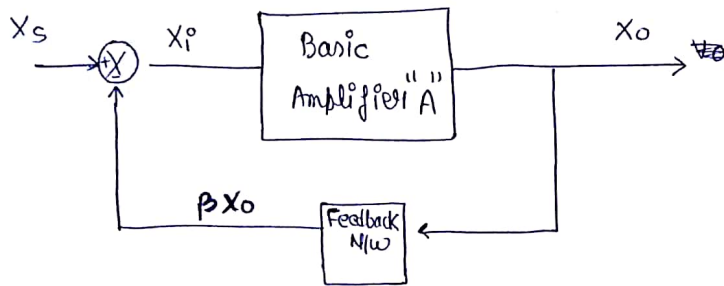
$$V_o = R_e \times (1+h_{fe})I$$

$$\therefore \frac{V_o}{V_i^\circ} = \frac{(1+h_{fe})R_e I}{\left[\frac{h_{ie}}{2} + (1+h_{fe})R_e \right] I}$$

$$A_v = \frac{(1+h_{fe})R_e}{\frac{h_{ie}}{2} + (1+h_{fe})R_e}$$

myTechMint

Feedback amplifier



generally in case of -ve Fb, f/b N/w is resistive
" " " " +ve f/b f/d N/w is Combination of RLC

$$X_o = AX_i \quad \text{--- ①}$$

$$X_i = X_s - \beta X_o \quad \text{--- ②}$$

$$\Rightarrow X_i = X_s - \beta(AX_i)$$

$$\Rightarrow X_s = X_i + \beta AX_i$$

$$\Rightarrow X_s = (1 + \beta A)X_i$$

$$\text{open loop gain} = A = \frac{X_o}{X_i}$$

$$\begin{aligned} \text{closed loop gain} \\ \text{or} \\ \text{Gain with feedback} \end{aligned} = A_f \text{ or } A_{CL} = \frac{X_o}{X_s}$$

$$\Rightarrow A_f = \frac{X_o}{X_s} = \frac{AX_i}{(1 + \beta A)X_i}$$

$$A_f = \frac{A}{1+A\beta}$$

Stability of gain

if $\frac{\Delta A_f}{A_f} > \frac{\Delta A}{A}$ means close loop is more stable.

$\frac{\Delta A}{A} > \frac{\Delta A_f}{A_f}$ means open loop is more stable.

$$A_f = \frac{A}{1+A\beta}$$

Diff wrt 'A'

$$\frac{dA_f}{dA} = \frac{(1+A\beta) \cdot 1 - (0+\beta)A}{(1+A\beta)^2}$$

$$\frac{dA_f}{dA} = \frac{1}{(1+A\beta)^2}$$

$$dA_f = \frac{1}{(1+A\beta)^2} \cdot dA$$

$$dA_f = \frac{A}{1+A\beta} \cdot \frac{1}{A} \cdot dA \cdot \frac{1}{(1+A\beta)}$$

$$dA_f = A_f \cdot \frac{dA}{A} \cdot \frac{1}{(1+A\beta)}$$

$$\frac{dA_f}{A_f} = \frac{1}{(1+A\beta)} \frac{dA}{A}$$

*** (amb² theory)

$$\Rightarrow \frac{dA_f}{A_f} < \frac{dA}{A} \quad [\because 1+A\beta > 1]$$

For Objective type question

$$A_f = \frac{A}{1+A\beta}$$

but $A\beta \gg 1$

$$A_f \approx \frac{A}{A\beta}$$

$$\Rightarrow \boxed{A_f \approx \frac{1}{\beta}}$$

$\beta \rightarrow$ feedback factor or retransmission factor

Q An amp^r with open loop voltage gain $A = 1000 \pm 100$ is required to have an amp^r whose gain varies no more than $\pm 0.2\%$ find

- (1) Reverse transmission factor of the f/d N/w.
- (2) gain with f/b

Solⁿ $\frac{dA_f}{A_f} = 0.002$

$$\frac{dA_f}{A_f} = \frac{1}{(1+A\beta)} \frac{dA}{A}$$

$$0.002 = \frac{1}{(1+1000\beta)} \cdot \frac{100}{1000}$$

$$(1+1000\beta) = \frac{1}{10 \times 0.002} = \frac{1000}{20} = 50$$

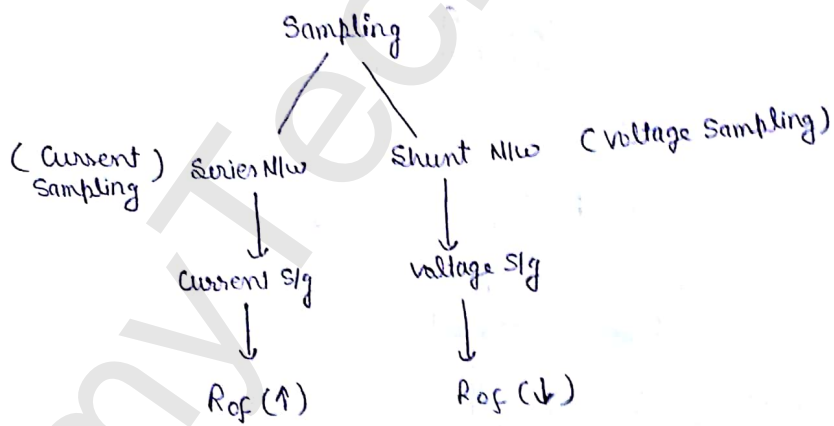
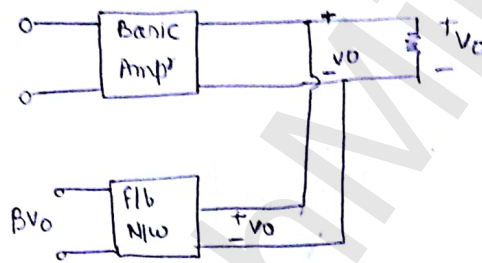
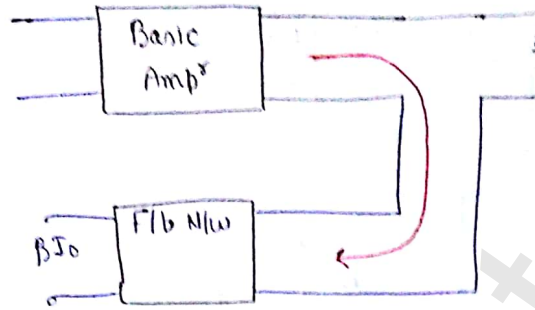
$$1000\beta = 49$$

$$\beta = \frac{49}{1000} = 0.049$$

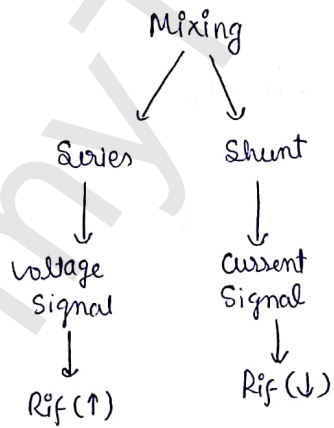
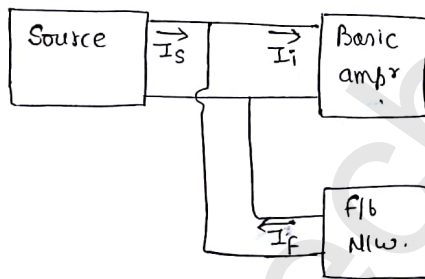
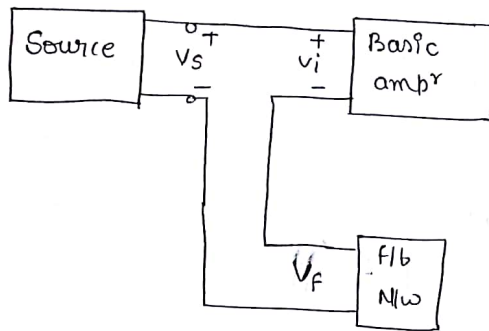
$$\boxed{\beta = 0.049}$$

$$A_f = \frac{A}{1+A\beta} = \frac{1000}{1000 \times 0.049 + 1} = 20 \text{ Am}$$

Sampling



Mixing :-



Voltage Shunt
 ↓ ↓
 Sampling Mixing

Voltage Series
 ↓ ↓
 Sampling Mixing

Series Shunt
 ↓ ↓
 Mixing Sampling

Shunt Shunt
 ↓ ↓
 Mixing Sampling

S.No.	Type of f/b amp ^r	R _{if}	R _{of}
1.	Voltage Series or Series Shunt	$R_i (1+A\beta)$	$\frac{R_o}{(1+A\beta)}$
2.	Voltage Shunt or Shunt Shunt	$\frac{R_i}{(1+A\beta)}$	$\frac{R_o}{(1+A\beta)}$
3.	Current Series or Series Series	$R_i (1+A\beta)$	$R_o (1+A\beta)$
4.	Current Shunt or Shunt Series	$\frac{R_i}{(1+A\beta)}$	$R_o (1+A\beta)$

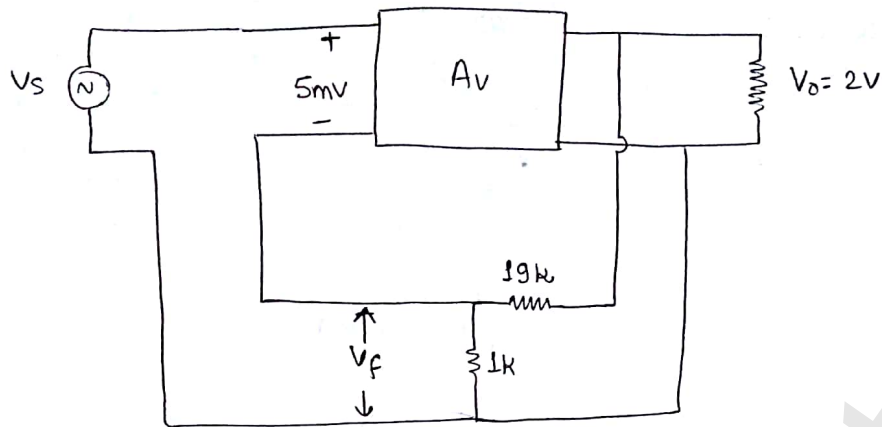
$R_i \rightarrow$ open loop i/p resistance

$R_o \rightarrow$ open loop o/p resistance

$D = 1 + A\beta$

$A \rightarrow$ open loop gain.

$\beta \rightarrow$ feedback factor.



For the voltage series fb amp^r shown below calc^e V_f fb ratio β
 A_v (voltage gain without fb), and A_{vf} (with fb)

Solⁿ

$$V_f = \frac{V_o \times 1k}{20k} =$$

$$V_f = \frac{V_o}{20}$$

$$V_f = \beta V_o$$

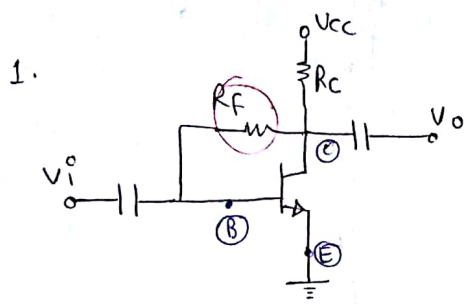
$$\beta = \frac{1}{20}$$

$$A_v = \frac{V_o}{5mV} = \frac{2000}{5} = 400$$

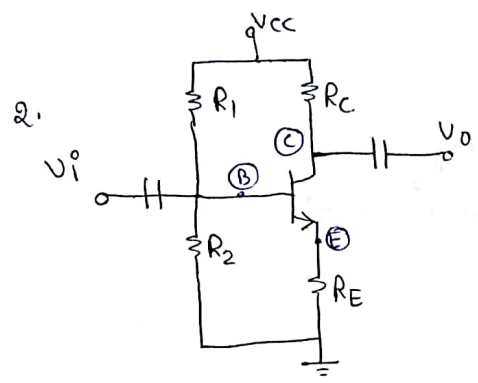
$$A_v = 400$$

$$A_{vf} = \frac{A_v}{1 + A_v \beta} = \frac{400}{1 + \frac{400}{20}} = \frac{400}{1 + 20} = \frac{400}{21} = 19.04$$

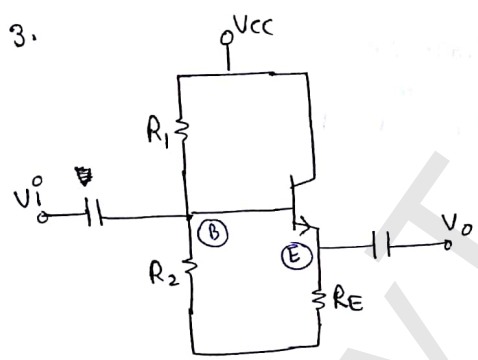
Q Identify the type of f/b in the ckt shown below



voltage shunt
or
shunt shunt

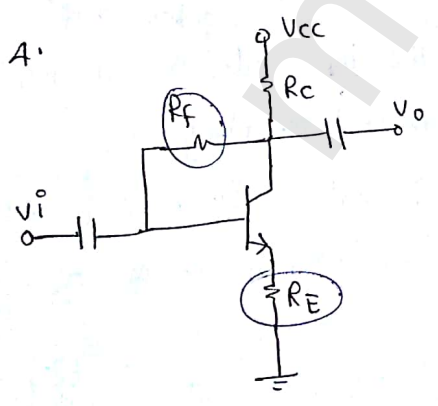


current series
or
series series



voltage series series
or
series shunt

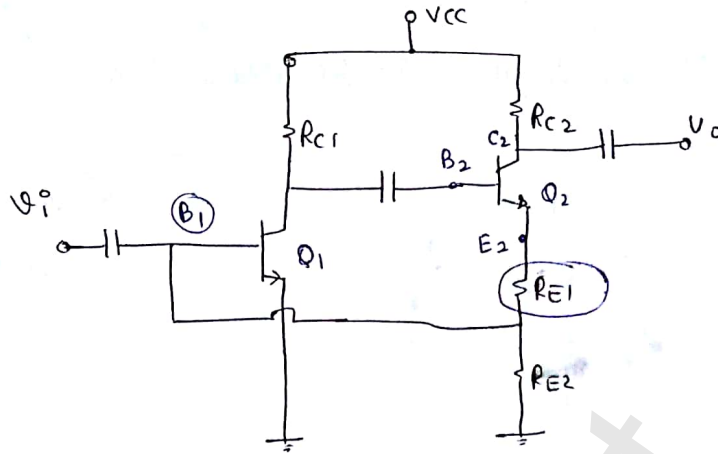
Q. { 9n Buffer amp^r which type of f/b { voltage ser- }



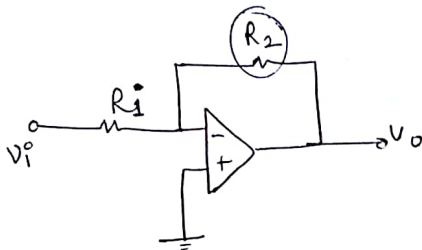
A ckt can have multiple f/b
 Rf creates voltage shunt f/b while
 RE creates current series f/b.
 Sh. If cap^r is connected across RE then voltage shunt f/b bcz effect of RE is removed.

⑤

Current shunt
or
shunt Series

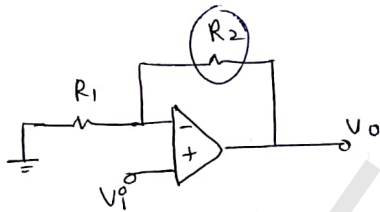


⑥



Voltage Shunt
or
Shunt Shunt

⑦



Voltage Series
or
Series Shunt.

Procedure to identify the type of f/b

- step ① Identify the element responsible for feedback of basic amp^r.
- step ② If f/b element is directly connected to the o/p node then it indicates voltage sampling otherwise it indicates current sampling
- step ③ If f/b element is directly connected to the i/p node of basic amp^r then it indicates shunt mixing otherwise it indicates series mixing.

16 July 2017

Oscillators : CKTs in which no ac i/p given but we get ac o/p.
but we give dc i/p in osc.

diff^{ce} b/w multivibrator and Oscillator

↓ we can get ↓ gives single freq^c o/p

Square wave

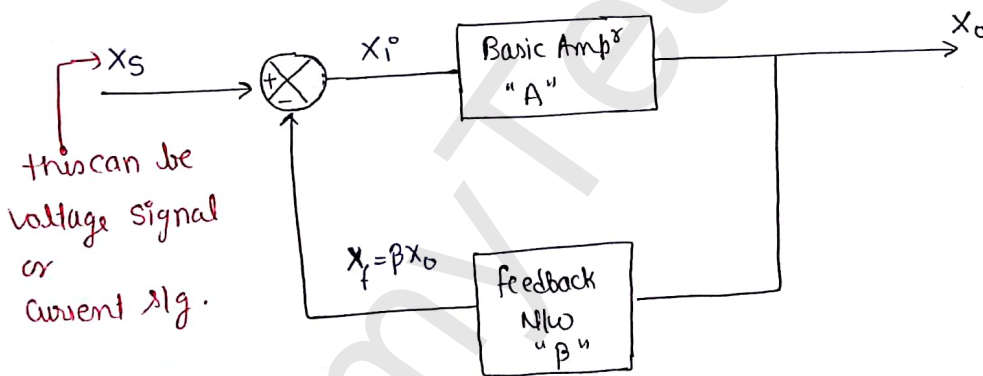
triangular wave

multi + vibrator

↓ ↓
many freq^c

multiple frequencies

Q Show that a f/b amp^r can be made to work as an oscillator



$$X_o = A X_i$$

$$X_f = \beta X_o = A\beta X_i$$

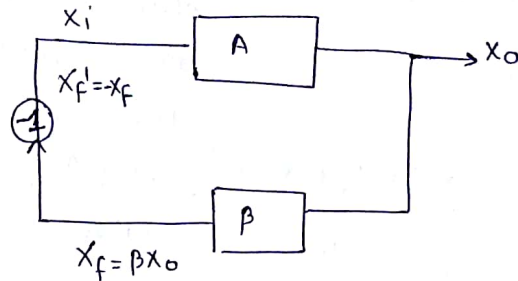
$$X_i = X_s - X_f$$

$$X_i = X_s - A\beta X_i$$

$$X_s = X_i (1 + A\beta)$$

$$A_f = \frac{X_o}{X_s} = \frac{A X_i}{X_i (1 + A\beta)} =$$

$$\Rightarrow A_f = \frac{A}{1+AB} \longrightarrow \textcircled{1}$$



Why loop gain is like this

$$\left\{ \begin{array}{l} \text{Loop gain} = \frac{x_f'}{x_i} = \frac{-x_f}{x_i} = \frac{-ABx_i}{x_i} = -AB \end{array} \right.$$

but $x_f' = x_i$

so loop gain $[-AB] = 1$

so from eqⁿ ①

$$A_f = \frac{A}{1+(-1)}$$

$$A_f = \frac{A}{0} \rightarrow \infty$$

gain is ∞ means.

There is just an o/p sig even in the absence of an externally applied

i/p sig. the condⁿ $[-BA] = 1$

$$\Rightarrow |[-BA]| = 1$$

$$\Rightarrow \angle[-BA] = 0^\circ \text{ or } 2n\pi$$

\Rightarrow condⁿ for oscillation

Why only these condⁿ for oscillation?

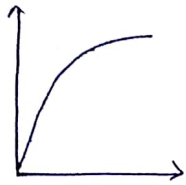
This is called **Barkhausen Criterion**

for oscillator ideally loop gain should 1 and phase shift should be 0° .
It is not that only the f/b gives oscillation.

Non linear devices की वजह से amplitude बढ़ती है



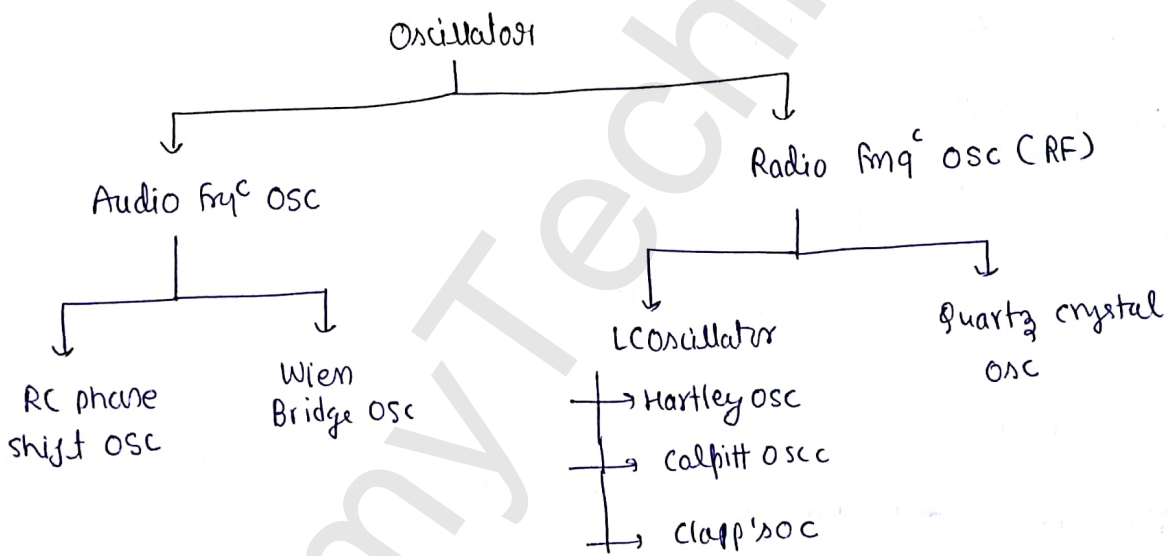
this is the O/P of oscillator which comes in nature due to non linearity of device.



$$i_c = \frac{K_1 + K_2 i_b + K_3 i_b^3}{K_4 i_b^4}$$

but after a fix value it will stop rising. i.e called ONSET OF NON-LINEARITY

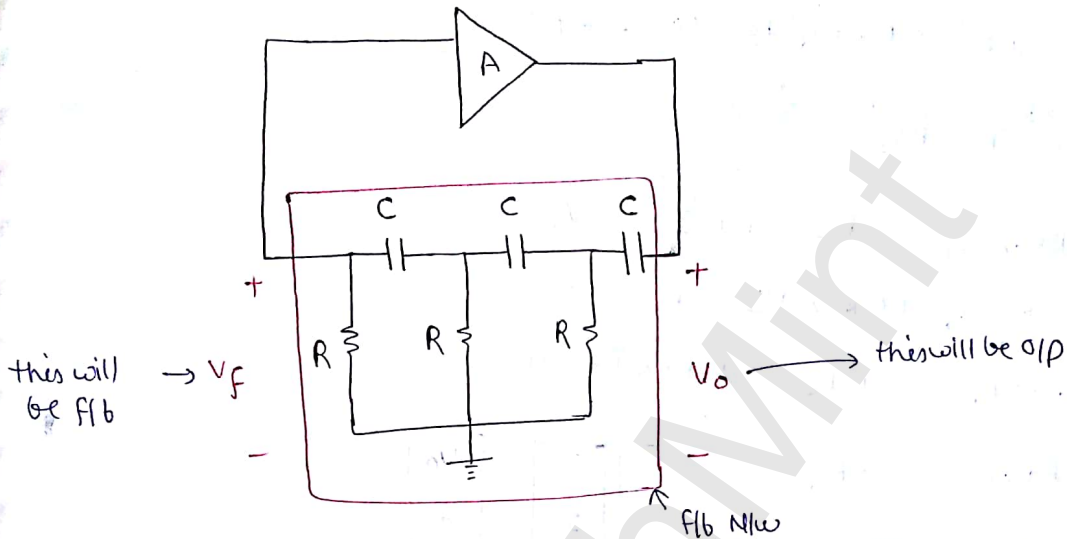
due to ONSET of Non-linearity. the O/P of oscillator can't increase beyond a fix value



Colpitt is used at which fm^c Range.

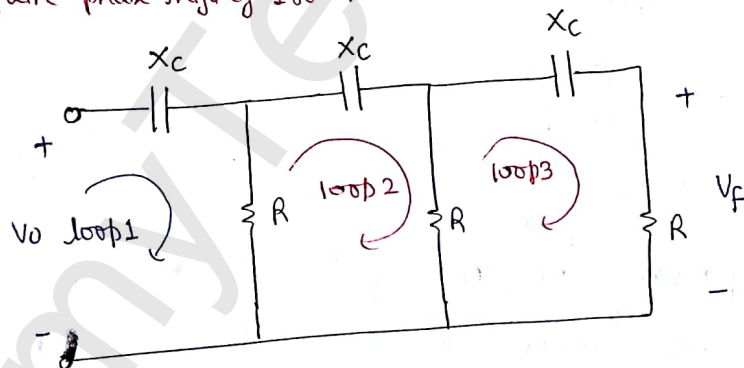
Solⁿ - Radio fm^c Range

Q Derive the condⁿ of oscillation and the expression for f_{oq} of oscillation for the ckt shown below.



one alone cap^c can provide 90° but with R i.e RC provide phase shift less than 90° \therefore 3 RC ckt/s are required.

Q why we require phase shift of 180° ?



KVL: loop 1

$$-V_o + X_c I_1 + R(I_1 - I_2) = 0$$

$$(R + X_c)I_1 - RI_2 = V_o \longrightarrow \textcircled{1}$$

KVL in loop 2

$$X_c I_2 + R(I_2 - I_3) + R(I_2 - I_1) = 0$$

$$X_c I_2 + R(2I_2 - I_3 - I_1) = 0$$

$$-RI_1 + (2R+X_c)I_2 - RI_3 = 0 \quad \text{--- (2)}$$

KVL in loop (3)

$$X_c I_3 + RI_3 + R(I_3 - I_2) = 0$$

$$-RI_2 + (2R+X_c)I_3 = 0 \quad \text{--- (3)}$$

we know $V_f = RI_3$

$$(R+X_c)I_1 - RI_2 + 0 \cdot I_3 = V_0$$

$$-R I_1 + (2R+X_c)I_2 - RI_3 = 0$$

$$+ 0 I_1 - RI_2 + (2R+X_c)I_3 = 0$$

$$\begin{bmatrix} (R+X_c) & -R & 0 \\ -R & 2R+X_c & -R \\ 0 & -R & (2R+X_c) \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} V_0 \\ 0 \\ 0 \end{bmatrix}$$

using crammers rule

$$I_3 = \frac{\Delta_3}{\Delta}$$

where

$$\Delta = \begin{vmatrix} R+X_c & -R & 0 \\ -R & 2R+X_c & -R \\ 0 & -R & 2R+X_c \end{vmatrix}$$

$$= (R+X_c) [(2R+X_c)^2 - R^2] + R [-2R^2 - RX_c]$$

$$\Delta = (R+X_c) [4R^2 + X_c^2 + 4RX_c - R^2] - 2R^3 - RX_c^2$$

$$= (R+x_c)(3R^2+x_c^2+4Rx_c) - 2R^3 - R^2x_c$$

$$= 3R^3 + Rx_c^2 + 4R^2x_c + 3R^2x_c + x_c^3 + 4Rx_c^2 - 2R^3 - R^2x_c$$

$$\Delta = R^3 + x_c^3 + 6R^2x_c + 5Rx_c^2$$

How we $\rightarrow \Delta^3 =$
find this?

$$\begin{vmatrix} R+x_c & -R & V_0 \\ -R & 2R+x_c & 0 \\ 0 & -R & 0 \end{vmatrix} = V_0 R^2$$

$$V_f = I_3 \cdot R$$

$$V_f = \frac{\Delta_3}{\Delta} \cdot R$$

$$V_f = \frac{V_0 R^2}{R^3 + x_c^3 + 6R^2x_c + 5Rx_c^2} \cdot R$$

$$\Rightarrow \frac{V_f}{V_0} = \beta = \frac{R^3}{R^3 + x_c^3 + 6R^2x_c + 5Rx_c^2}$$

$$\Rightarrow \beta = \frac{1}{1 + \left(\frac{x_c}{R}\right)^3 + 6\left(\frac{x_c}{R}\right) + 5\left(\frac{x_c}{R}\right)^2}$$

put $x_c = \frac{1}{j\omega C}$

$$\beta = \frac{1}{1 + \frac{1}{(j\omega RC)^3} + \frac{6}{j\omega RC} + \frac{5 \cdot 1}{(j\omega RC)^2}}$$

Let us assume $\alpha = \frac{1}{\omega RC}$

So

$$\beta = \frac{1}{1 + j\alpha^3 - j6\alpha + 5\alpha^2}$$

$$\beta = \frac{1}{(1-5\alpha^2) + j(\alpha^3 - 6\alpha)}$$

$$\text{Loop gain} = A\beta$$

$$= \frac{A}{(1-5\alpha^2) + j(\alpha^3 - 6\alpha)}$$

To satisfy Barkhausen criterion

$$\angle A\beta = 0^\circ \text{ or } 2n\pi$$

$$\text{So } \text{Imj}[A\beta] = 0^\circ \text{ at } \omega = \omega_0$$

$$\alpha^3 - 6\alpha = 0$$

$$\alpha(\alpha^2 - 6) = 0$$

$$\alpha \text{ can't be } 0 \text{ so } \alpha^2 - 6 = 0$$

$$\alpha^2 = 6$$

$$\alpha = \sqrt{6}$$

$$\text{At } \omega = \omega_0$$

$$\alpha = \frac{1}{\omega_0 RC} = \sqrt{6}$$

$$\omega_0 = \frac{1}{\sqrt{6} RC} \text{ rad/sec}$$

$$f = \frac{1}{2\pi RC \sqrt{6}} \text{ Hz}$$

↳ frequency of oscillation

क्या मैं RC की ऐसी value choose कर सकूँ हूँ जो phase shift 70° के लिए 3RC circuit का phase shift 210° हो जायगा. पर उस RC के corresponding को तो हमें एक function मिलेगी

या मुझे R and C की ऐसी ही value choose करनी है जिससे phase shift 60° मिले

क्या R and C के different different combination के लिए phase shift 60° हो सकता है?

condition of oscillation

$$|A\beta| = 1 \quad \text{at } \omega = \omega_0$$

For sustained oscillation

$$\left| \frac{A}{(1-5\alpha^2) + j0} \right| \geq 1$$

$$\Rightarrow \left| \frac{A}{1-5\alpha^2} \right| \geq 1$$

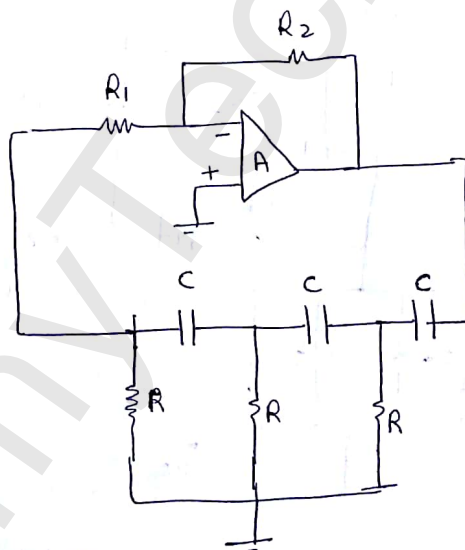
$$|A| \geq 29$$

$$\boxed{|A| \geq 29}$$

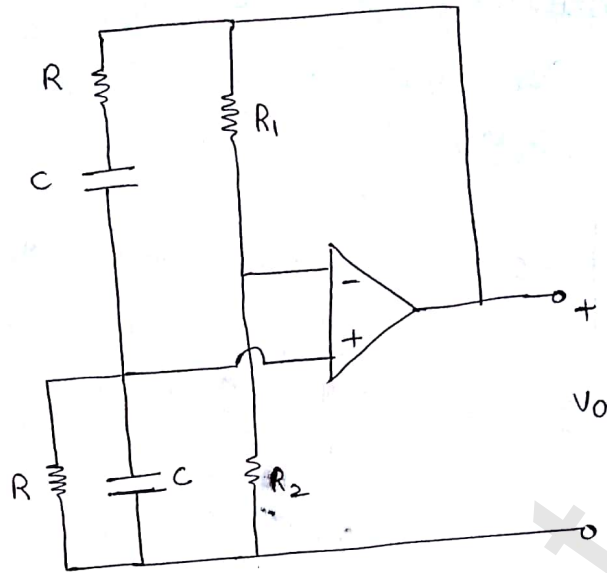
For practical oscillation the gain $|A\beta|$ should be slightly $>$ than 1 so that if due to some imperfection if gain dec. then it must not fall below 1.

Oscillations are occurring that means imaginary part is 0. or imag. part is 0 - that's why oscillations are there.

actual ckt of RC phase shift oscillator

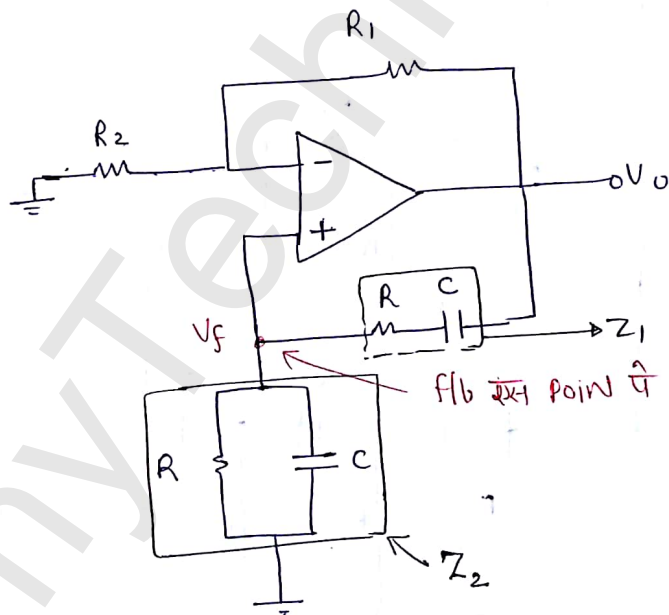


Q



obtain the condⁿ under which the ckt below produce oscillation what is the f_m^c of oscillation.

Solⁿ # Wein Oscillator



$$V_f = \frac{Z_2}{Z_1 + Z_2} \cdot V_0$$

$$= \frac{V_f}{V_0} = \beta = \frac{Z_2}{Z_1 + Z_2}$$

We have two flb

- ① R_1
- ② RC

2nd flb will be dominating and providing phase shift
 -ve flb in opamp work as amp^r but we want to operate it as an oscillator.

Now

$$Z_1 = R_1 + \frac{1}{j\omega C} = \frac{1 + j\omega RC}{j\omega C}$$

$$Z_2 = \frac{R \times \frac{1}{j\omega C}}{R + \frac{1}{j\omega C}} = \frac{R/j\omega C}{\frac{1 + j\omega RC}{j\omega C}}$$

$$Z_2 = \frac{R}{1 + j\omega RC}$$

$$\beta = \frac{\frac{R}{1 + j\omega RC}}{\frac{1 + j\omega RC}{j\omega R} + \frac{R}{1 + j\omega RC}}$$

$$A\beta = \frac{A}{3 + j(\omega RC - \frac{1}{\omega RC})}$$

at $\omega = \omega_0$, phase shift of loop gain should be zero

$$\therefore \omega_0 RC - \frac{1}{\omega_0 RC} = 0$$

$$\Rightarrow \begin{cases} \omega_0 = \frac{1}{RC} \text{ rad/sec} \\ f_0 = \frac{1}{2\pi RC} \text{ Hz} \end{cases}$$

For sustained oscillation

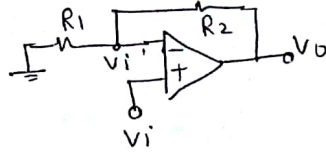
$$|A\beta| \geq 1$$

$$\frac{|A|}{3} \geq 1$$

$$\boxed{|A| \geq 3}$$

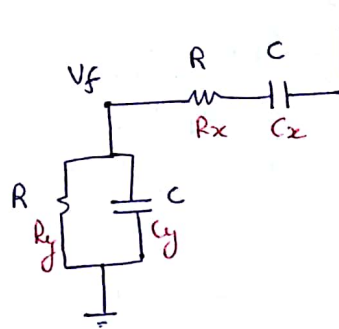
open loop gain of op amp. Without flb

$$A = 1 + \frac{R_1}{R_2}$$



$$\therefore 1 + \frac{R_1}{R_2} \geq 3$$

$$\Rightarrow R_1 \geq 2R_2$$



Note*

$$f_0 = \frac{1}{2\pi \sqrt{R_x R_y C_x C_y}}$$

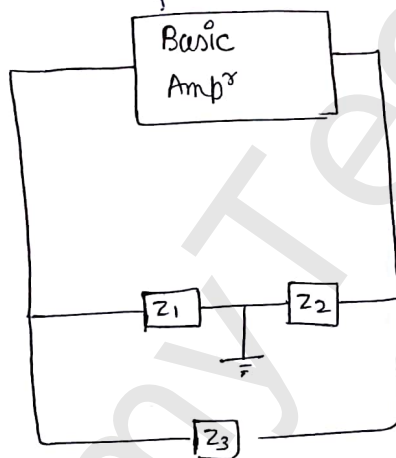
$$|A| \geq 1 + \frac{R_x}{R_y} + \frac{C_y}{C_x}$$

$$1 + \frac{R_x}{R_y} + \frac{C_y}{C_x} \Rightarrow \text{should not be less than } 3.$$

so $R_x > R_y$ and $C_y > C_x$

LC oscillators

it can be BJT, FET, opamp.



S.No.	Type of LC Osc	Z ₁	Z ₂	Z ₃
1.	Hartley	—m	—m	— —
2.	Colpitts <i>c caps are dominating.</i>	— —	— —	—m
3.	clapp's	— —	— —	—m— —

clap is modification of colpitt.

To calculate resonant f_{m}^c

$$\boxed{X_1 + X_2 + X_3 = 0} \quad \text{at } \omega = \omega_0$$

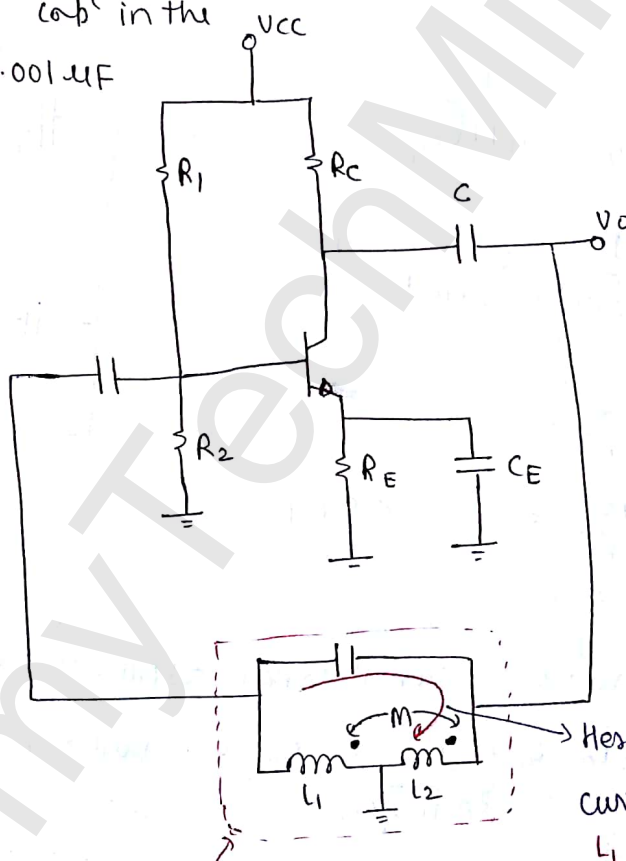
where 'x's are reactances without 'j' term.

$$X_C = \frac{1}{j\omega C}$$

$$X_C = \frac{-j}{\omega C} \quad \text{--- j removed.}$$

$$X_C = \frac{-1}{\omega C}$$

- Q Consider the Hartley oscillator ckt shown below given $L_1 = 100 \mu\text{H}$, $L_2 = 100 \mu\text{H}$ the mutual inductance b/w L_1 and L_2 is $20 \mu\text{H}$ what is the f_{m}^c of oscillation for given ckt if cap^c in the flb N/w is of $0.001 \mu\text{F}$



this is flb N/w.

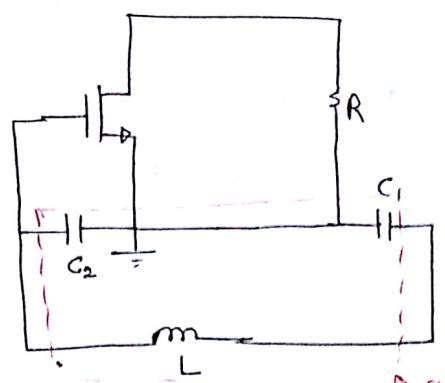
Here we will flow a current current in C, L_1 and L_2 will be same i.e. L_1, L_2 and C are in series for both L_1 and L_2 current entering from dot so additive polarity.

Solⁿ

$$f_0 = \frac{1}{2\pi\sqrt{L_{eq}C_{eq}}} = \frac{1}{2\pi\sqrt{L_{eq}C}}$$

$$\begin{aligned} L_{eq} &= L_1 + L_2 + 2M \\ &= 100 + 100 + 2 \times 20 \\ &= 240 \mu\text{H} \end{aligned}$$

$$f_0 = \frac{1}{2\pi\sqrt{240 \times 10^{-6} \times 0.001 \times 10^{-6}}}$$



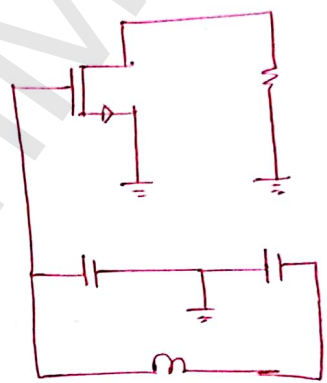
consider colpitt osc. ckt shown above with $L = 5 \mu H$ $C_1 = 1 nF$
 $C_2 = 1 nF$ $R = 4 k\Omega$ what is the f_o of osc. for the ckt.

$$f_o = \frac{1}{2\pi\sqrt{L C_{eq}}} = \frac{1}{2\pi\sqrt{L C_1}}$$

$$f_o = \frac{1}{2\pi\sqrt{10^{-6} \times 0.5 \times 10^{-9}}} \text{ Hz}$$

$$C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

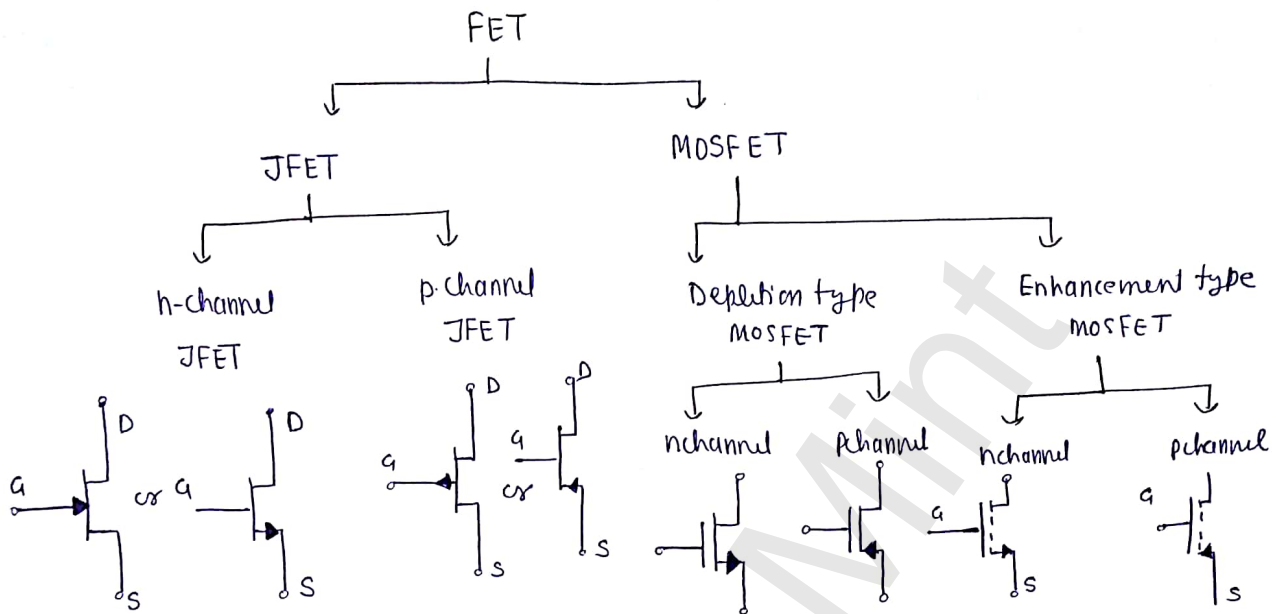
$$= \frac{1 \times 1}{1 + 1} = \frac{1}{2} = 0.5 nF$$



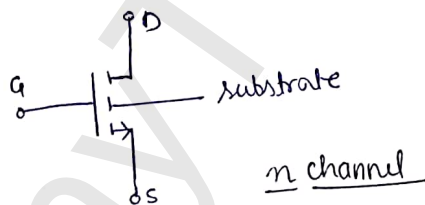
what is f_b ?

if R is across C_1 , then it is not colpitt osc. so we can't calculate from the formula $f_o = \frac{1}{2\pi\sqrt{L C_{eq}}}$ so we need to calc separately f_o from complete process.

Field Effect Transistor



Depletion mosfet and JFET ^{show} same char. ~~show~~
 follow same mathematical equations $I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$
 one more MOSFET



Biggest advantage of JFET is its i/p resistance is very high. whereas in BJT it is very low.

For JFET and Depletion type MOSFET

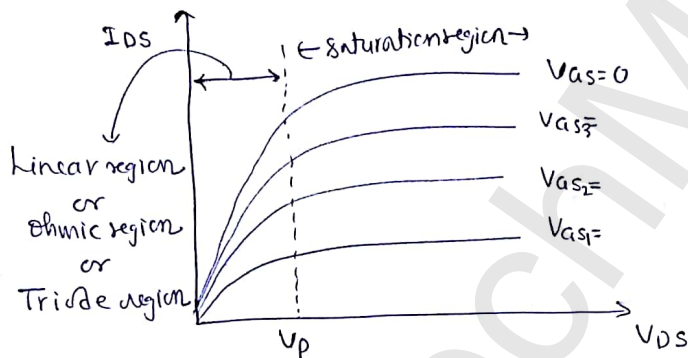
Drain Current

$$I_{DS} = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

Where $I_{DSS} \rightarrow$ Drain to source saturation current (when $V_{GS} = 0$)

$V_P \rightarrow$ pinch off voltage

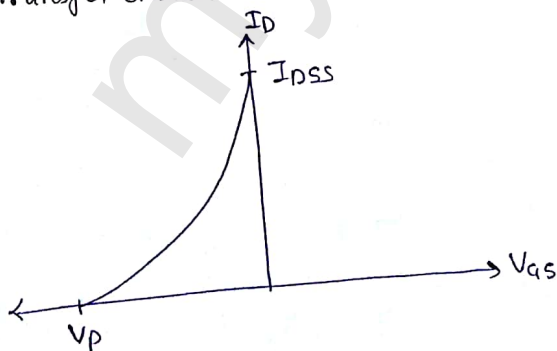
o/p characteristics



\Rightarrow used as an amp^r in saturation region for sat. region

$$V_{DS} \geq |V_{GS}| - |V_P|$$

Transfer characteristics



For Enhancement type mosFET

Drain to Source current

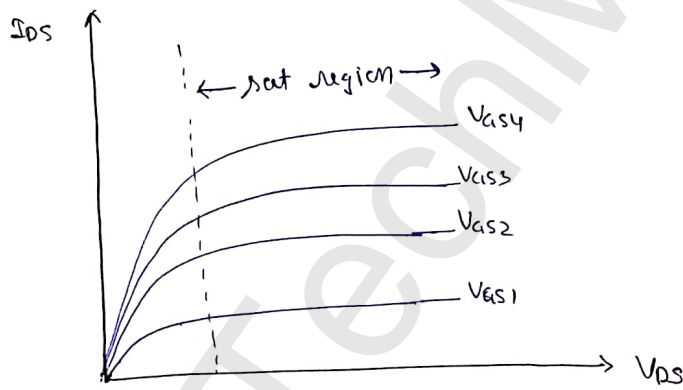
$$I_{DS} = K_n (V_{GS} - V_T)^2$$

where $K_n = \frac{1}{2} \mu_n C_{ox} \frac{W}{L}$

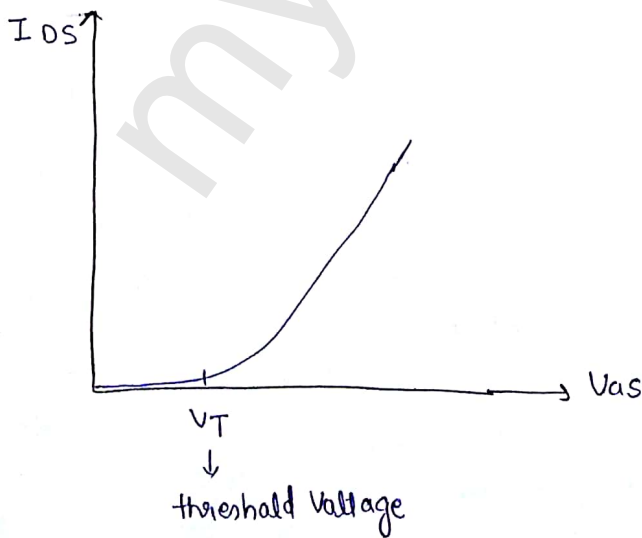
$$K_n = \frac{1}{2} K_n' \frac{W}{L}$$

$$I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T)^2$$

O/p characteristics

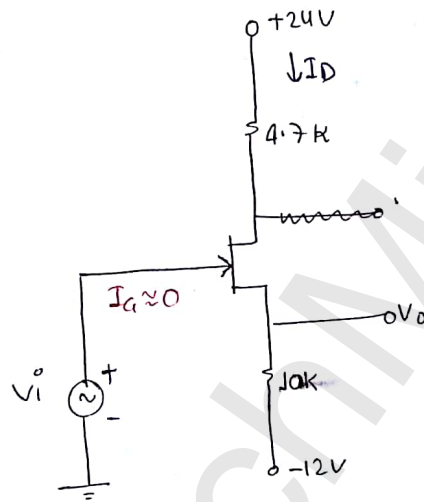


Transfer characteristics



Q The FET shown below has following parameters $I_{DSS} = 5.6 \text{ mA}$ and $V_p = -4 \text{ V}$

- If $V_i = 0$ find V_o
- If $V_i = 10 \text{ V}$ find V_o
- If $V_o = 0 \text{ V}$ find V_i
-



$I_g = 0$ is assumption that we take while solving FET questions.

Solⁿ.

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$I_D = 5.6 \text{ mA} \left(1 - \frac{V_{GS}}{-4}\right)^2$$

$$I_D = 5.6 \left(1 + \frac{12 - 10 I_D}{4}\right)^2$$

$$\frac{16}{5.6} I_D = (4 + 12 - 10 I_D)^2$$

$$2.86 I_D = 196 + 100 I_D^2 - 320 I_D$$

$$100 I_D^2 - 322.86 I_D + 196 = 0$$

$$I_D = \frac{322.86 \pm \sqrt{(322.86)^2 - 4 \times 100 \times 196}}{200}$$

$$I_D = \frac{322.86 \pm 160.74}{200} = 2.410 \text{ mA}, \quad 0.8106 \text{ mA}$$

$$-12.16 \quad 3.894$$

$$V_{GS} = -V_i + 10k I_D - 12$$

$$V_{GS} = 12 - 10k I_D$$

$$V_{GS} = 12 - 10 I_D$$

By Sn

$$V_i = 0$$

$$V_{as} + 10k I_{DS} - 12 = 0$$

$$I_{DS} = \frac{12 - V_{as}}{10} \text{ mA}$$

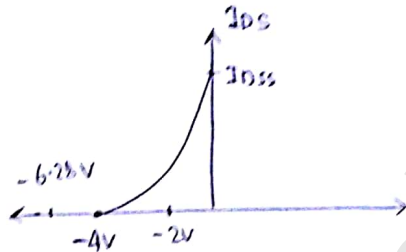
but

$$I_{DS} = I_{DSS} \left(1 - \frac{V_{as}}{V_p}\right)^2$$

$$\frac{12 - V_{as}}{10} \text{ mA} = 5.6 \text{ mA} \left(1 + \frac{V_{as}}{4}\right)^2$$

$$V_{as} = -2 \text{ V } \checkmark$$

$$= -6.26 \text{ V } (X)$$



$$V_{as} = -2$$

$$I_{DS} = \frac{12 + 2}{10} = 1.4 \text{ mA}$$

(ii) $V_i = 10 \text{ V}$

$$-10 + V_{as} + 10k I_{DS} - 12 = 0$$

$$I_{DS} = \frac{22 - V_{as}}{10} \text{ mA}$$

$$\frac{22 - V_{as}}{10} \text{ mA} = 5.6 \text{ mA} \left(1 + \frac{V_{as}}{4}\right)^2$$

$$V_{as} = -1.413 \text{ V } (\checkmark)$$

$$= -6.87 \text{ V } (X)$$

$$\therefore I_{DS} = \frac{1.413}{22 + 1142} = \frac{2.341}{2314} \text{ mA}$$

$$V_o = 10 \times 2.214 - 12$$

$$= 10.14$$

(ii) $V_o = 0$

$$V_o = 10K I_{DS} - 12$$

$$V_o = 10K I_{DS} - 12$$

$$I_{DS} = 1.2 \text{ mA}$$

$$1.2 \text{ mA} = 5.6 \text{ mA} \left[1 + \frac{V_{GS}}{4} \right]^2$$

$$V_{GS} = -2.148 \text{ V} \checkmark$$

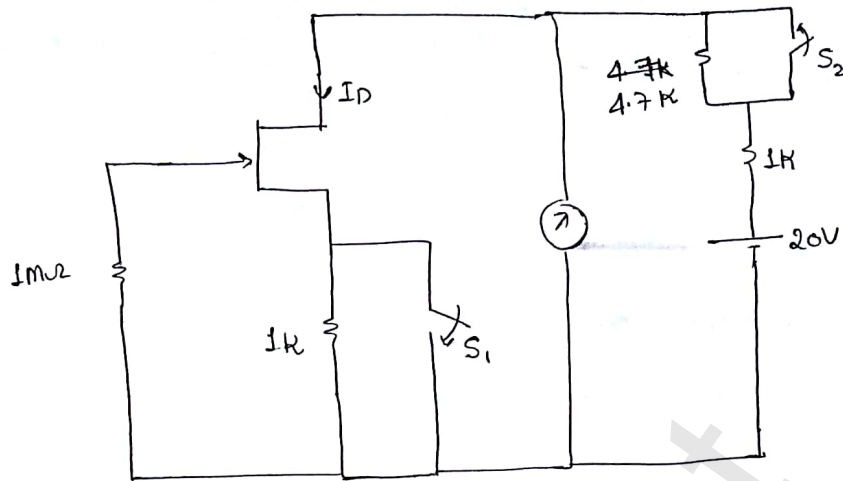
$$= -5.85 \text{ V} \times$$

$$V_{GS} = -2.148 \text{ V}$$

$$V_{GS} = V_G - V_S$$

$$V_{GS} = V_i - 0$$

$$V_i = V_{GS} = -2.148 \text{ V} \quad \underline{\underline{\text{Ans}}}$$



In the ckt of JFET shown below

- ① Find I_{DSS} when both switches S_1 and S_2 are closed take the reading of the dc voltmeter as 10V
- ② Find the operating point and dc voltmeter reading when both switches are open given $V_p = -5V$

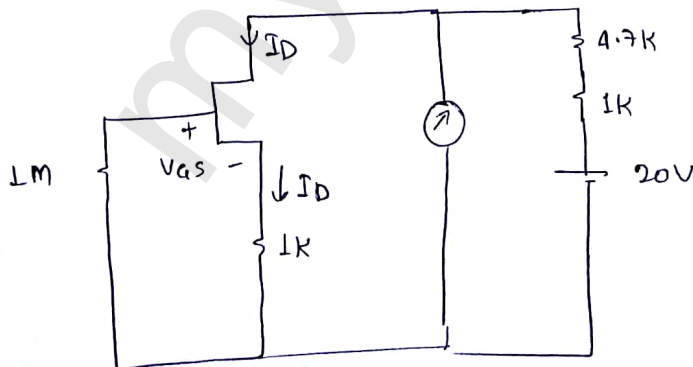
Solⁿ ① S_1 and S_2 are short ckt

$$V_{GS} = 0$$

$$I_D = I_{DSS}$$

$$I_D = I_{DSS} = \frac{20 - 10}{1K} = 10 \text{ mA}$$

②



$$V_{GS} + I_D 1K = 0$$

$$I_D = -V_{GS} \text{ mA}$$

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

$$-V_{GS} = I_{DSS} R_s \left(1 + \frac{V_{GS}}{V_P}\right)^2$$

$$V_{GS} = -2.5V$$
$$= -10V$$

$$V_{GS} = -2.5V$$

$$I_D = 2.5mA$$

$$-20 + 6.7k I_D + V_{DS} = 0$$

$$V_{DS} = 20 - 6.7 \times 2.5$$

$$V_{DS} = 3.25V$$

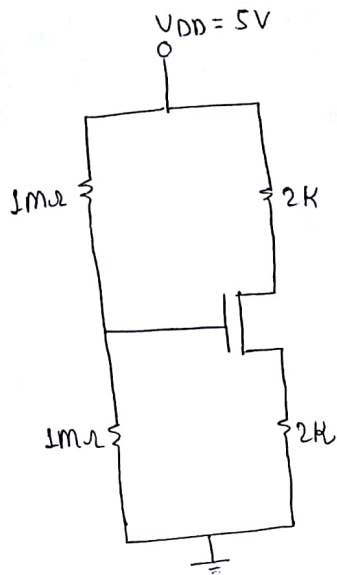
Operating point

$$= (3.25V, 2.5mA)$$

$$\text{Reading of voltmeter} = V_{DS} + I_D \times 1k$$

$$= 3.25 + 2.5$$

$$= ~~3.45~~ 5.75 \text{ volt}$$

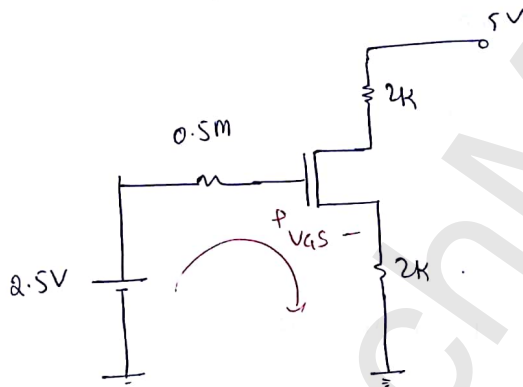


Calculate I_{DS} and V_{DS} for the ckt shown below assume $V_T = 1$ volt

and $k_n' \left(\frac{W}{L}\right) = 1 \text{ mA/V}^2$

$k_p \text{ Cox } \frac{W}{L} = 1 \text{ mA/V}^2$

Solⁿ



$2.5 = 0 + V_{GS} + I_{DS} 2k$

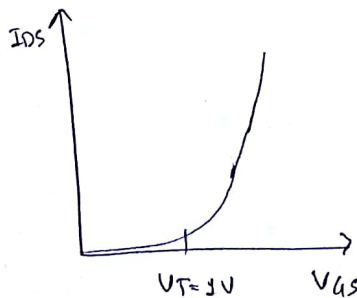
$I_{DS} = \frac{2.5 - V_{GS}}{2} \text{ mA}$

but $I_{DS} = \frac{1}{2} k_n \text{ Cox } \frac{W}{L} (V_{GS} - V_T)^2$

$\left(\frac{2.5 - V_{GS}}{2}\right) \text{ mA} = \frac{1}{2} \cdot 1 \cdot (V_{GS} - 1)^2$

$V_{GS} = 1.82 \text{ V}$ ✓

$V_{GS} = -0.82 \text{ V}$ ✗



$$V_{GS} = 1.82 \text{ V}$$

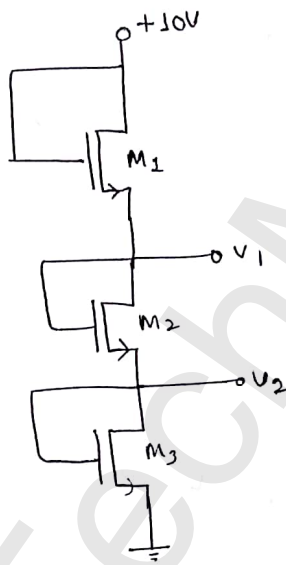
$$I_{DS} = \frac{2.5 - 1.82}{2} \text{ mA}$$

$$V_{DS} = 5 - 4k \times \left(\frac{2.5 - 1.82}{2} \right) \text{ m}$$

$$= 5 - 4x$$

$$V_{DS} = 3.64 \text{ Volt}$$

Question



In the ckt shown below the transistor parameters are $V_T = 1 \text{ V}$

and $k_n' = 36 \mu\text{A/V}^2$

if $I_{DS} = 0.5 \text{ mA}$

$V_1 = 5 \text{ V}$, $V_2 = 2 \text{ V}$ then calc

the $\frac{W}{L}$ ratio required in each transistor

Solution :

66 If Drain and gate are shorted then MOSFET is in saturation,,

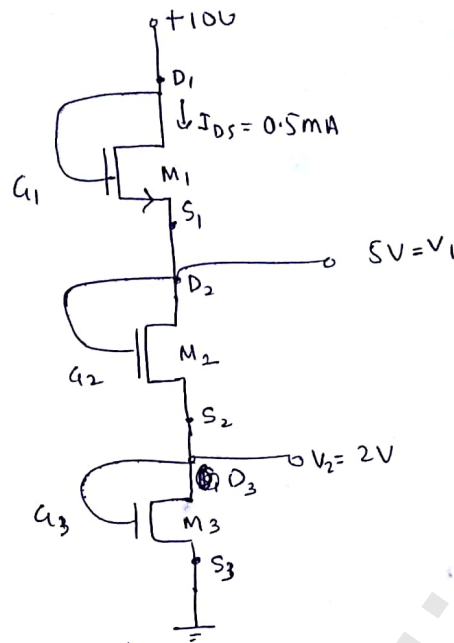
$$V_D = V_G$$

$$V_D - V_S = V_G - V_S$$

$$V_{DS} = V_{GS}$$

$$V_{DS} > V_{GS} - V_T$$

$$\Rightarrow \text{if } \boxed{V_{DS} \geq V_{GS} - V_T} \Rightarrow \text{MOSFET in saturation}$$



For M1

$$V_{GS1} = V_{G1} - V_{S1}$$

$$= 10 - 5 = 5V$$

$$\text{So } I_{DS} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS1} - V_T)^2$$

$$0.5 \text{ mA} = \frac{1}{2} \times 36 \mu \times \left(\frac{W}{L}\right)_1 (5-1)^2$$

$$\boxed{\left(\frac{W}{L}\right)_1 = 1.736}$$

For M2

$$V_{GS2} = V_1 = 5V$$

$$V_{DS2} = V_2 = 2V$$

$$\therefore V_{GS2} = 5 - 2 = 3V$$

$$0.5 \text{ mA} = \frac{1}{2} \times 36 \mu \times \left(\frac{W}{L}\right)_2 (3-1)^2$$

$$\left(\frac{W}{L}\right)_2 = 6.94 \text{ } \mu\text{m}$$

For M_3

$$V_{G3} = V_2 = 2V$$

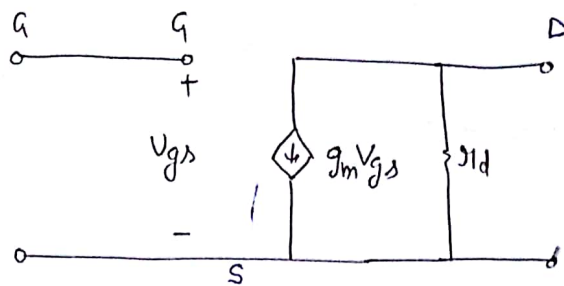
$$V_{S3} = 0$$

$$V_{G3S3} = 2V$$

$$0.5 \text{ m} = \frac{1}{2} 36 \mu \left(\frac{\omega}{L}\right)_3 \times (2-1)^2$$

$$\boxed{\left(\frac{\omega}{L}\right)_3 = 27.7 \text{ } \mu\text{m}}$$

FET AC Analysis or AC Eq^v Model



r_{id} - drain to source ac resistance

$$r_{id} = \frac{1}{\text{slope of } \sigma_p \text{ characteristics}}$$

$$r_{id} = \frac{1}{\lambda I_{DQ}}$$

I_{DQ} - Drain to source Q point current DC bias current

λ → channel length modulation paramtr.

$V_A = \frac{1}{\lambda}$ → Early voltage of FET

If channel length modulation is negligible or λ is not given then

$r_{id} \rightarrow \infty$

$$\text{unit of } \lambda = \frac{1}{V_A} = \text{volt}^{-1}$$

~~λ is calculated by slope of transfer characteristic~~

g_m

$$g_m = \frac{\partial I_{DS}}{\partial V_{GS}}$$

For JFET and depletion type mosfet:

$$I_{DS} = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$\frac{\partial I_{DS}}{\partial V_{GS}} = \frac{\partial I_{DSS}}{\partial V_{GS}} = I_{DSS} \times 2 \left(\frac{-1}{V_p}\right) \left(1 - \frac{V_{GS}}{V_p}\right)$$

$$g_m = \frac{-2I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)}{V_p}$$

$$g_m = \frac{2I_{DSS}}{|V_p|} \left(1 - \frac{V_{GS}}{V_p}\right) \quad \text{---(I)}$$

or

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_p}\right) \quad \text{---(II)} \quad \text{where } g_{m0} = \frac{2I_{DSS}}{|V_p|}$$

we have

$$\left(1 - \frac{V_{GS}}{V_p}\right) = \sqrt{\frac{I_{DS}}{I_{DSS}}}$$

so

$$g_m = \frac{2I_{DSS}}{|V_p|} \times \sqrt{\frac{I_{DS}}{I_{DSS}}}$$

$$\Rightarrow g_m = \frac{2}{|V_p|} \sqrt{I_{DS} \cdot I_{DSS}}$$

objective

- g_m vs I_{DS} — parabola curve
- g_m vs V_{GS} — straight line

in BJT g_m is exponential func of i/p voltage. so g_m rises rapidly bcz exponential curve rises faster.

- * Transconductance of FET is less than BJT due to which gain of FET is less (disadvantage)

$A_v \propto g_m$

$$A_v = -g_m R_L$$

* gain is less

g_m for Enhancement type MOSFET

$$I_{DS} = k_n (V_{GS} - V_T)^2 \quad \text{--- (1)}$$

$$\frac{\partial I_{DS}}{\partial V_{GS}} = 2k_n (V_{GS} - V_T)$$

$$\boxed{g_m = 2k_n (V_{GS} - V_T)} \quad \text{--- (2)}$$

but $k_n = \frac{1}{2} \mu_n \epsilon_{ox} \frac{w}{L}$

$$g_m = 2 \times \frac{1}{2} \mu_n \epsilon_{ox} \frac{w}{L} (V_{GS} - V_T)$$

$$\boxed{g_m = \mu_n \epsilon_{ox} \frac{w}{L} (V_{GS} - V_T)} \quad \text{--- (3)}$$

From eqⁿ

$$V_{GS} - V_T = \sqrt{\frac{I_{DS}}{k_n}}$$

∴ From eqⁿ (2)

$$g_m = 2k_n \sqrt{\frac{I_{DS}}{k_n}}$$

$$\Rightarrow g_m = \sqrt{4k_n I_{DS}}$$

$$g_m = \sqrt{4 \times \frac{1}{2} \mu_n \epsilon_{ox} \frac{w}{L} I_{DS}}$$

$$\boxed{g_m = \sqrt{2 \mu_n \epsilon_{ox} \frac{w}{L} I_{DS}}}$$

I_{DS} = DC bias current Drain to source.

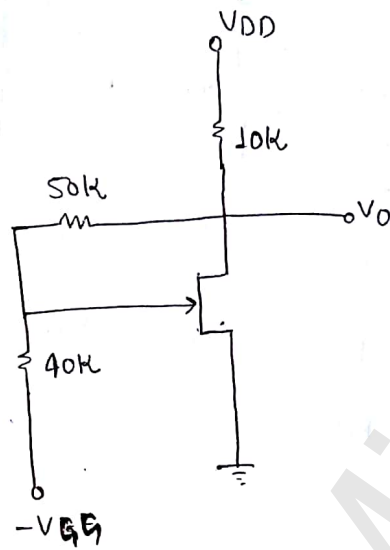
Note* For any FET

$$\boxed{\mu = g_m r_{id}}$$

where μ = amplification factor

μ = unit less

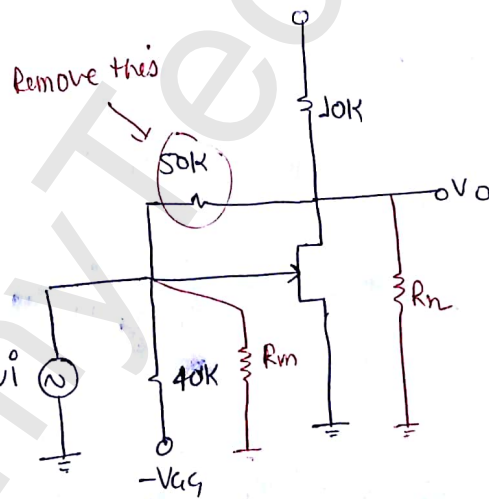
Question



If an i/p sig V_i is impressed b/w gate and ground find the amplification $A = \frac{V_o}{V_i}$

apply millers theorem to the 50k resistor the FET parameters are $\mu = 30$ and $g_{d1} = 5k\Omega$ neglect capacitances.

Solution

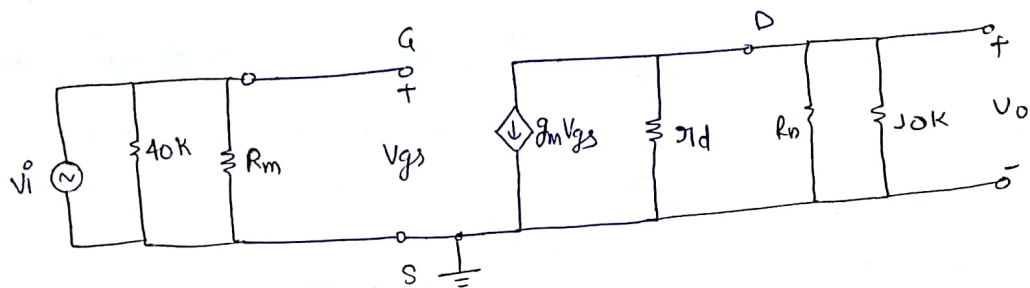


$$\mu = 30$$

$$g_{d1} = 5k$$

$$\mu = g_m g_{d1}$$

$$\Rightarrow g_m = \frac{\mu}{g_{d1}} = \frac{30}{5k} = 6mA/V$$



First we need to find open loop voltage gain i.e. by removing R_m and R_n voltage gain without R_m and R_n

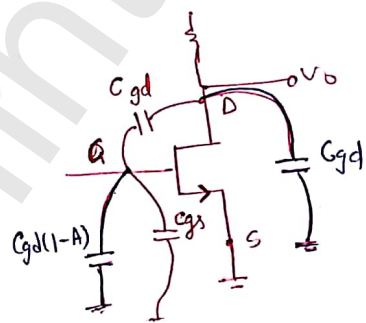
$$V_{gs} = V_i$$

$$V_o = -g_m V_{gs} (r_{ds} \parallel 10k)$$

$$\frac{V_o}{V_{gs}} = \frac{V_o}{V_i} = A = -g_m (r_{ds} \parallel 10k)$$

$$= -6m \left(\frac{5k \times 10k}{15k} \right)$$

$$= -20$$



Now

$$R_m = \frac{50k}{1 - (-20)} = \frac{50k}{21} = 2.38k$$

$$R_n = \frac{50k}{1 - \frac{1}{A}} = \frac{50k}{1 + \frac{1}{20}} = 47.62$$

In gate.

Multe*

$$C_i = C_{gs} + (1-A)C_{gd}$$

↑
input capacitance.

Voltage gain ofckt (connecting R_m and R_n)

$$V_{gs} = V_i$$

$$V_o = -g_m V_{gs} (r_{ds} \parallel R_m \parallel R_n \parallel 10k)$$

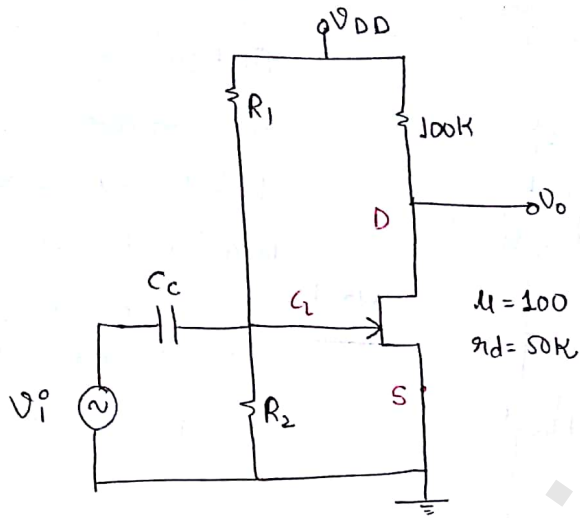
$$\frac{V_o}{V_{gs}} = \frac{V_o}{V_i} = A_f = -g_m (r_{ds} \parallel R_n \parallel 10k)$$

$$= -6 \frac{mA}{V} (5 \parallel 47.62 \parallel 10k)$$

$$= -6 (3.33 \parallel 47.62) = -6 \times 3.11$$

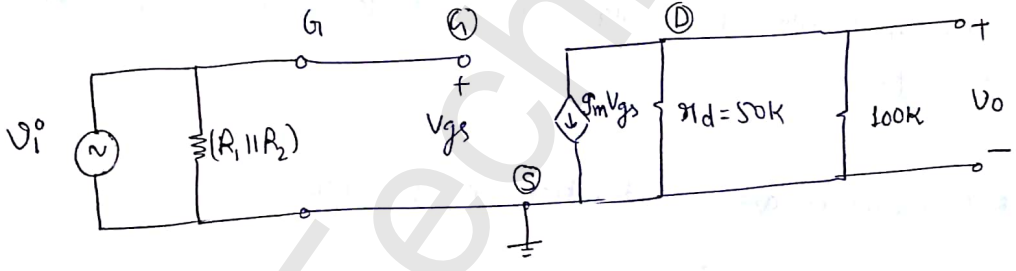
$$\boxed{\frac{V_o}{V_{gs}} = -18.67}$$

Q



For the ckt shown below draw the ac eq^v ckt and find voltage gain of the amplifier

Solⁿ



$$\mu = 100 = g_m r_{d1}$$

$$g_m = \frac{100}{50k} = 2 \text{ mA/V}$$

$$V_{gs} = V_i$$

$$V_o = -g_m V_{gs} (r_{d1} \parallel 100k)$$

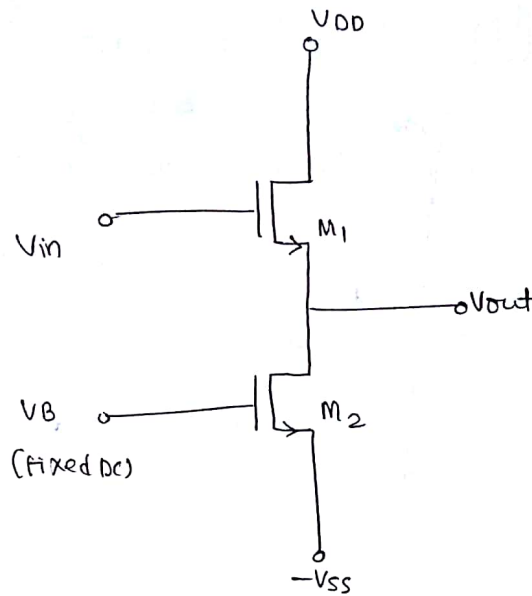
$$\frac{V_o}{V_{gs}} = -g_m (r_{d1} \parallel 100k)$$

$$\frac{V_o}{V_i} = A_v = -2 \times 10^{-3} (33.33 \times 10^3)$$

$$= -66.66$$

P2

11)



The figure below is a source follower using an n-channel MOSFET. Assume that M_1 and M_2 both are in saturation and have different transconductance parameters k_1 and k_2 where $k_i = \mu_n C_{ox} \left(\frac{W}{L}\right)_i$ $i=1,2$ and symbols have their usual meaning.

Derive an expression for V_{out} in terms of V_{in} , V_{DD} , V_{SS} , V_B , V_T and k_1, k_2 . Find the op small sig voltage gain and dc offset voltage appearing at the op.

Solⁿ

Both M_1 and M_2 are in saturation so $I_{D1} = I_{D2}$

$$I_{D1} = I_{D2}$$

$$k_1 (V_{GS1} - V_T)^2 = k_2 (V_{GS2} - V_T)^2$$

$$k_1 [V_{in} - V_{out} - V_T]^2 = k_2 [V_B - (-V_{SS}) - V_T]^2$$

$$k_1 [V_{in} - V_{out} - V_T]^2 = k_2 [V_B + V_{SS} - V_T]^2$$

$$V_{in} - V_{out} - V_T = \sqrt{\frac{k_2}{k_1}} [V_B + V_{SS} - V_T]$$

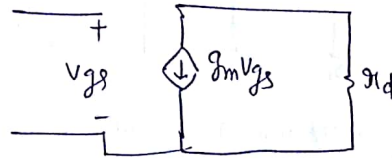
$$V_{out} = V_{in} - V_T - \sqrt{\frac{k_2}{k_1}} [V_B + V_{SS} - V_T]$$

$$V_{out} = V_{in} + V_T \left[\sqrt{\frac{k_2}{k_1}} - 1 \right] - \sqrt{\frac{k_2}{k_1}} (V_B + V_{SS})$$

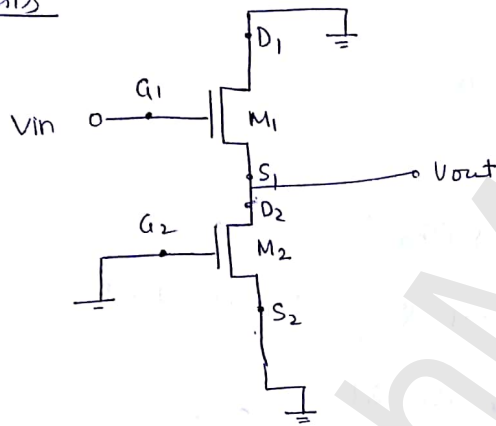
op offset voltage is $V_{out} = V_{oo}$ if $V_{in} = 0$

$$V_{oo} = \left(\sqrt{\frac{k_2}{k_1}} - 1 \right) V_T - \sqrt{\frac{k_2}{k_1}} (V_B + V_{SS})$$

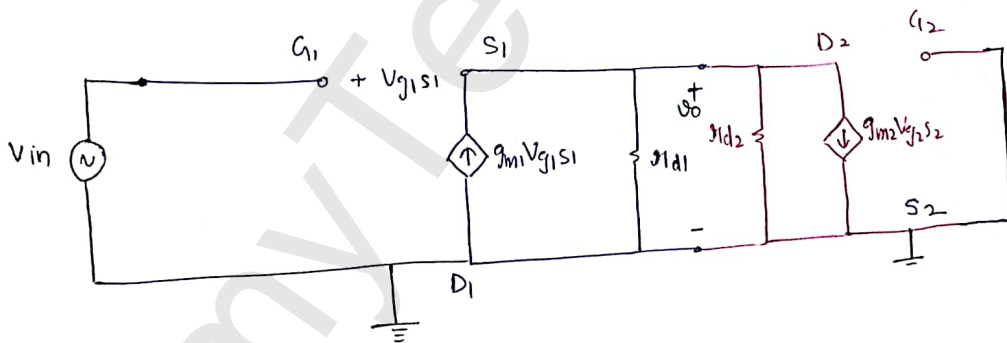
ac analysis.



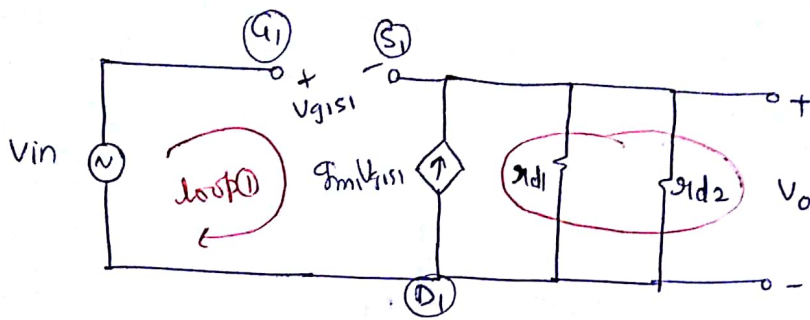
Ac analysis



g_{m1} and g_{m2} are different i.e given in question.



C_2 S_2 short means $V_{gs2} = 0$
 means $g_{m2} V_{gs2} = 0$ i.e make current source open



$$V_o = g_{m1} V_{gs1} (r_{d1} \parallel r_{d2}) \rightarrow \textcircled{1}$$

KVL in loop $\textcircled{1}$

$$-V_{in} + V_{gs1} + V_o = 0$$

$$V_{gs1} = V_{in} - V_o$$

$$V_o = g_{m1} (r_{d1} \parallel r_{d2}) (V_{in} - V_o)$$

$$\Rightarrow V_o = g_{m1} (r_{d1} \parallel r_{d2}) V_{in} - g_{m1} (r_{d1} \parallel r_{d2}) V_o$$

$$\frac{V_o}{V_{in}} = A_v = \frac{g_{m1} (r_{d1} \parallel r_{d2})}{1 + g_{m1} (r_{d1} \parallel r_{d2})} \approx 1$$

u-gnd.

Most Important

OP- Amp

⇒ Available as IC-741 in 8 pin package

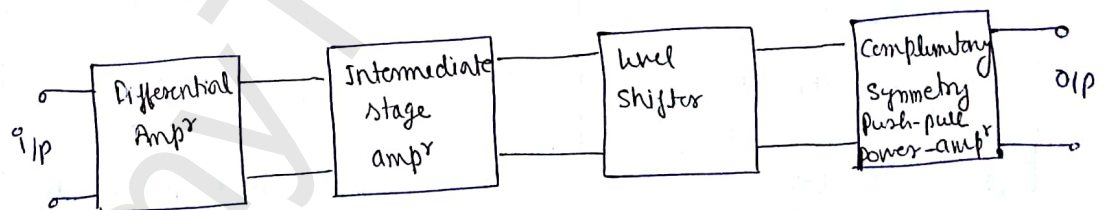
7 : 7 pins are used

4 : 4 pins as i/p pins (inverting i/p and non inverting i/p)
($+V_{CC}$, $-V_{EE}$)

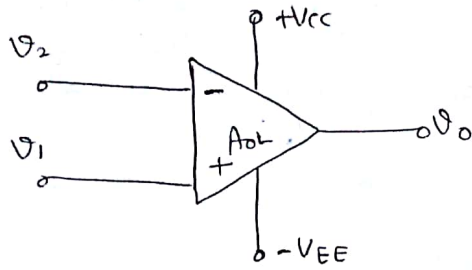
1 : 1 pin as o/p.

Note :- Remaining 2 pins are used ^{for} as off set null balancing.

⇒ It is a direct coupled multistage amplifier with very high voltage gain



Q why op-amp called op-amp?



$$V_o = A_{oL} V_d$$

$$V_o = A_{oL} (V_1 - V_2) \quad \text{Governing equation}$$

$$V_d = V_1 - V_2$$

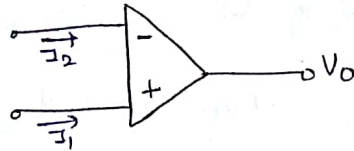
Obj

V.Imp.

properties of op-amp

S.No.	Parameter	Ideal op amp.	Practical op-amp
1.	A_{oL}	∞	Practical op-amp
2.	R_i	∞	1 to 2 M Ω
3.	R_o	0	50 to 100 Ω
4.	BW	∞	open loop BW = 5 Hz
5.	offset voltage	if $V_1=0, V_2=0$ then $V_o=0$	if $V_1=0, V_2=0$ then $V_o \neq 0$
6.	CMRR	∞	10^6 or 120 dB
7.	slur rate	∞	0.5 to 1 V/ μ sec

Some imp^r defⁿ For practical op-amp



① Input Bias Current

It is the avg of two currents I_1 and I_2 which flow into the i/p node

For IC 741 : 100's of nA

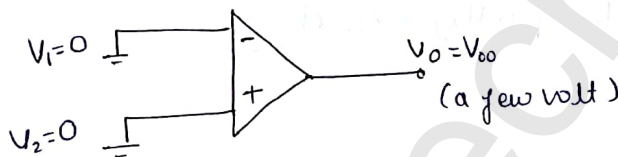
② Input offset current

It is the difference of I_1 and I_2

$$I_{io} = I_1 \sim I_2 \quad \text{: For IC 741 a few nA}$$

↳ this sign indicates that subtract smaller one from larger one.

③ op offset voltage



V_{00} = op offset voltage

④ i/p offset voltage It is the voltage which must be applied as difference i/p to make the op voltage 0.

$$\text{If } V_d = V_{io} \text{ then } V_o = 0$$

↓
10's of μV

⑤ Power supply rejection ratio (PSRR or SPRR)

It is a measure of change in i/p offset voltage due to changes in supply voltages and is given by

$$\text{PSRR in dB} = 20 \log \frac{\Delta V_s}{\Delta V_{io}} \rightarrow \begin{matrix} \text{change in i/p supply vltz} \\ \text{" " " offset vltz} \end{matrix}$$

⑥ CMRR

It is the ratio of differential ^{mode} gain to the common mode gain

$$CMRR = \frac{A_{dm}}{A_{cm}}$$

A_{dm} - diff^r mode gain

A_{cm} - common mode gain

$$CMRR \text{ in dB} = 20 \log \left(\frac{A_{dm}}{A_{cm}} \right)$$

$$= A_{dm} (\text{in dB}) - A_{cm} (\text{in dB})$$

CMRR is a measure of sensitivity of a differential amp^r to common mode ip such as noise.

High CMRR indicates that op-amp is efficiently rejecting the noise sig.

⑦ Slew rate Max^m rate at which op voltage can change

$$SR = \left. \frac{dV_o}{dt} \right|_{\max}$$

consider an op-amp with closed loop gain A_{CL}

$$\therefore V_o = A_{CL} V_i$$

$$\text{If } V_i = V_m \sin \omega t$$

$$\text{then } V_o = A_{CL} V_m \sin \omega t$$

$$\text{So } \left. \frac{dV_o}{dt} \right|_{\max} = (A_{CL} V_m \omega \cos \omega t) \Big|_{\max}$$

$$SR = A_{CL} V_m \cdot \omega$$

$$SR = 2\pi A_{CL} V_m f \quad \frac{\text{volt}}{\text{sec}}$$

$$SR = \frac{2\pi A_{CL} V_m f}{10^6} \quad \frac{\text{volt}}{\mu\text{sec}}$$

SR provided by manufacturer.

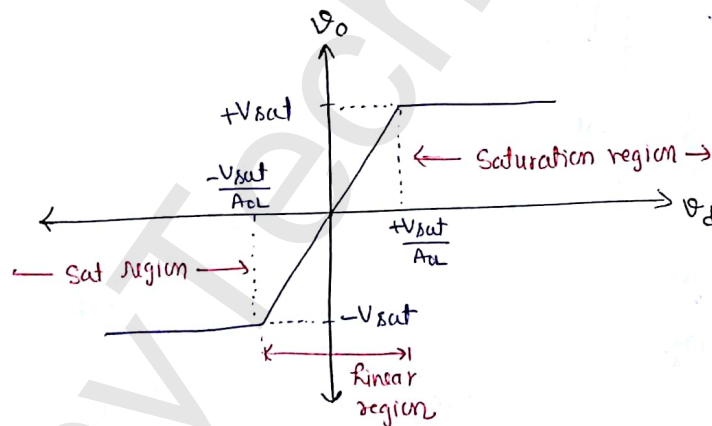
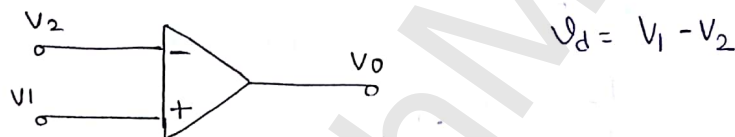
To obtain distortionless output

$$SR \leq \frac{2\pi A_{CL} f V_m}{10^6} \text{ V}/\mu\text{sec}$$

Note* In question if A_{CL} is not given then

$$A_{CL} = 1$$

Transfer characteristics



⇒ op-amp can be used as an amp^r only in linear region.

⇒ with +ve fb configuration or with open loop configuration op-amp always operates in saturation region

i.e. $V_0 = \pm V_{sat}$ for open loop or +ve feedback.

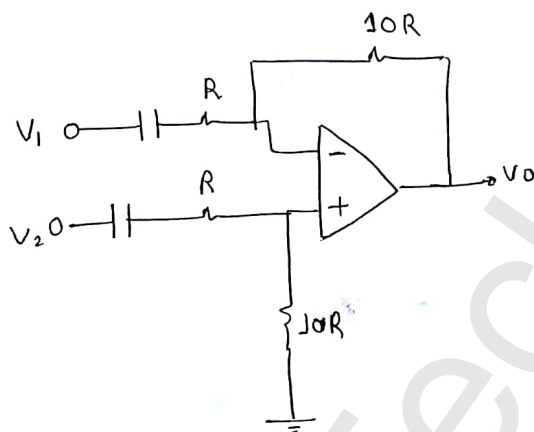
⇒ For -ve feedback configuration op-amp can be operated in linear region

In this case $V_o = A_{OL}(V_1 - V_2)$ but $A_{OL} \rightarrow \infty$, so $V_1 - V_2 = 0$

$$V_1 - V_2 = \frac{V_o}{A_{OL}} \Rightarrow \boxed{V_1 \approx V_2} \Rightarrow \text{Inverting and non-inverting terminals are virtually short-circuited to each other.}$$

Note* Virtual Short (vt) concept ($V_1 = V_2$) is valid for negative feedback opamp and this concept is not applicable for open loop or no feedback opamp.

110



In fig if offset voltage of the opamp is 2mV calc the O/P^{dc} error voltage or dc offset voltage.

O/p offset voltage =

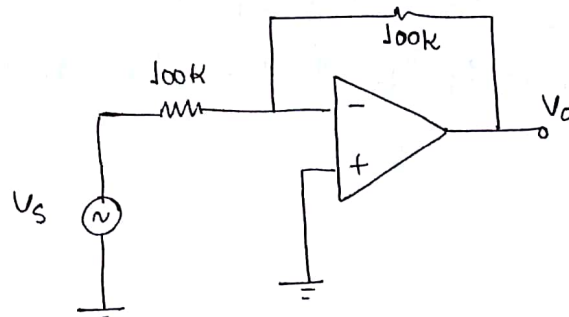
$$\boxed{V_{oo} = \left(1 + \frac{R_f}{R}\right) V_{io}}$$

For inverting opamp and non-inverting opamp both

$$V_{oo} = \left(1 + \frac{10R}{R}\right) V_{io}$$

$$V_{oo} = 11 \times 2\text{mV} = 22\text{mV}$$

Q In the ckt shown below the op-amp has i/p bias current $I_b < 10\text{nA}$ and i/p offset vltage $V_{io} < 1\text{mV}$ calc the max^m dc error voltage in the op



DC error voltage in the op. of op-amp

① Due to bias current

$$\begin{aligned} V_{o01} &= |I_b R_F| \\ &= |10 \times 10^{-9} \times 100 \times 10^3| \\ &= 1\text{mV} \end{aligned}$$

② Due to i/p offset voltage

$$\begin{aligned} V_{o02} &= \left(1 + \frac{R_F}{R}\right) V_{io} \\ &= \left(1 + \frac{100\text{k}}{100\text{k}}\right) \times 1 \\ &= 2\text{mV} \end{aligned}$$

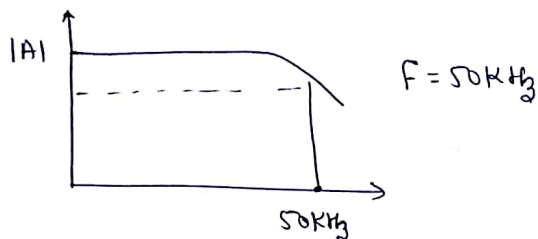
So total error in op voltage

$$\begin{aligned} V_{o0} &= V_{o01} + V_{o02} \\ &= 1\text{mV} + 2\text{mV} \\ V_{o0} &= 3\text{mV} \end{aligned}$$

Q Define and use the expression for slew rate of op-amp. op-amp has slew rate

has slew rate of $0.5 \text{ V}/\mu\text{sec}$. It is used as a non-inverting amp^r with gain of 25. the voltage gain against f_m curve is flat upto 50 kHz . Calc^e the max^m (p-p) i/p sig that can be applied to get undistorted o/p.

$$A_{CL} = 25$$



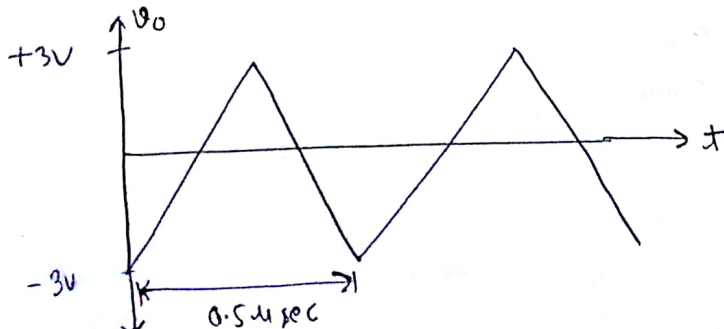
$$SR \leq \frac{2\pi f A_{CL} V_m}{10^6}$$

$$\Rightarrow 0.5 \leq \frac{2\pi \cdot 50 \times 10^3 \times 25 \times V_m}{10^6}$$

$$V_m = 63.7 \text{ mV}$$

$$\begin{aligned} \text{peak to peak i/p} &= 2 \times 63.7 \text{ mV} \\ &= 127.4 \text{ mV} \end{aligned}$$

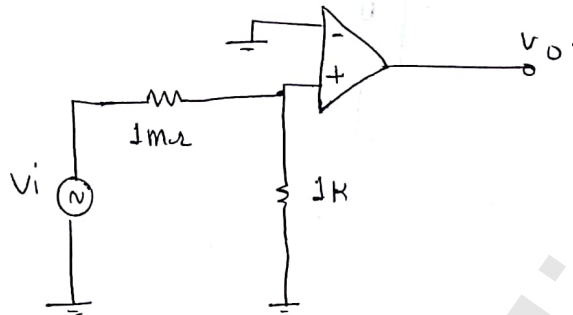
Q. The o/p of an op-amp voltage follower is a triangular wave. assume for a square wave i/p of f_m of 2 MHz and 8 volt (p-p) voltage what is the slew rate of op-amp.



$$SR = \left. \frac{dV_o}{dt} \right|_{\max} = \frac{3 - (-3)}{0.5/2} \text{ V}/\mu\text{sec}$$

$$SR = 24 \text{ V}/\mu\text{sec}$$

②

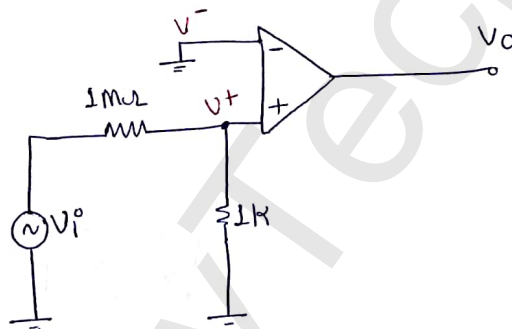


The fig shown uses an opamp that is ideal except for having finite gain A . measurement indicate that $V_o = 4 \text{ volt}$ when $V_i = 4 \text{ volt}$. What is the opamp gain A (open loop gain)

solⁿ

$$V_o = 4 \text{ V}$$

$$V_i = 4 \text{ V}$$



$$V^+ = \frac{V_i \times 1K + 0 \times 1m}{1m + 1K}$$

$$= \frac{V_i \times 1K}{1001K}$$

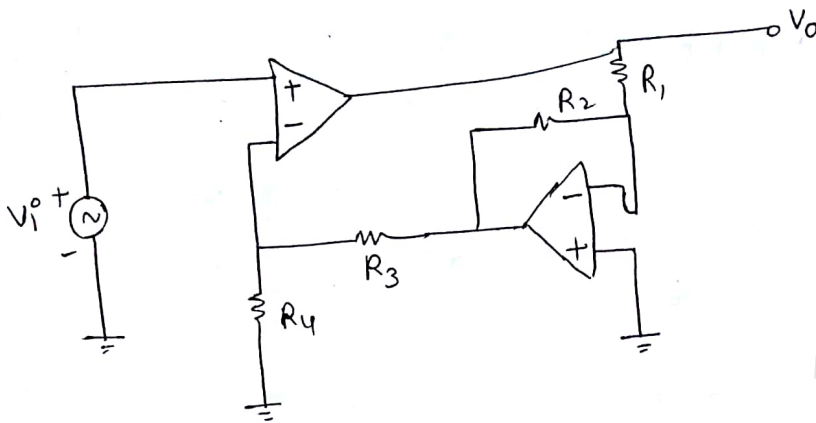
$$V_o = A(V^+ - V^-) \quad \leftarrow \text{this always valid either +ve loop, -ve loop or open loop.}$$

$$V_o = A \left(\frac{V_i}{1001} - 0 \right)$$

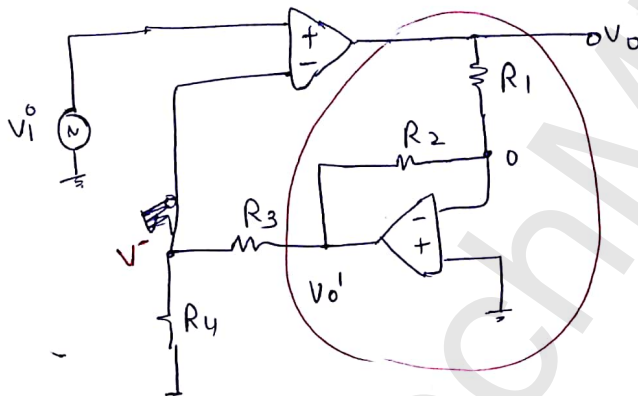
$$A = 1001 \frac{V_o}{V_i}$$

$$A = 1001 \times \frac{4}{4} = 1001$$

Q For the ckt shown below cal^c $\frac{V_o}{V_i}$



Solⁿ



$$V_{o'} = -\frac{R_2}{R_1} V^-$$

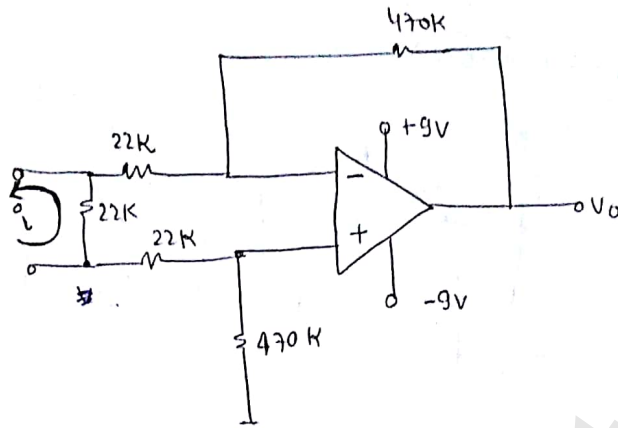
$$V^- = \frac{R_4}{R_3 + R_4} V_i$$

$V^- = V_i$ virtual gnd.

$$V^- = \frac{R_4}{R_3 + R_4} \left(-\frac{R_1}{R_2} \right) V_o = V_i$$

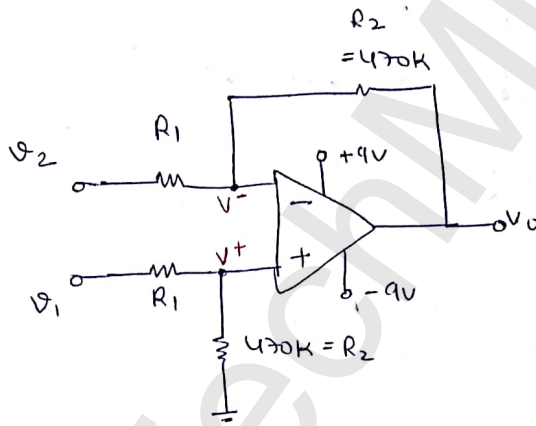
$$\Rightarrow \frac{V_o}{V_i} = \frac{1}{\left(\frac{R_4}{R_3 + R_4} \right) \left(-\frac{R_2}{R_1} \right)}$$

110



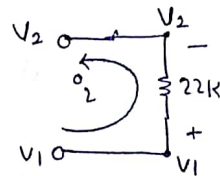
calc the op voltage of the ckt if ip sig current i is $5.5 \mu A$

Solⁿ



$$V^+ = \frac{R_2 \cdot V_1}{R_1 + R_2}$$

$$V^- = \frac{V_2 \times R_2 + V_0 \times R_1}{R_1 + R_2}$$



$$V^+ = V^-$$

$$\frac{R_2}{R_1 + R_2} \cdot V_1 = \frac{V_2 R_2 + V_0 R_1}{R_1 + R_2}$$

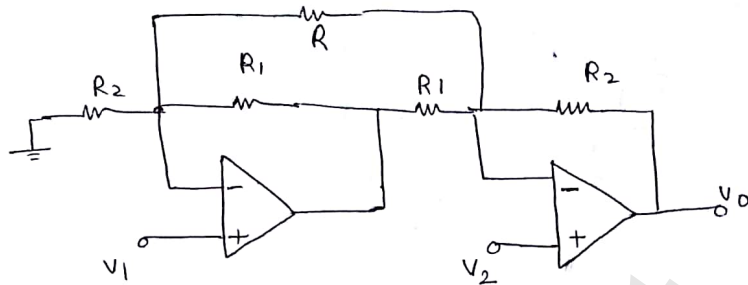
$$V_0 R_1 = R_2 (V_1 - V_2)$$

$$V_0 = \frac{R_2}{R_1} (V_1 - V_2)$$

$$\text{So } V_1 - V_2 = i \times 22K = 5.5 \times 10^{-3} \times 22$$

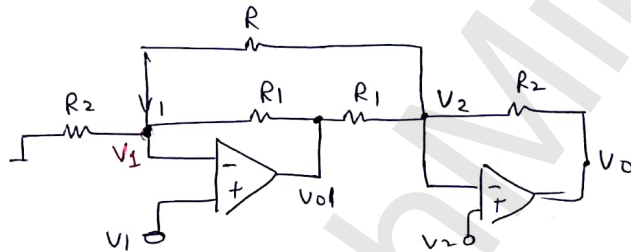
$$V_o = \frac{470}{22} (5.5 \times 10^{-3} \times 22)$$

10



Calculate V_o in terms of V_1 and V_2 and resistances.

Solⁿ



KCL at V_1

$$\frac{V_1}{R_2} + \frac{V_1 - V_2}{R} + \frac{V_1 - V_{o1}}{R_1} = 0$$

$$\frac{V_1}{R_2} + \frac{V_1}{R_1} - \frac{V_{o1}}{R_1} + \frac{V_1}{R} - \frac{V_2}{R} = 0$$

$$\frac{V_{o1}}{R_1} = V_1 \left(\frac{1}{R_2} + \frac{1}{R_1} + \frac{1}{R} \right) - \frac{V_2}{R}$$

$$\Rightarrow V_{o1} = V_1 \left(1 + \frac{R_1}{R_2} + \frac{R_1}{R} \right) - \frac{R_1}{R} V_2 \quad \text{--- (1)}$$

KCL at V_2

$$\frac{V_2 - V_{o1}}{R_1} + \frac{V_2 - V_1}{R} + \frac{V_2 - V_o}{R_2} = 0$$

$$\frac{V_o}{R_2} = \frac{V_2}{R_1} - \frac{V_{o1}}{R_1} + \frac{V_2}{R} - \frac{V_1}{R} + \frac{V_2}{R_2}$$

$$\Rightarrow V_o = \left(\frac{R_2}{R_1} + \frac{R_2}{R} + 1 \right) V_2 - \frac{R_2}{R} V_1 - \frac{R_2}{R_1} V_{o1}$$

$$V_o = \left(1 + \frac{R_2}{R} + \frac{R_2}{R_1}\right) V_2 - \frac{R_2}{R} V_1$$

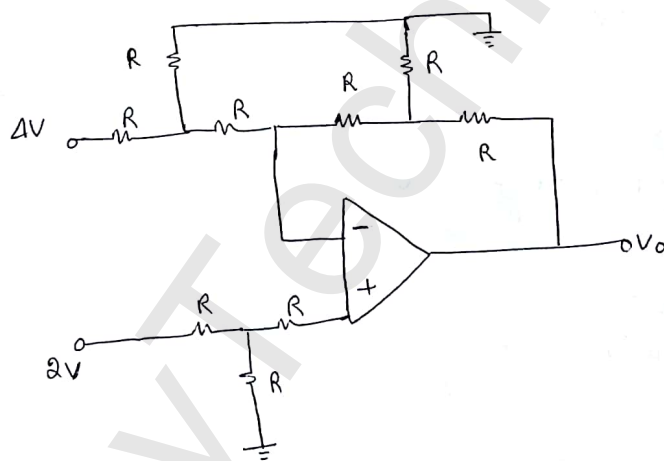
$$= -\frac{R_2}{R_1} \left[V_1 + \frac{R_1}{R} V_1 + \frac{R_1}{R_2} V_1 - \frac{R_1}{R} V_2 \right]$$

$$\Rightarrow V_o = V_2 + \frac{R_2}{R} V_2 + \frac{R_2}{R_1} V_2 - \frac{R_2}{R} V_1 - \frac{R_2}{R_1} V_1 - \frac{R_2}{R} V_1 - V_1 + \frac{R_2}{R} V_2$$

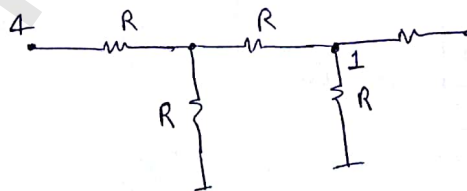
$$= V_2 \left[1 + \frac{R_2}{R} + \frac{R_2}{R_1} + \frac{R_2}{R} \right] + V_1 \left[-\frac{R_2}{R} - \frac{R_2}{R_1} - \frac{R_2}{R} - 1 \right]$$

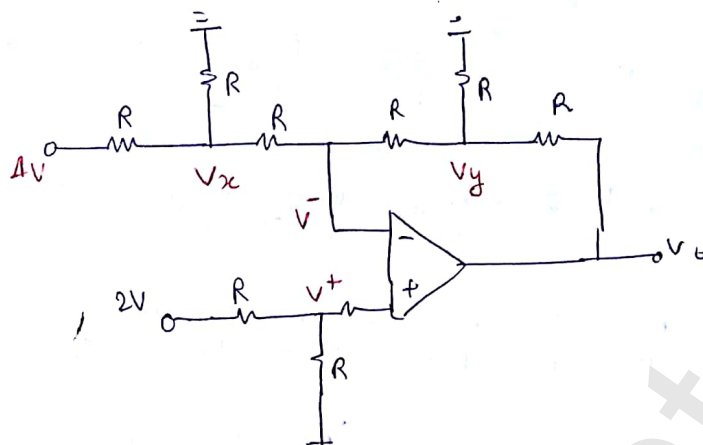
$$= V_2 \left[1 + \frac{R_2}{R_1} + \frac{2R_2}{R} \right] - V_1 \left[1 + \frac{R_2}{R_1} + \frac{2R_2}{R} \right]$$

$$V_o = \left[1 + \frac{R_2}{R_1} + \frac{2R_2}{R} \right] (V_2 - V_1)$$



sum





$$V^+ = \frac{R}{R+R} \cdot 2 = 1V$$

By virtual ground
 $V^+ = V^- = 1V$

KCL at V_x

$$\frac{V_x}{R} + \frac{V_x - 4}{R} + \frac{V_x - 1}{R} = 0$$

$$3V_x - 5$$

$$V_x = \frac{5}{3}$$

KCL at V_y

$$\frac{V_y}{R} + \frac{V_y - 1}{R} + \frac{V_y - v_o}{R} = 0$$

$$3V_y = 1 + v_o$$

$$\boxed{v_o = 3V_y - 1} \rightarrow \textcircled{1}$$

KCL at V^-

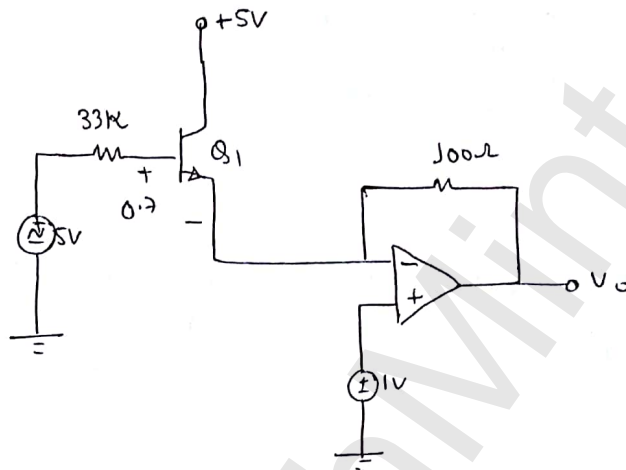
$$\frac{1 - V_x}{R} + 1 - \frac{V_y}{R} = 0$$

$$2 \times 1 = \frac{5}{3} + \frac{V_y}{R}$$

$$V_y = 2 - \frac{5}{3} = \frac{1}{3}$$

$$\text{So } V_o = 3 \times \frac{1}{3} - 1 \\ = 0 \text{ volt.}$$

Question



Assume base emitter voltage of 0.7 volt and $\beta = 99$ of Q_1 (Tr) calc the op voltage V_o in the ckt shown.

$$-5 + I_B 33k + 0.7 + 1 = 0$$

$$I_B = \frac{0.3}{33} = 0.1 \text{ mA}$$

$$I_E = I_C + I_B = 100 \times$$

$$= (\beta + 1) I_B = 100 \times 0.1 \text{ mA} = 20 \text{ mA} \quad \text{--- } 10 \text{ mA}$$

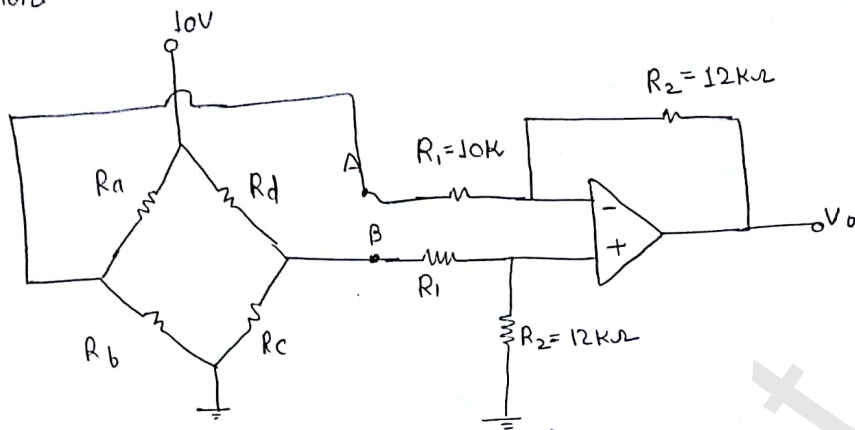
$$= 100 \times 0.1 \times 10^{-3} = \frac{100 \times 1}{1000 \times 10} = 0.01$$

$$1 - V_o = 100 \times 10 \quad 100 \times 0.01$$

$$1 - V_o = 1$$

$$V_o = 0 \text{ volt}$$

Question



The ckt shown uses an ideal opamp. assume the impedances at nodes A and B don't load the preceding bridge ckt calculate the op voltage V_o

- ① $R_a = R_b = R_c = R_d = 100\Omega$
 ② $R_a = R_b = R_c = 100\Omega$ $R_d = 120\Omega$

Solⁿ

$$V_B = \frac{R_c}{R_c + R_d} \cdot 10 \qquad V_o = \frac{R_2}{R_1} (V_B - V_A)$$

$$V_A = \frac{R_b}{R_a + R_b} \cdot 10 \qquad V_o = \frac{12k}{10k} (V_B - V_A)$$

Case ① $V_B = \frac{1}{2} \times 10 = 5$

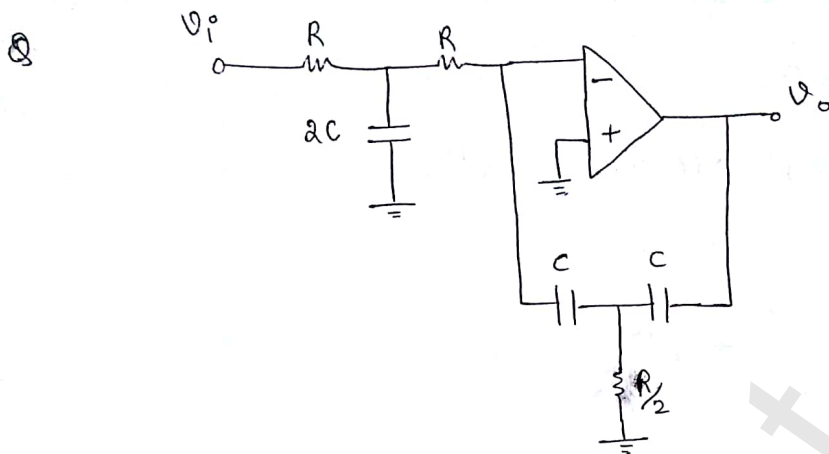
$V_A = \frac{1}{2} \times 10 = 5$

$\therefore V_o = \frac{12k}{10k} (5 - 5) = 0$

Case ② $V_B = \frac{100}{100 + 120} \times 10$

$V_A = \frac{100}{100 + 100} \times 10$

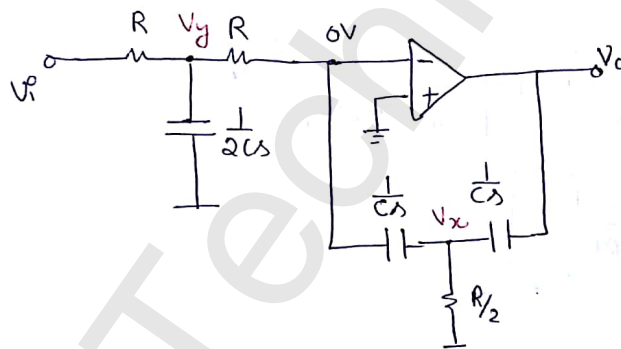
$V_o = \frac{12k}{10k} \left[\frac{100 \times 10}{220} - \frac{100 \times 10}{200} \right]$



Show that the ckt shown below act as a double integrator i.e

$$\frac{V_o(s)}{V_i(s)} = \frac{-1}{(RC)^2 s^2}$$

Solⁿ



KCL at \$V^- = 0\$

$$\frac{0 - V_y}{R} + \frac{0 - V_x}{1/Cs} = 0$$

$$\Rightarrow \frac{-V_y}{R} - V_x Cs = 0$$

$$V_x = -\frac{V_y}{RCs} \quad \text{--- (1)}$$

KCL at \$V_y\$

$$\frac{V_y}{1/2Cs} + \frac{V_y - 0}{R} + \frac{V_y - V_i}{R} = 0$$

$$\Rightarrow 2sRC V_y + \frac{1}{R} V_y + \frac{1}{R} V_y = \frac{V_i}{R}$$

$$(2sRC + 2) V_y = V_i$$

$$\Rightarrow V_i = (2 + 2sRC) (-sRC) V_x \quad \text{--- (ii)}$$

KCL at V_x :

$$\frac{V_x}{R/2} + \frac{V_x - 0}{\frac{1}{Cs}} + \frac{V_x - V_o}{\frac{1}{Cs}} = 0$$

$$\frac{2}{R} V_x + sC V_x + sC V_x - sC V_o = 0$$

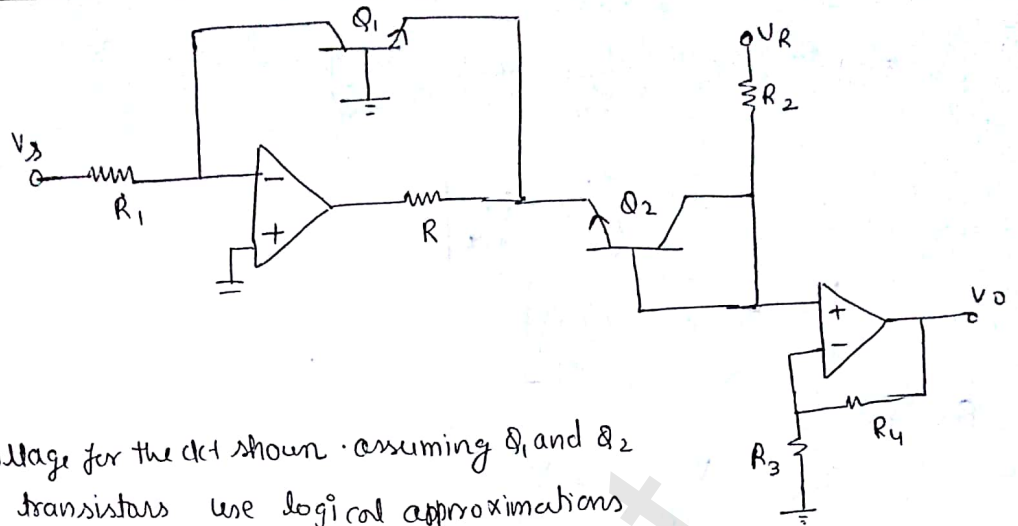
$$\frac{2}{sRC} V_x + V_x + V_x - V_o = 0$$

$$\Rightarrow V_o = \left(2 + \frac{2}{sRC}\right) V_x = \left(\frac{2 + 2sRC}{sRC}\right) V_x$$

$$V_o = \left(\frac{2 + 2sRC}{sRC}\right) \times \left[\frac{-1}{(sRC)(2 + 2sRC)}\right] V_i$$

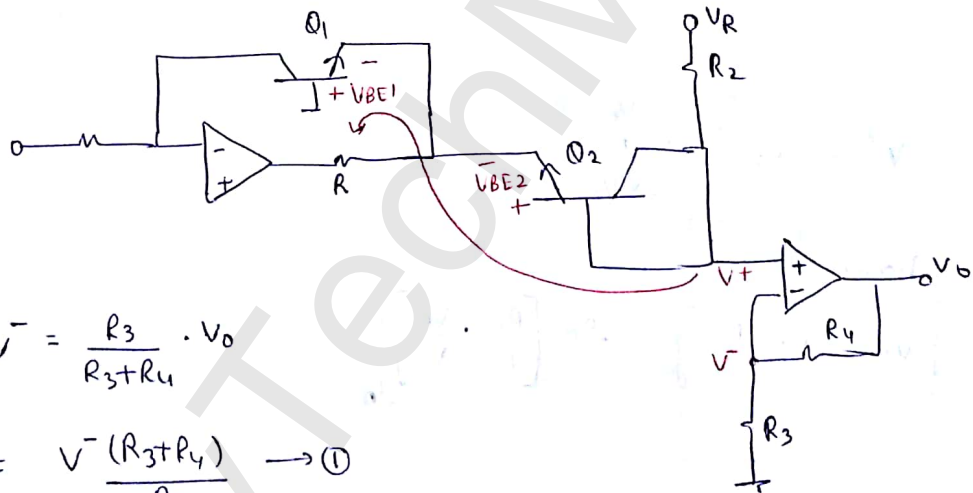
$$\boxed{\frac{V_o}{V_i} = \frac{-1}{(RC)^2 s^2}}$$

Q2



Calc the op voltage for the ckt shown. assuming Q_1 and Q_2 are matched transistors use logical approximations if any required.

Solⁿ



$$V^+ = V^- = \frac{R_3}{R_3 + R_4} \cdot V_0$$

$$V_0 = \frac{V^- (R_3 + R_4)}{R_3} \rightarrow \text{①}$$

$$V^+ = V_{BE2} - V_{BE1} \rightarrow \text{②}$$

$$I_c = I_{co} e^{V_{BE}/V_T}$$

$$V_{BE} = V_T \ln\left(\frac{I_c}{I_{co}}\right)$$

$$V_{BE1} = V_T \ln\left(\frac{I_{c1}}{I_{co}}\right)$$

$$V_{BE2} = V_T \ln\left(\frac{I_{c2}}{I_{co}}\right)$$

$$\text{So } V^+ = V_T \ln\left(\frac{I_{C2}}{I_{C0}}\right) - V_T \ln\left(\frac{I_{C1}}{I_{C0}}\right)$$

$$= V_T \ln\left[\frac{I_{C2}}{I_{C0}} \times \frac{I_{C0}}{I_{C1}}\right]$$

$$\boxed{V^+ = V_T \ln\left(\frac{I_{C2}}{I_{C1}}\right)}$$

From ckt

$$I_{C1} = \frac{V_S - 0}{R_1} = \frac{V_S}{R_1}$$

$$I_{C2} = \frac{V_R - V^+}{R_2}$$

bcz $V^+ = V_{BE2} - V_{BE1}$ so very very small

$$I_{C2} \approx \frac{V_R}{R_2}$$

$$V^+ = V_T \ln\left(\frac{\frac{V_R}{R_2}}{\frac{V_S}{R_1}}\right)$$

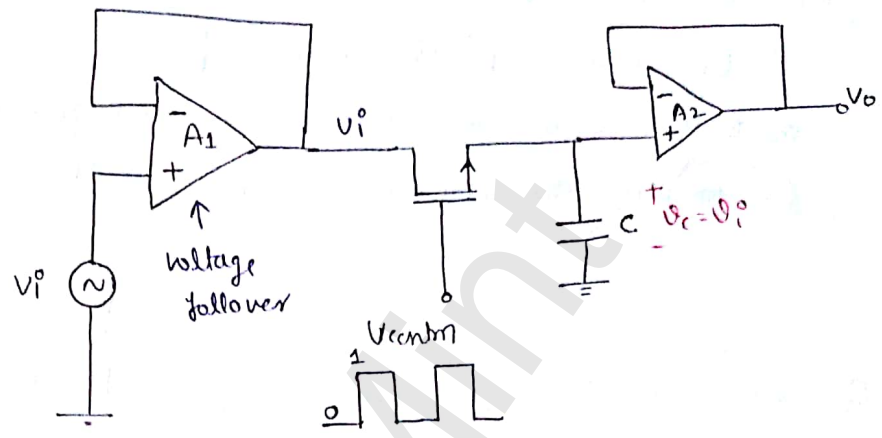
Hence

$$\boxed{V_O = \left(1 + \frac{R_4}{R_3}\right) V_T \ln\left[\frac{R_1}{R_2} \cdot \frac{V_R}{V_S}\right]}$$

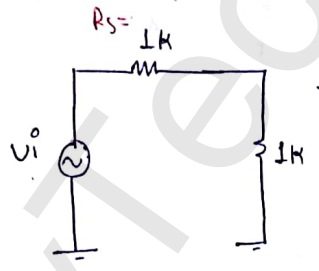
using op-amp

Q Draw the ckt dgm for Sample and Hold ckt & explain its operation

Sample and Hold ckt



above mosfet is working as a switch when $V_{control} = 1$ switch = 0.
we can't directly use V_i across MOSFET



$\frac{1}{2} V_i$

← voltage across mos switch
bez of $R_s = 1k\Omega$
इस mos के across V_i voltage को धरें
पर source (V_s) के resistance के कारण
 $\frac{1}{2} V_i$ ही मिल पा रही है इसी का source
resistance के across कोई वोल्ट नहीं मिले है

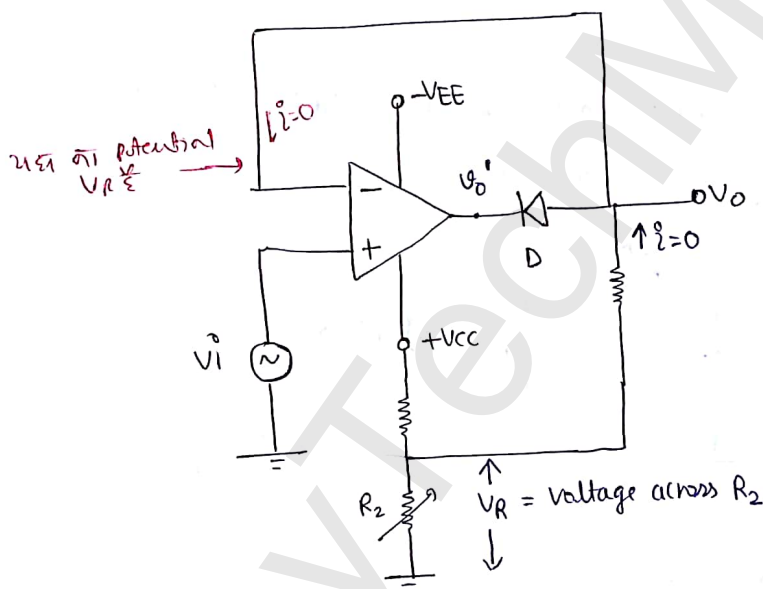
- It is used in A to D converter
- It consists of two voltage follower, a MOSFET switch and a capacitor having negligible charge leakage property.
- when $V_{control} = 1$ mos switch turns ON and V_c follows V_i this is called sampling operation
- when $V_{control} = 0$ mos switch turns off then cap^c voltage remains constant at V_c bez it doesn't have any discharging path
voltage follower A2 prevents discharge of cap^c this is called Hold operation this is resemble Sample and Hold ckt

• wsl follow A_1 is used to eliminate the effect of s_g source resistance R_s C if A_1 is not used then R_s appears in conduction path during sampling operation these by V_c can't follow V_i perfectly

• For better hold operation -

- ① low leakage cap^c should be used .
- ② MOSFET switch should have negligible leakage current .
- ③ opamp A_2 should have negligible bias current .

Q Draw the ckt dgm for clipper using op-amp & diode explain its operation



is assumed to be $i_i = 0$. then reference voltage V_R appears at the inverting terminal of the opamp and hence V_i is compared with V_R .

Case 1

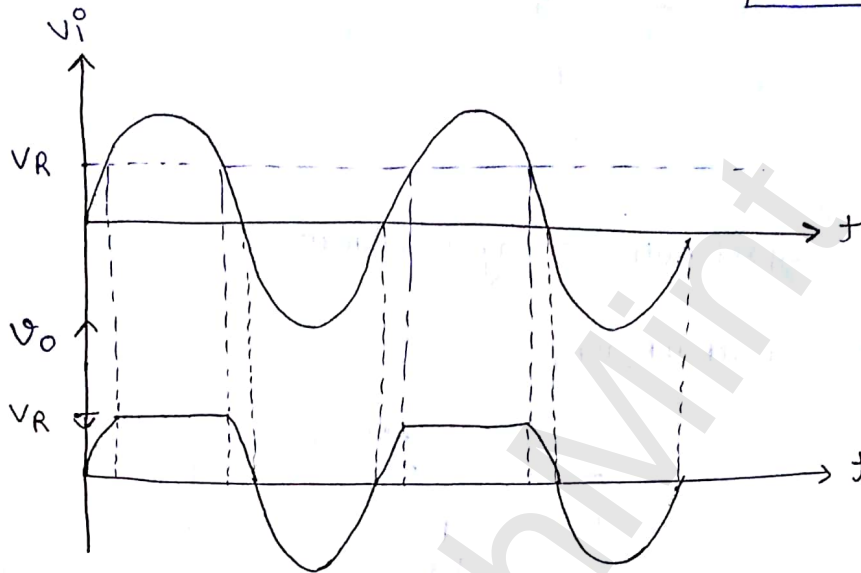
eg $V_i < V_R \Rightarrow v_o' = -ve \rightarrow D$ is FB \rightarrow replace with short ckt \rightarrow opamp act as voltage follower

$\rightarrow V_o = V_i$

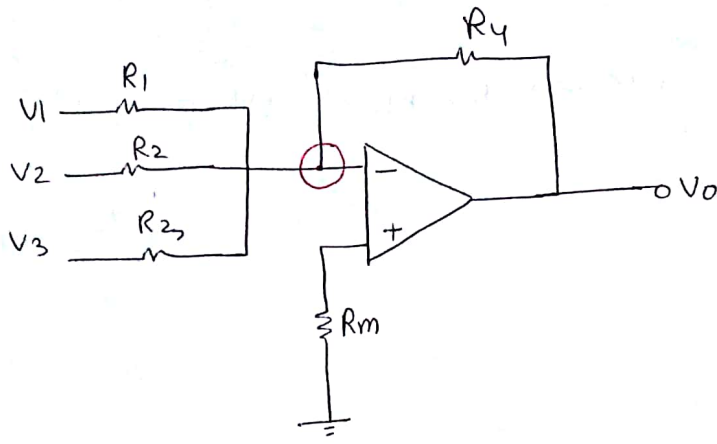
Case 2

If $V_i^o > V_R \Rightarrow V_o' = +ve \rightarrow$ Dis RB \rightarrow Replace with open ckt

$$V_o = V_R$$



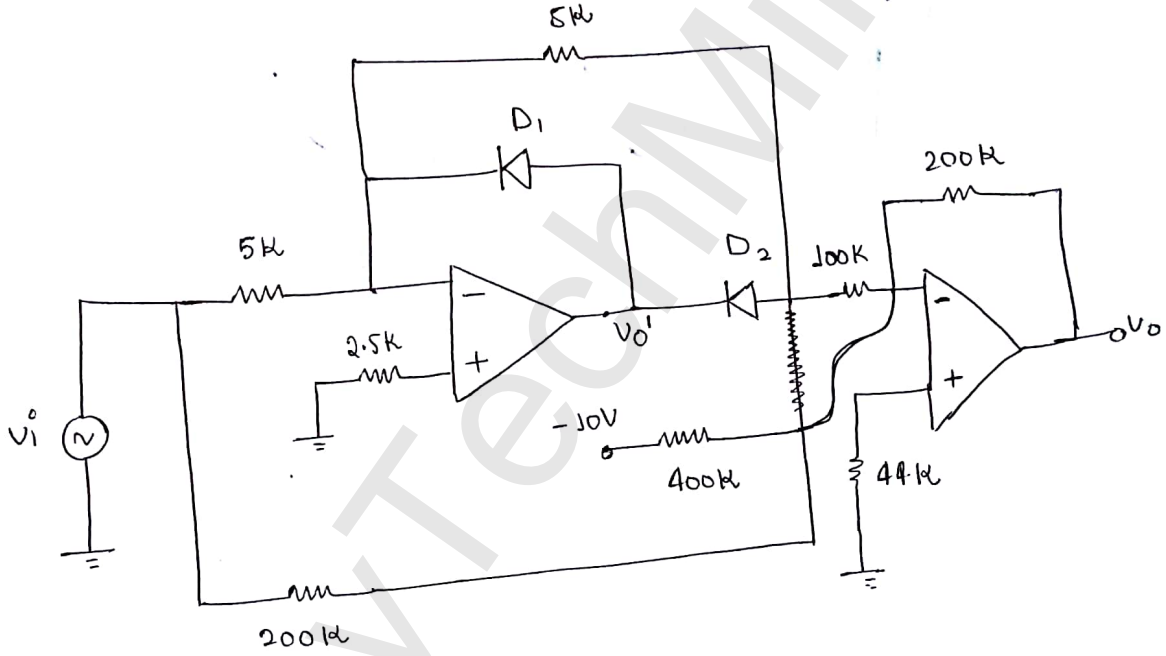
Q Note



$R_m =$ offset null balancing resistance

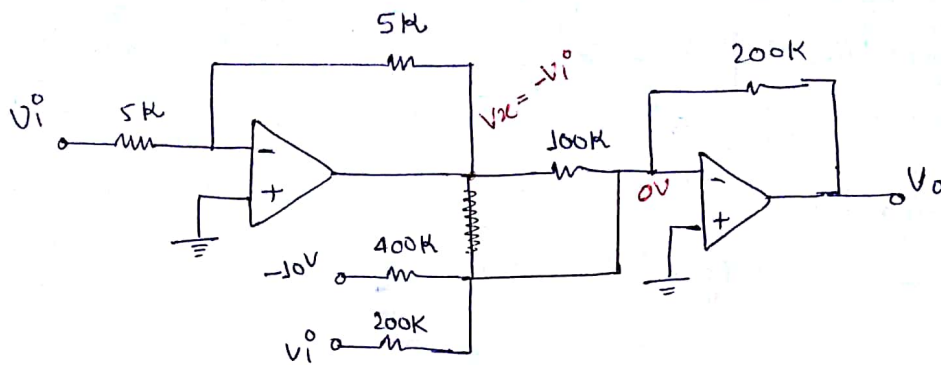
$$R_m = R_1 \parallel R_2 \parallel R_3 \parallel R_4$$

Q



Draw the transfer char^s of opamp ckt shown below assuming diodes ideal (by default considered ideal)

Solⁿ For +ve half cycle of the i/p



Very important thing to understand here is when $V_i > 0$ $V_o' < 0$, actually our 1st opamp is not in-ve feedback (it looks like but it's not) bcz the feedback is always taken from op. and feedback is not given through diode.

For $V_i > 0 \Rightarrow V_o' < 0 \Rightarrow D_1$ is off and D_2 is on

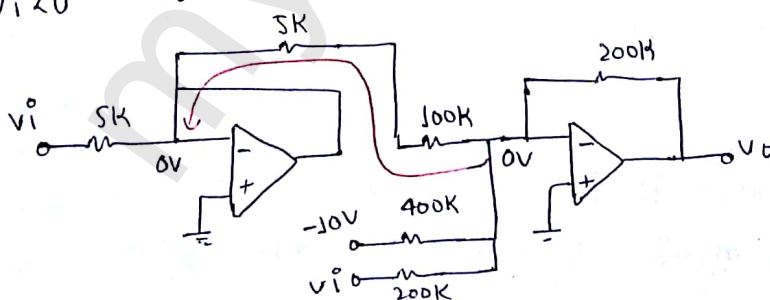
$$\frac{0 + V_i}{100k} + \frac{0 + 10}{400k} + \frac{0 - V_i}{200k} + \frac{0 - V_o}{200k} = 0$$

$$\frac{4V_i + 10 - 2V_i - 2V_o}{400k} = 0$$

$$2V_o = 2V_i + 10$$

$$V_o = V_i + 5$$

For $V_i < 0$ $V_o' > 0 \Rightarrow D_1$ is ON & D_2 is off



0V to 0V no current flow.

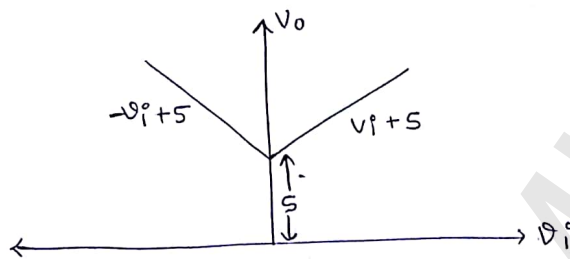
$$\frac{0 - (-10)}{400k} + \frac{0 - V_i}{200k} + \frac{0 - V_o}{200k} = 0$$

$$\frac{10 - 2V_i - 2V_o}{400k} = 0$$

$$2V_o = -2V_i + 10$$

$$V_o = -V_i + 5$$

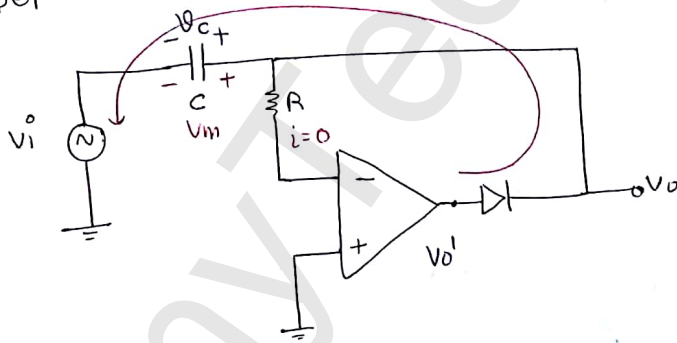
$$V_o = \begin{cases} V_i + 5 & \text{if } V_i > 0 \\ -V_i + 5 & \text{if } V_i < 0 \end{cases}$$



∴ Transfer char^c :-

Q Draw the ckt dgm for clamper kft using opamp and diode wiring.

clamper



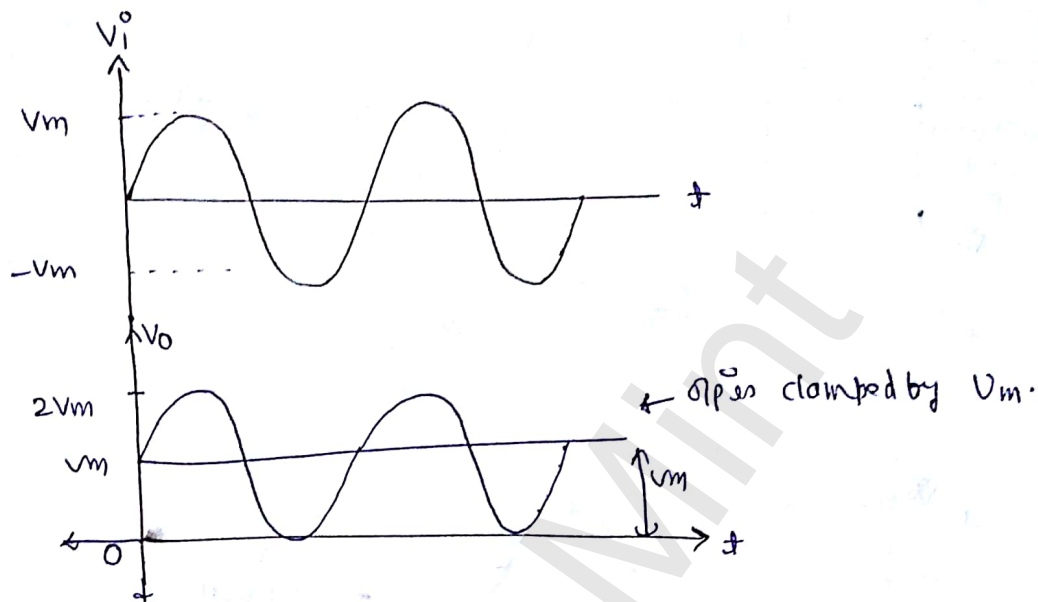
$$V_o = V_i + V_m$$

in clamper we charge C first.

At first -ve cycle of V_i diode ON and cap^c charge

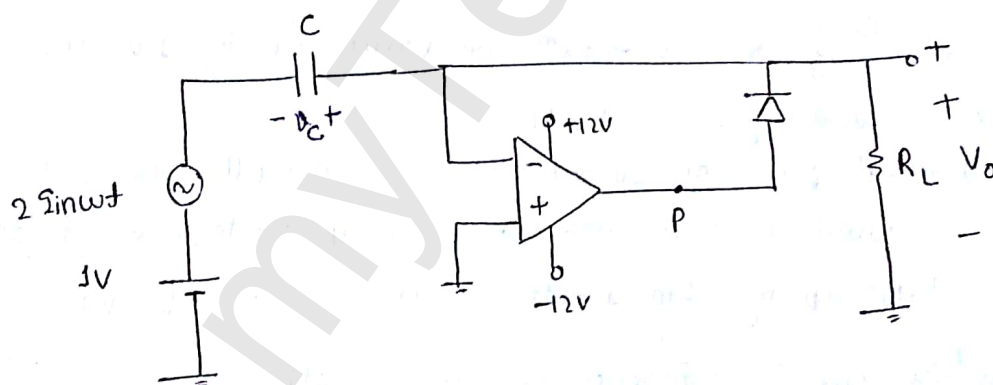
o during -ve cycle cycle of the i/p V_i opamp o/p V_o' becomes +ve and diode begins conduction hence cap^c charges through diode up to peak value of i/p voltage i.e $V_c = V_m$

during the cycle of 'ip' V_o becomes -ve and diode remains off so cap^c can't discharge therefore if cap^c is fully charged up to peak value of 'ip' then V_c remains at V_m and $V_o = V_i + V_m$



Note* if diode connection is reversed then ckt becomes -ve clamper

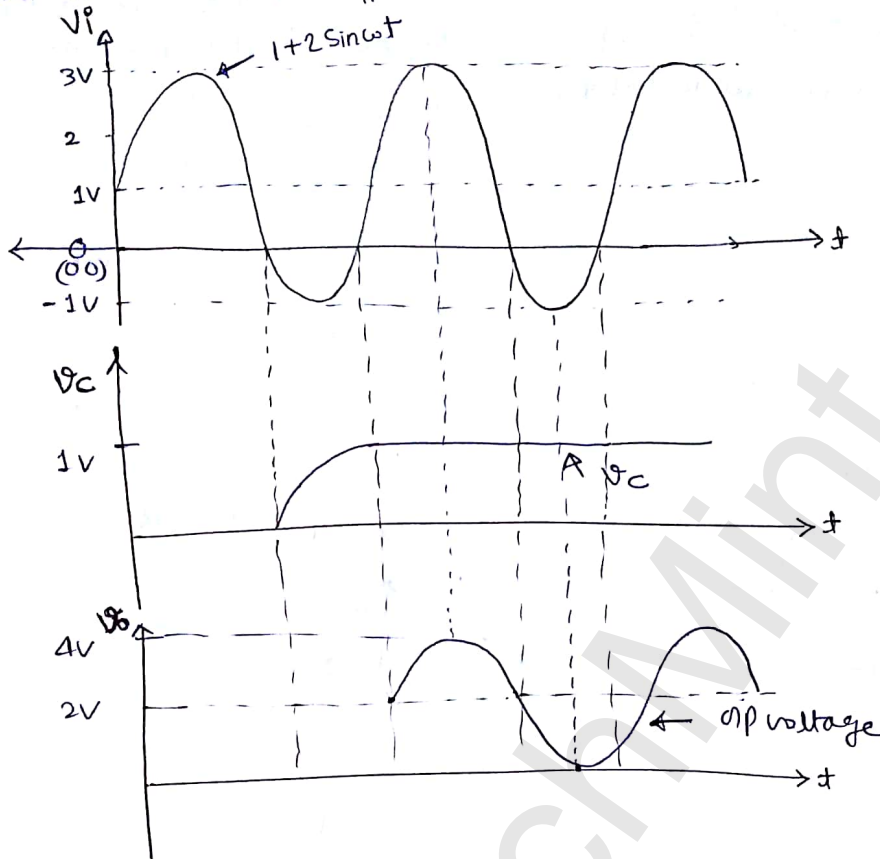
10



a voltage $V_i = 1 + 2 \sin \omega t$ is applied to the ckt shown below draw the o/p voltage and cap^c voltage waveform find the avg o/p voltage assuming $\omega = 1 \text{ rad/sec}$.

Solⁿ

1 volt dc is available in i/p



when V_i will be -ve the op of diopamp will be +ve $D \rightarrow ON$

so cap^c will charge by the max^m -ve value i.e by 1V. bcz

here max^m -ve value of V_i is 1 volt.

Now this cap^c for always remains at +1V, actually this cap^c don't discharge through R_L also. and now our i/p voltage $V_i = 1 + 2\sin\omega t$ again^t shift up by 1m 1 volt (bcz cap^c is charged by 1V)

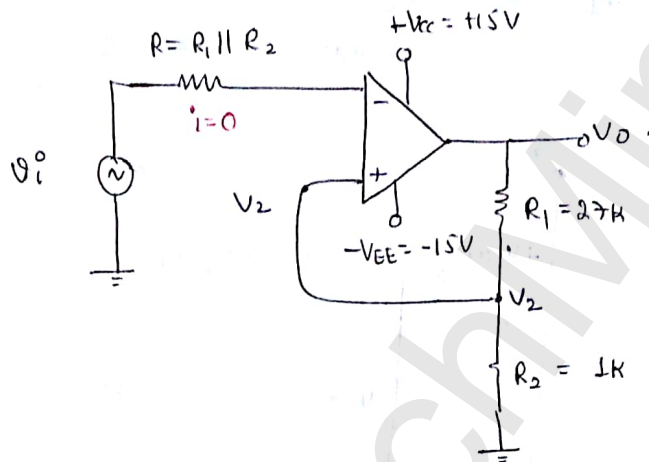
so for V_o our dc reference is now 2 volt.

10

A regenerative comparator ckt is shown below

- ① derive expression for upper threshold and lower threshold voltages and hence the value of hysteresis voltage. also calculate values of these parameters for given values of R_1 and R_2
- ② A sine wave with 2V (p-p) amplitude and 1 kHz f_m is applied at the ip of the ckt plot the ip and op waveforms.

Schmitt trigger



Schmitt trigger also called Regenerative comparator

$$V_d = V^+ - V^-$$

$$V_d = V_2 - V_i$$

$$\text{if } V_d > 0 \Rightarrow V_o = +V_{sat}$$

$$\text{if } V_d < 0 \Rightarrow V_o = -V_{sat}$$

$$V_2 = \frac{R_2}{R_1 + R_2} \cdot V_o$$

$$\text{if } V_o = +V_{sat}$$

$$\text{then } V_2 = \frac{R_2 \cdot V_{sat}}{R_1 + R_2} = V_{UT}$$

$$\text{if } V_o = -V_{sat}$$

$$V_2 = \frac{R_2 (-V_{sat})}{R_1 + R_2} = V_{LT}$$

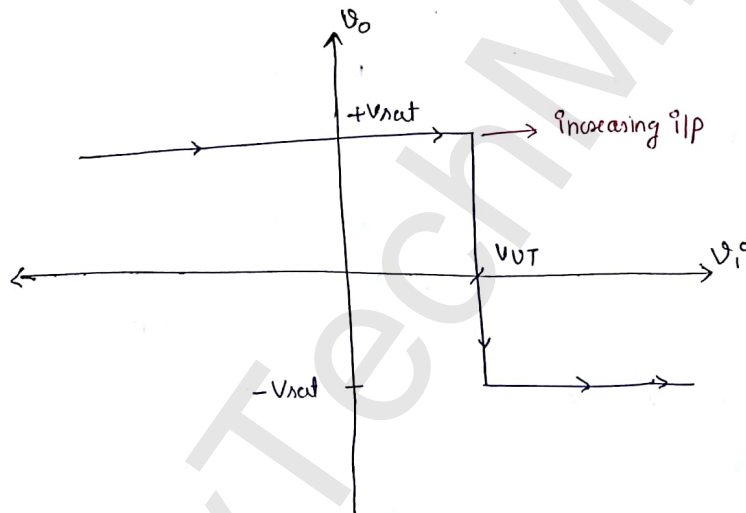
Case 1: Assume $v_o = +V_{sat}$

$$\text{then } V_2 = V_{UT} = \frac{R_2}{R_1 + R_2} \cdot V_{sat} = \frac{15 \times 1}{28} = 0.54 \text{ V}$$

$$V_d = V_{UT} - v_i$$

eg $v_i < V_{UT} \Rightarrow v_o = +ve \Rightarrow v_o = +V_{sat}$
→ means o/p remains at $+V_{sat}$

eg $v_i > V_{UT} \Rightarrow v_d = -ve \Rightarrow v_o = -V_{sat}$
→ means o/p changes from $+V_{sat}$ to $-V_{sat}$



Note* For an increasing i/p sly o/p voltage changes from $+V_{sat}$ to $-V_{sat}$ only at V_{UT}

Case 2

$$V_o = -V_{sat}$$

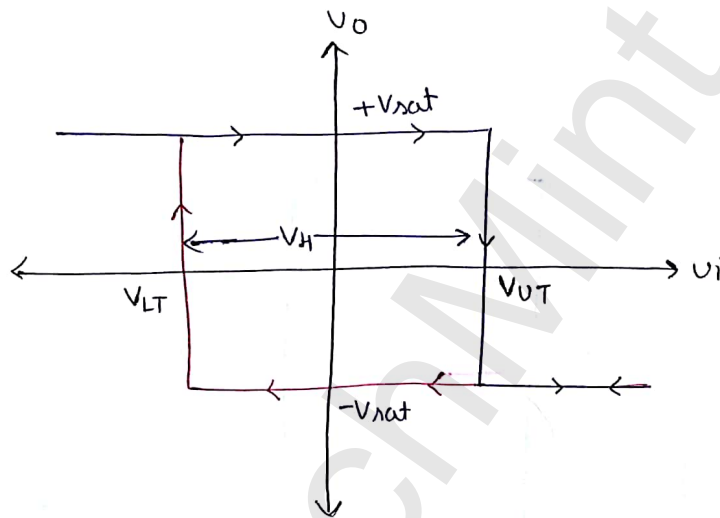
then

$$V_2 = V_{LT} = \frac{-R_2}{R_1 + R_2} \cdot V_{sat}$$

$$V_d = V_{LT} - V_i$$

If $V_i > V_{LT} \Rightarrow V_d = -ve \Rightarrow V_o = -V_{sat}$... op remains at $-V_{sat}$

If $V_i < V_{LT} \Rightarrow V_d = +ve \Rightarrow V_o = +V_{sat}$... op changes from $-V_{sat}$ to $+V_{sat}$



Note* For a rising i/p voltage, o/p changes from $-V_{sat}$ to $+V_{sat}$ only at

$$V_i = V_{LT}$$

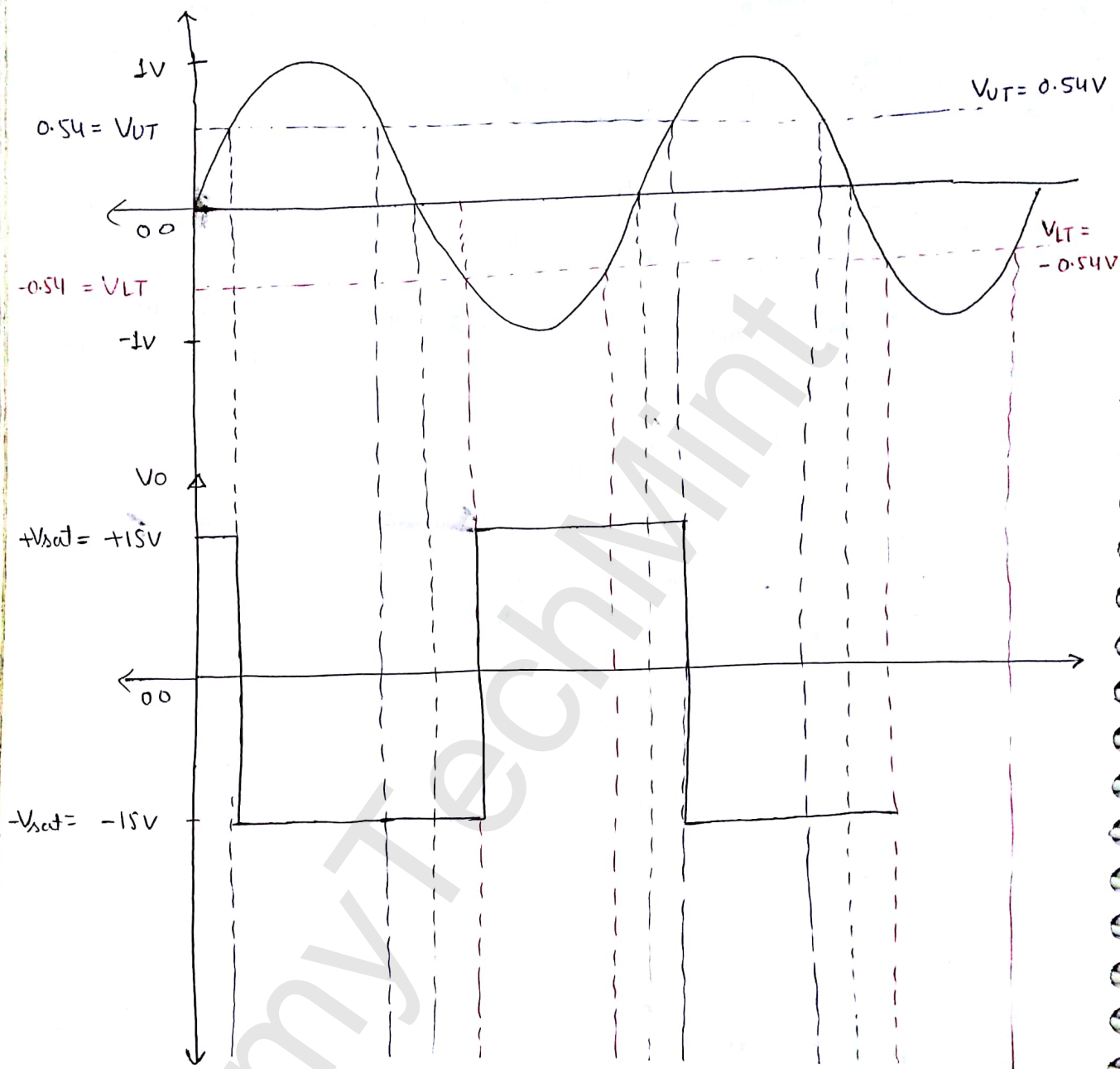
$V_H \Rightarrow$ Hysteresis voltage

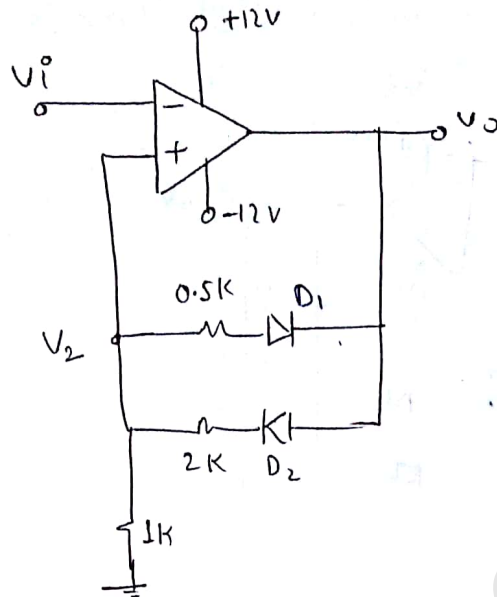
$$V_H = V_{UT} - V_{LT}$$

$$\frac{R_2}{R_1 + R_2} \cdot V_{sat} - \frac{R_2}{R_1 + R_2} \cdot V_{sat}$$

$$V_H = \frac{2 R_2 V_{sat}}{R_1 + R_2}$$

V_{sat} if not given, taken as V_{CC}





Q. Drawn are ideal plot transfer characteristic

Solⁿ

$$\text{If } V_o = +V_{sat} = +12V$$

$$\text{then } V_2 = V_{UT}$$

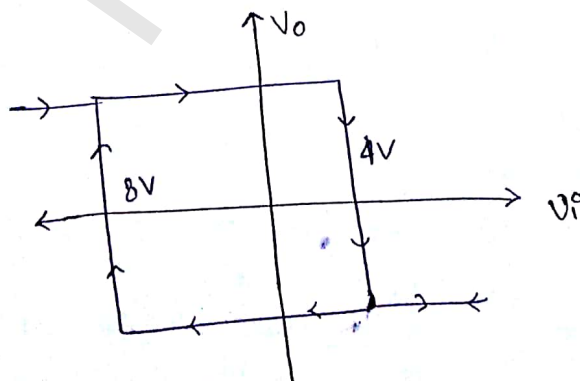
In this case D_1 is RB and D_2 is FB

$$V_2 = V_{UT} = \frac{1K}{1K + 2K} \times 12 = 4V$$

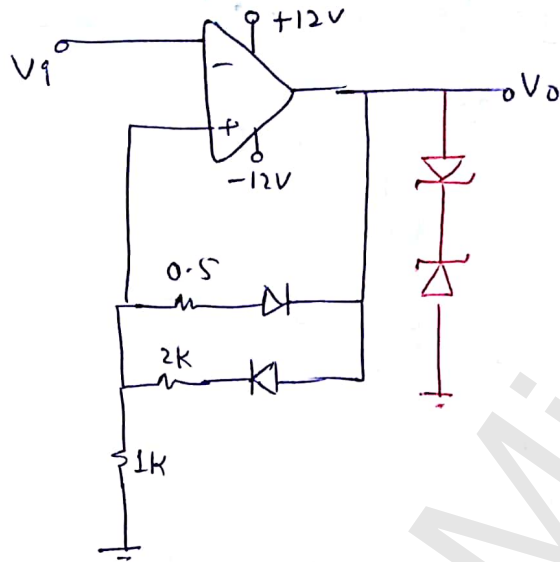
$$\text{If } V_o = -V_{sat} = -12V$$

In this case D_1 is FB and D_2 is RB.

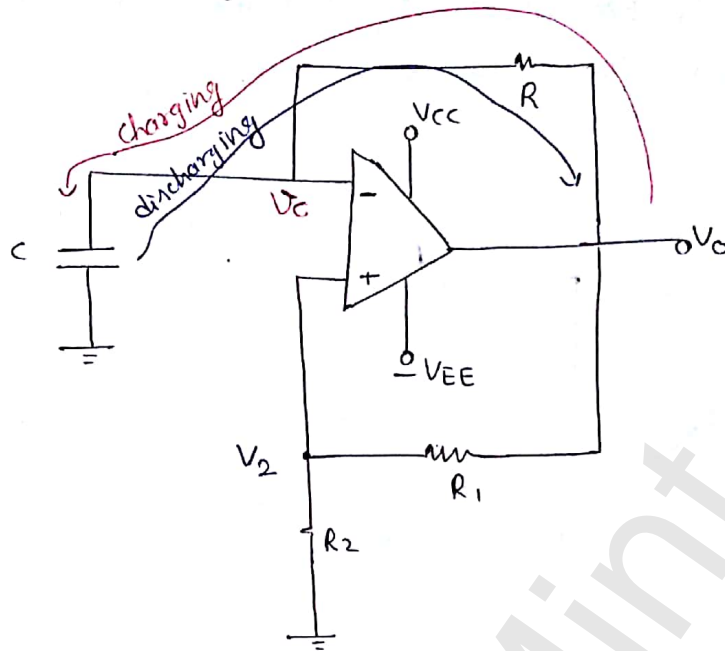
$$V_2 = V_{LT} = \frac{1K}{1K + 0.5K} \times (-12) = -8V$$



Note^x If we want to take less than V_{sat}
then we add.



Q Explain the working of Astable multivibrator



$$V_2 = \frac{R_2}{R_1 + R_2} \cdot V_0$$

β

If $V_0 = +V_{sat}$ then $V_2 = +\beta V_{sat}$

If $V_0 = -V_{sat}$ then $V_2 = -\beta V_{sat}$

Case 1:

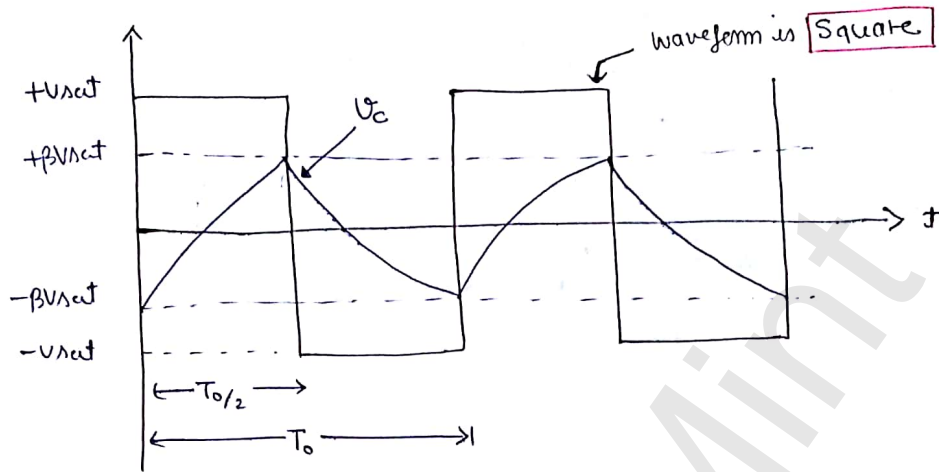
Assume $V_0 = +V_{sat}$ then $V_d = \beta V_{sat} - V_c$

In this case cap^e charge through resistance R and V_c continues to increase till βV_{sat}

If V_c becomes slightly \downarrow than βV_{sat} then V_d becomes $-ve$ and V_0 changes to $-V_{sat}$

Case 2 If $V_0 = -V_{sat}$ then $V_2 = -\beta V_{sat}$
and $V_d = (-\beta V_{sat}) - V_c$

In this case cap' discharges through resistance R and V_c continuously less till $-\beta V_{sat}$. If V_c becomes slightly less than $-\beta V_{sat}$ then V_d becomes +ve and V_o changes to $+V_{sat}$



calⁿ of T_0 or f_0

For capacitor

$$V_{\text{initial}} = -\beta V_{\text{sat}}$$

$$V_{\text{final}} = +V_{\text{sat}}$$

$$\tau = RC$$

$$V_c(t) = V_{\text{final}} + [V_{\text{initial}} - V_{\text{final}}] e^{-t/\tau}$$

$$V_c(t) = V_{\text{sat}} + [-\beta V_{\text{sat}} - V_{\text{sat}}] e^{-t/RC}$$

$$V_c(t) = V_{\text{sat}} - V_{\text{sat}}(1+\beta) e^{-t/RC}$$

but at $t = \frac{T_0}{2}$; $V_c(\frac{T_0}{2}) = +\beta V_{\text{sat}}$

$$\text{so } +\beta V_{\text{sat}} = V_{\text{sat}} [1 - (1+\beta) e^{-T_0/2RC}]$$

$$(1+\beta) e^{-T_0/2RC} = 1 - \beta$$

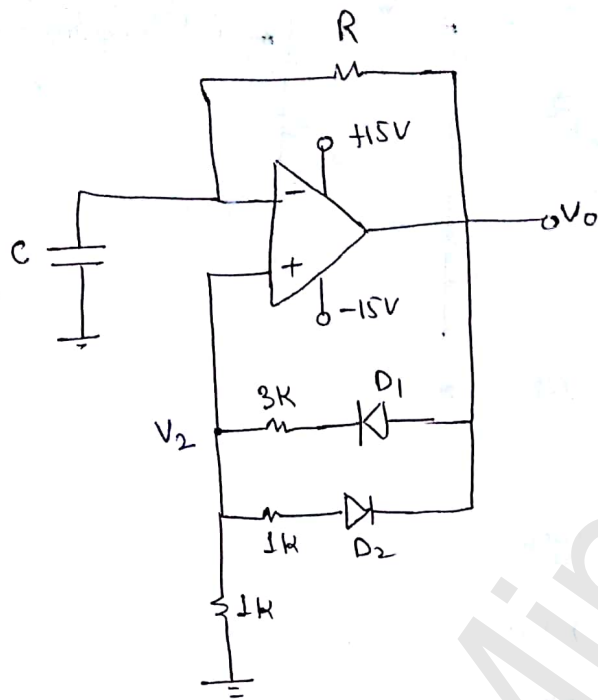
$$e^{T_0/2RC} = \frac{1+\beta}{1-\beta}$$

$$\Rightarrow T_0 = 2RC \ln\left(\frac{1+\beta}{1-\beta}\right)$$

$$\text{and } f_0 = \frac{1}{T_0}$$

$$\beta = \frac{R_2}{R_1 + R_2}$$

Q



An oscillator circuit using ideal op-amp and diode is shown below. The time duration for the ^{part of the cycle is} Δt_1 and for -ve part is Δt_2 . Then calc the value of $e^{(\Delta t_1 - \Delta t_2)/RC}$

Solⁿ here Δt_1 and Δt_2 are not equal bcz $+V_{sat}$ and $-V_{sat}$ magnitude are different.

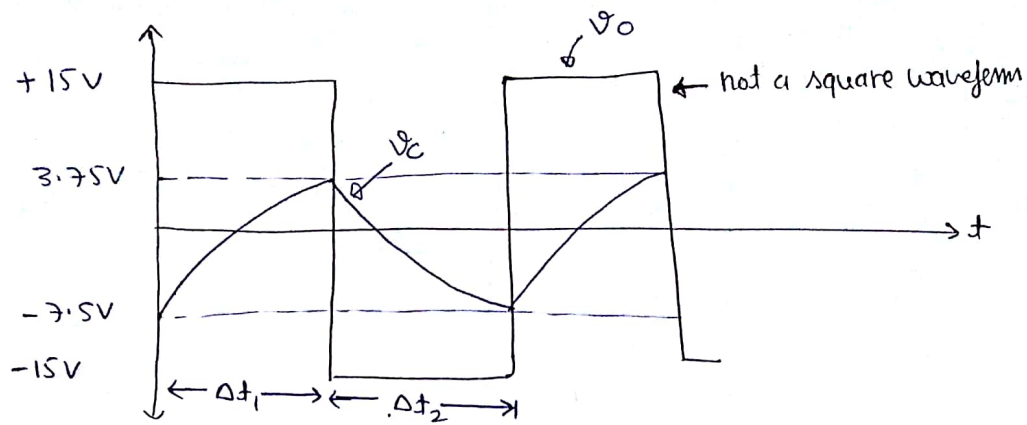
$$\text{If } V_0 = +V_{sat} = +15$$

$$V_2 = V_{UT} = \frac{1K}{1K+3K} \times 15$$

$$V_{UT} = 3.75 \text{ V}$$

$$\text{If } V_0 = -V_{sat} = -15$$

$$V_2 = V_{LT} = \frac{1K}{1K+1K} (-15) = -7.5 \text{ V}$$



Case 1 During +ve cycle

$$V_{\text{initial}} = -7.5V$$

$$V_{\text{final}} = 15V$$

$$V_c(t) = 15 + [-7.5 - 15] e^{-t/RC}$$

$$= 15 - 22.5 e^{-t/RC}$$

$$\text{at } t = \Delta t_1$$

$$3.75 = 15 - 22.5 e^{-\Delta t_1/RC}$$

$$e^{-\Delta t_1/RC} = \frac{15 - 3.75}{22.5}$$

$$e^{-\Delta t_1/RC} = 0.5$$

$$\boxed{e^{\Delta t_1/RC} = 2}$$

Case 2 During -ve cycle

$$V_{\text{initial}} = 3.75$$

$$V_{\text{final}} = -15V$$

$$V_c(t) = -15 + [3.75 + 15] e^{-t/RC}$$

$$= -15 + 18.75 e^{-t/RC}$$

$$\text{at } t = \Delta t_2$$

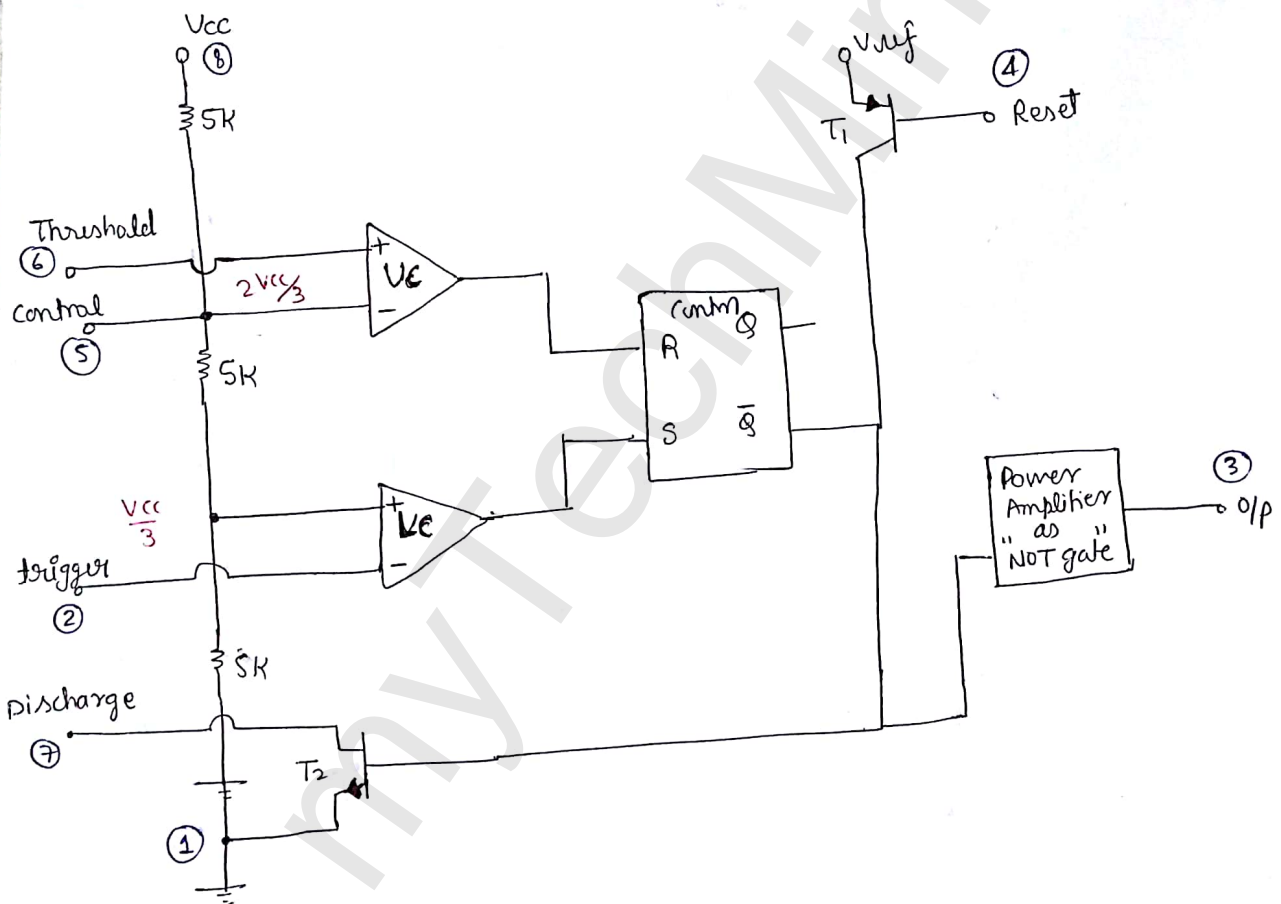
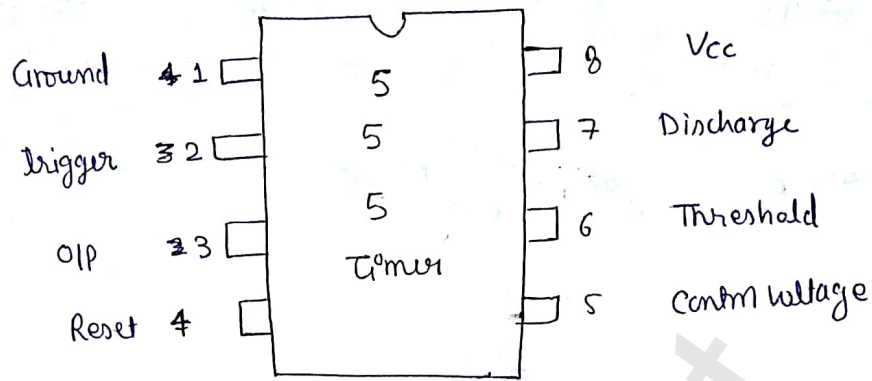
$$-7.5 = -15 + 18.75 e^{-\Delta t_2/RC}$$

$$\boxed{e^{-\Delta t_2/RC} = 0.4}$$

$$e^{(\Delta t_1 - \Delta t_2)/RC} = e^{\Delta t_1/RC} \times e^{-\Delta t_2/RC}$$

$$= 2 \times 0.4$$

$$= 0.8 \text{ Answer}$$



Two opamps in open loop so work as comparators

RS F/F

Power amp^y are CE type if we give \bar{Q} so that o/p we get is in phase (amplified). bcz CE gives 180° phase shift and \bar{Q} also will give 180° phase shift so net phase shift will be 0° .

if threshold $> \frac{2V_{cc}}{3}$

Two comparators are used internally used as upper comparator &

Lower comparator

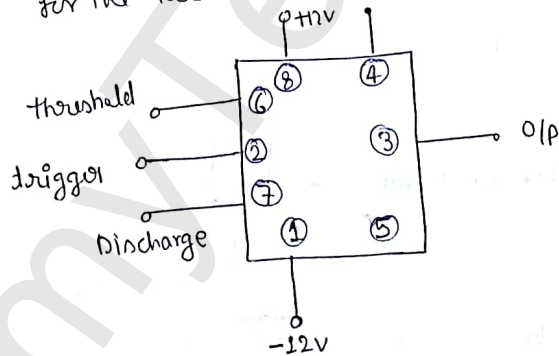
if $V^+ > V^-$ $V_{comp} = 1$ → o/p of comparator

if $V^+ < V^-$ $V_{comp} = 0$

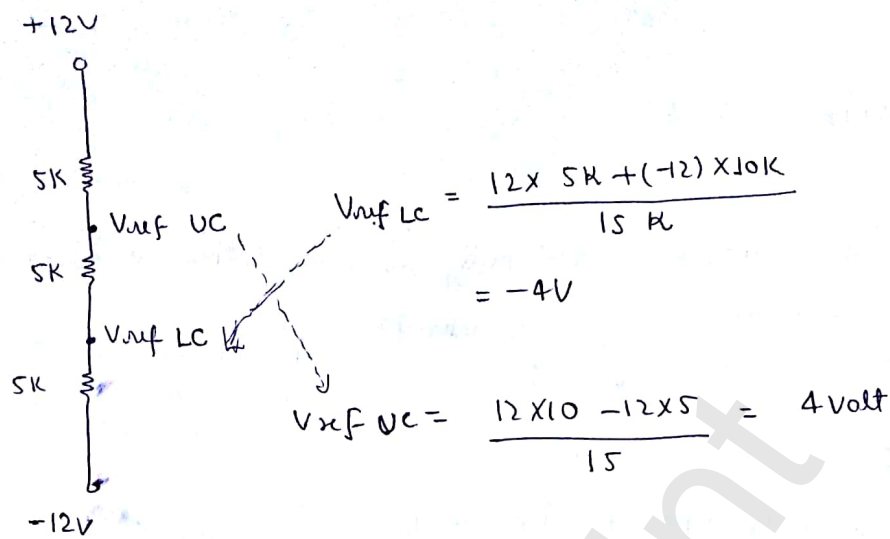
comparator o/p compares the i/p for SR

(S) V_{OLC}	(R) V_{OUC}	Q_{n+1}
0	0	Q_n
0	1	0
1	0	1
1	1	X (Not allowed)

Question: The IC timer 555 is shown below. determine the reference level for the two comparators inside the chip justify your

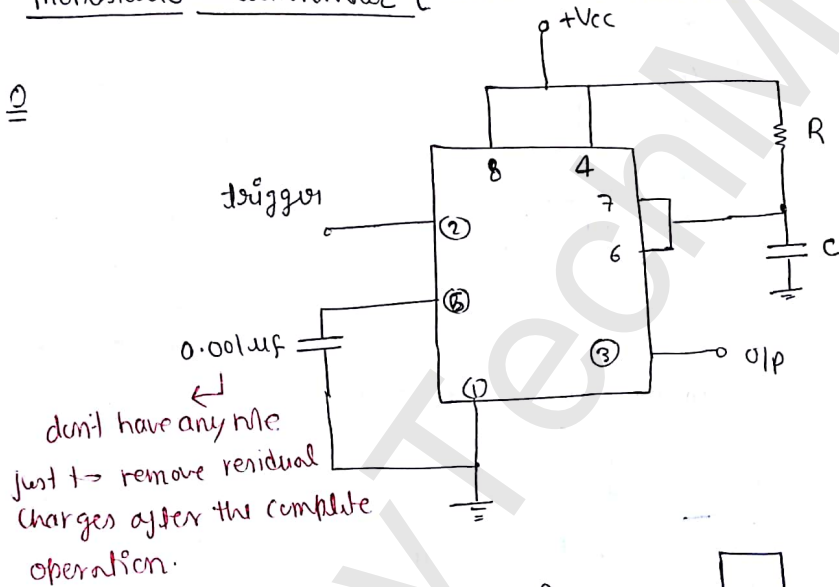


Answer by drawing a block diagram of internal ckt of IC timer 555

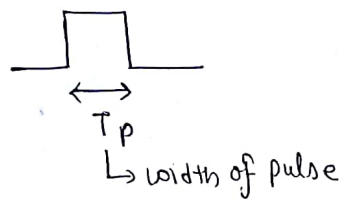


Monostable Multivibrator [we can make monostable Multivibrator from 555 IC]

110

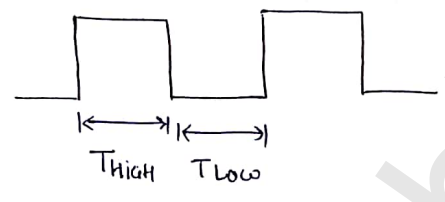
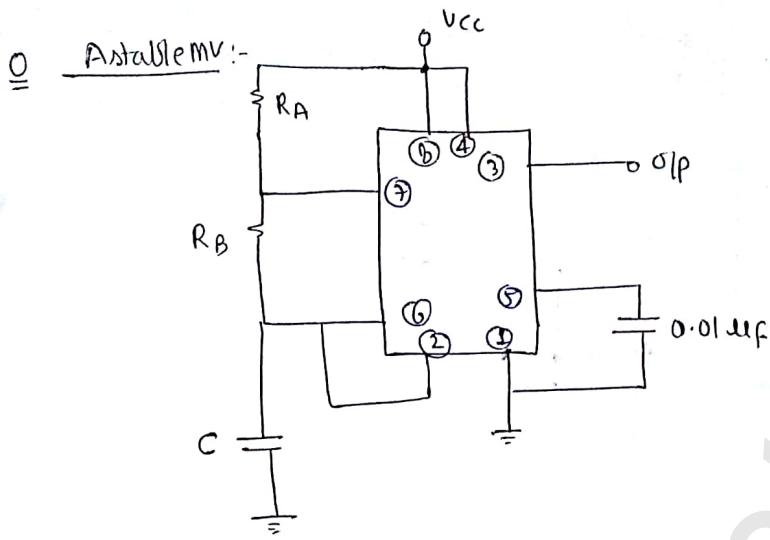


it generates a pulse waveform



$$T_p = RC \ln 3$$

$$T_p = 1.1 RC$$

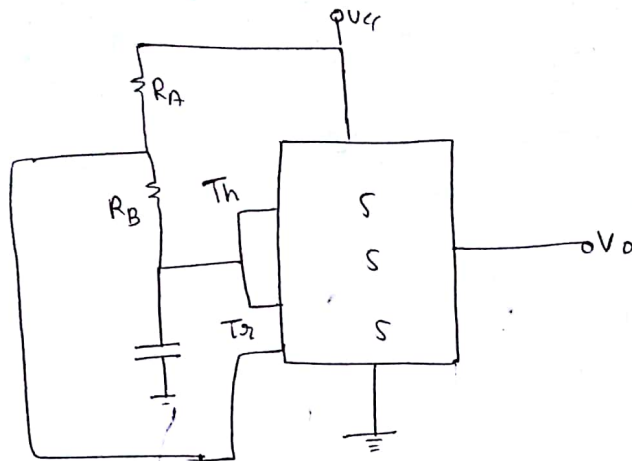


$$T_{high} = 0.69(R_A + R_B)C$$

$$T_{low} = 0.69 R_B C$$

$$T_0 = 0.69(R_A + 2R_B)C$$

$$f_0 = \frac{1}{T_0}$$



555 Timer IC is connected as Astable MV IC the value of cap^c $C = 10\text{nf}$ the value of resistor R_A and R_B for f_0 of 10kHz and duty cycle of 0.75 for the op waveform are

Solⁿ

$$C = 10\text{nf}$$

$$D_T = 0.75$$

$$f_0 = 10\text{kHz}$$

$$T_0 = \frac{1}{f_0} = \frac{1}{10} = 0.1\text{msec}$$

$$D_T = \frac{T_{\text{ON}}}{T_0} = \frac{T_{\text{HIGH}}}{T_0} =$$

$$T_0 \cdot 0.75 = T_{\text{HIGH}} =$$

$$T_{\text{HIGH}} = 0.1 \times 0.75 \times 10^{-3}$$

$$T_{\text{HIGH}} = 0.69(R_A + R_B)C = 0.75 \times 0.1 \times 10^{-3} \quad \text{--- (i)}$$

$$\frac{T_{\text{LOW}}}{T_0} = 0.25$$

$$T_{\text{LOW}} = 0.25 \times 0.1 \times 10^{-3} = 0.69 R_B C \quad \text{--- (ii)}$$